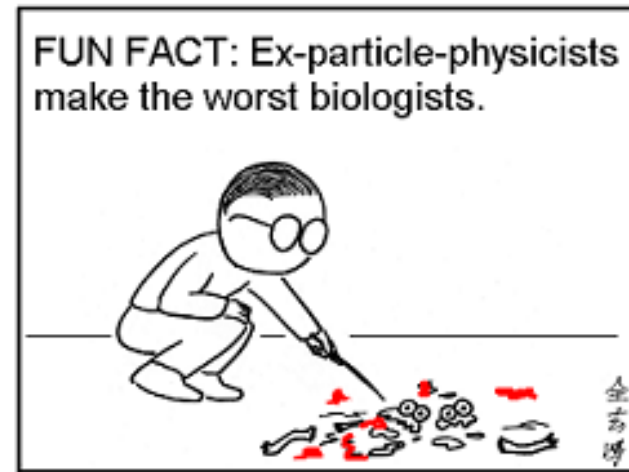
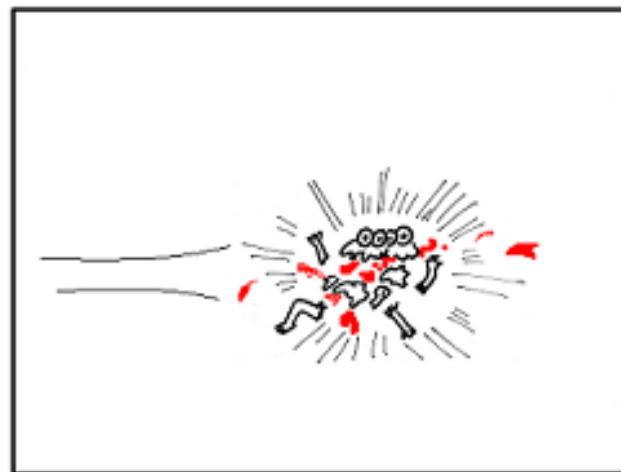
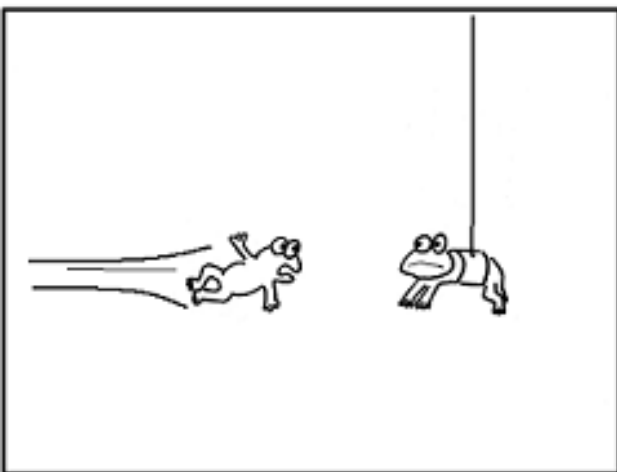
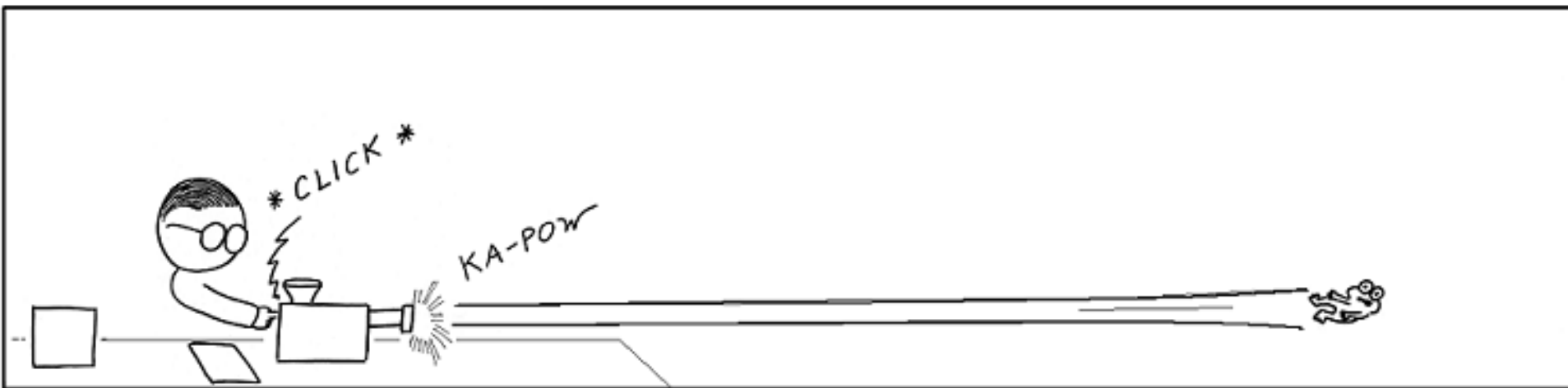
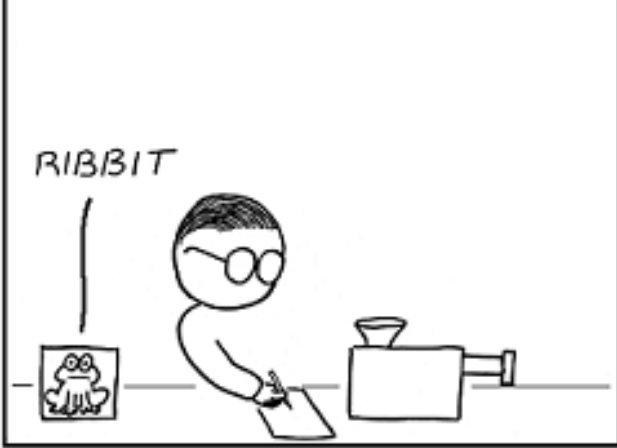


# Octupole bands in the mass 160 region

M.A. Stankiewicz

University of Cape Town and iThemba LABS





# Nuclear deformations

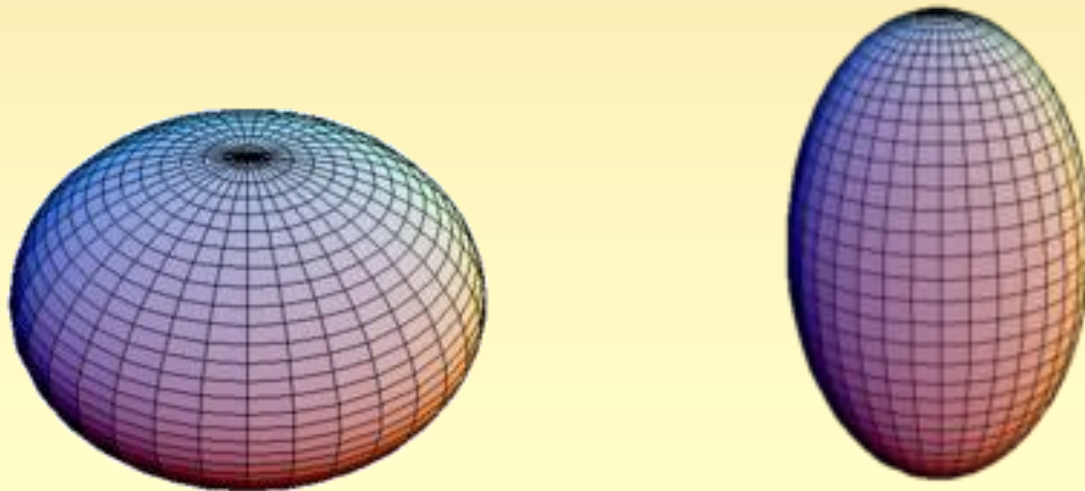
- Have ~150 body problem, with two sets of fermions. Use collective approach
- Apply liquid drop model to surface
- General expansion:

$$R(\theta, \phi, t) = R_0 \left( 1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \alpha_{\lambda\mu}(t) Y_{\lambda\mu}(\theta, \phi) \right)$$

$$R(\theta, \phi) = R_0 \left( 1 + \sum_{\lambda=0}^4 \sum_{\mu=0}^{\lambda} \alpha_{\lambda\mu} Y_{\lambda\mu}(\theta, \phi) \right)$$

# Nuclear deformations

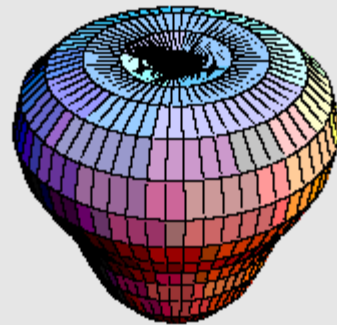
- The monopole and dipole deformations are scaling and translational – do not effect shape
- Ground state, most even-even nuclei are quadrupole-deformed:





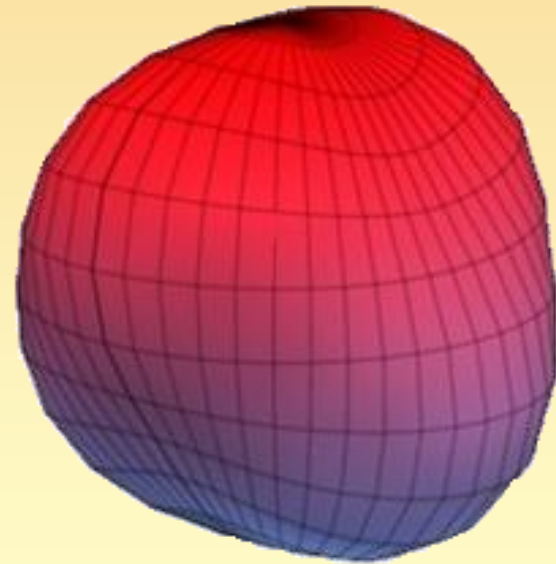
# Octupole deformations

- Standard octupole deformation is  $\alpha_{30} \neq 0$
- Corresponds to ‘pear’ shape:
- Onto this we can superimpose a vibration:



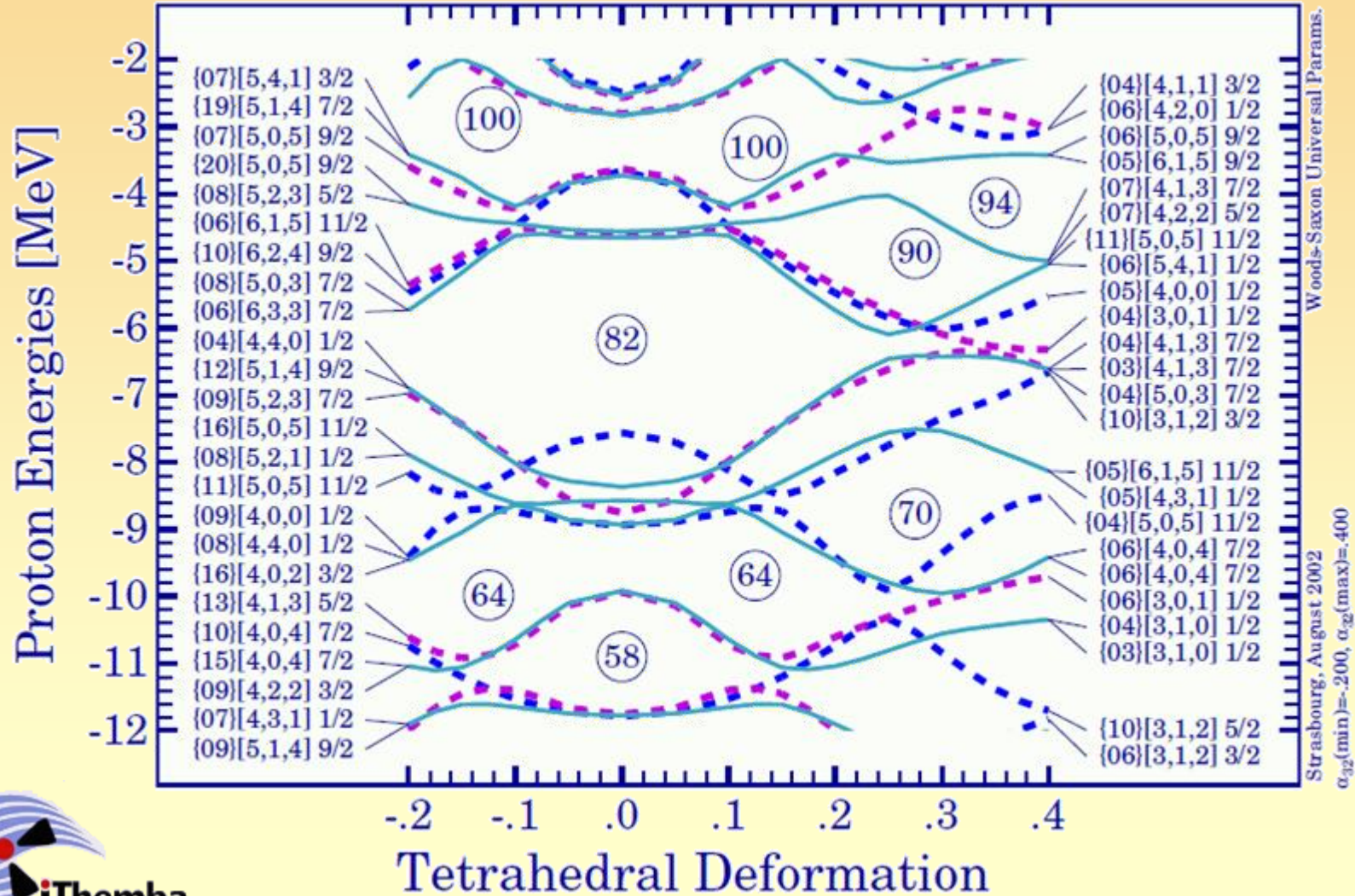
# Tetrahedral deformations

- It is also possible to have  $\alpha_{32} \neq 0$
- However, for this to exist, cannot have a quadrupole moment.



So  $\alpha_{20} = 0$

# Where to find them?



# Look for doubly-magic nuclei

- Looking for shell-gaps in the tetrahedral nucleon energies.
- There are some at 64 and 70, then 90 and 94
- So focus in the  $A \sim 160$  region:  
 $^{154}\text{Gd}$ ,  $^{158}\text{Gd}$ ,  $^{160}\text{Yb}$ ,  $^{164}\text{Yb}$
- Next deformed shell gaps are 112, 136, 142, so can look in  $^{232}\text{Th}$  region.



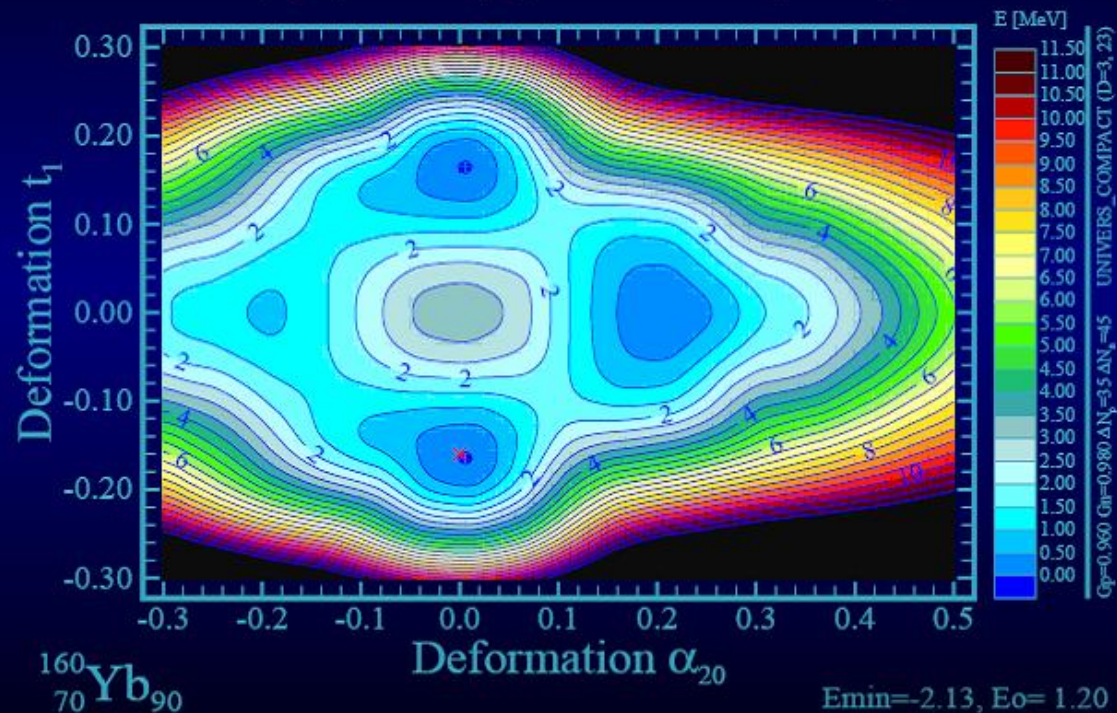
# Calculations were promising:

Tetrahedral Nuclei - Theoretical Predictions

Total Energies  
Experiment

## Survey of Doubly-Magic Tetrahedral Symmetry Nuclei

$E(\text{fyu}) + \text{Shell}[e] + \text{Correlation}[\text{PNP}]$

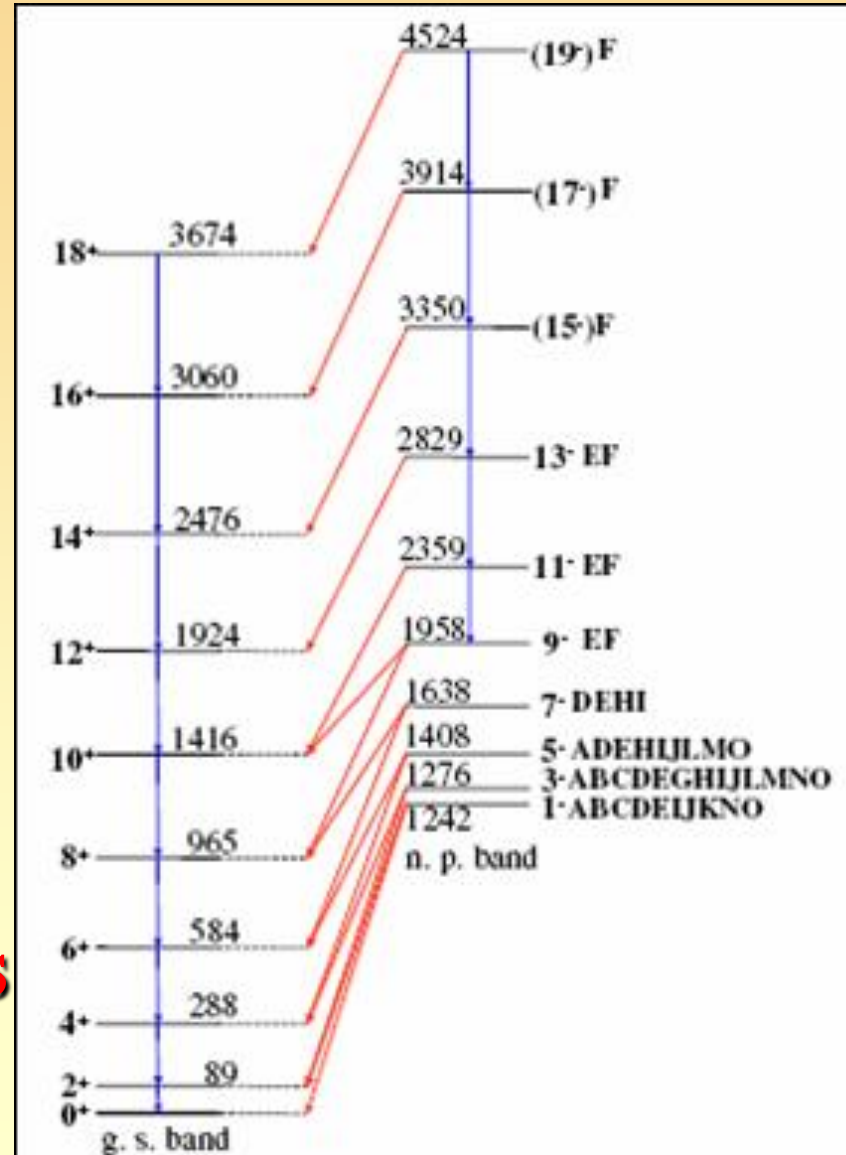


# What to look for?

- With zero quadrupole moment, there will be no in-band E2 transitions

Generally thought of as octupole vibrations, but now:

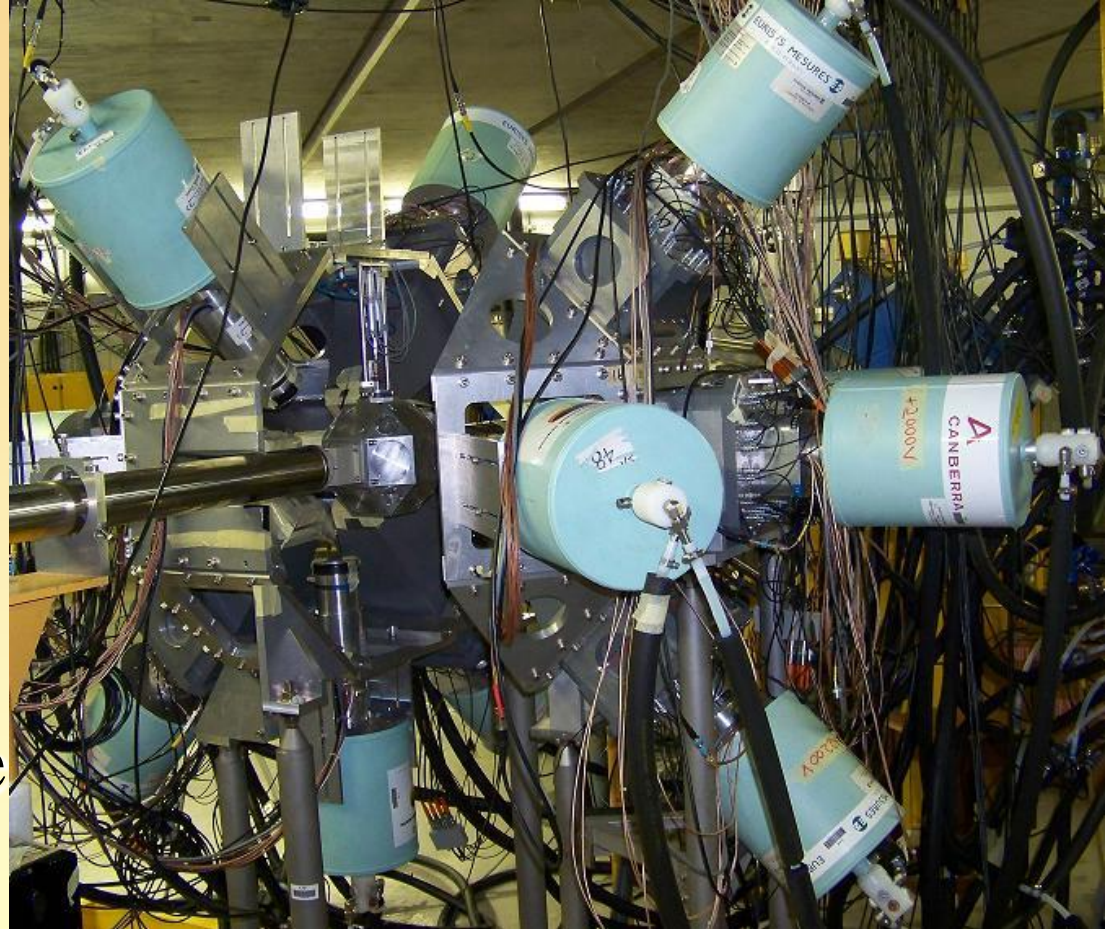
**Tetrahedral candidates**





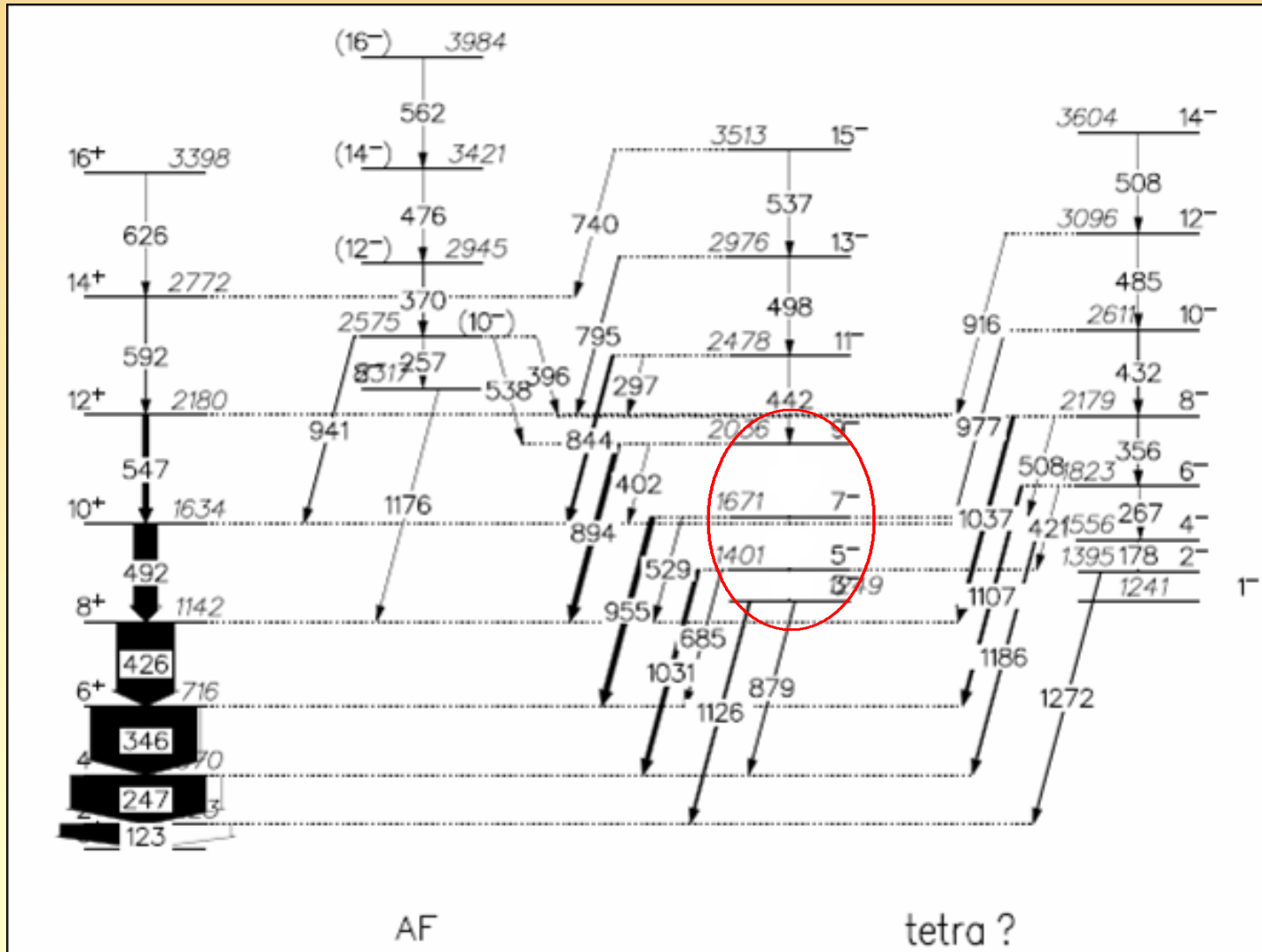
# AFRODITE setup

- HPGe detectors:  
9 Clover and  
up to 8 LEPS
- Collect up to  
 $10^9$   $\gamma\gamma$  coincidence  
events / weekend



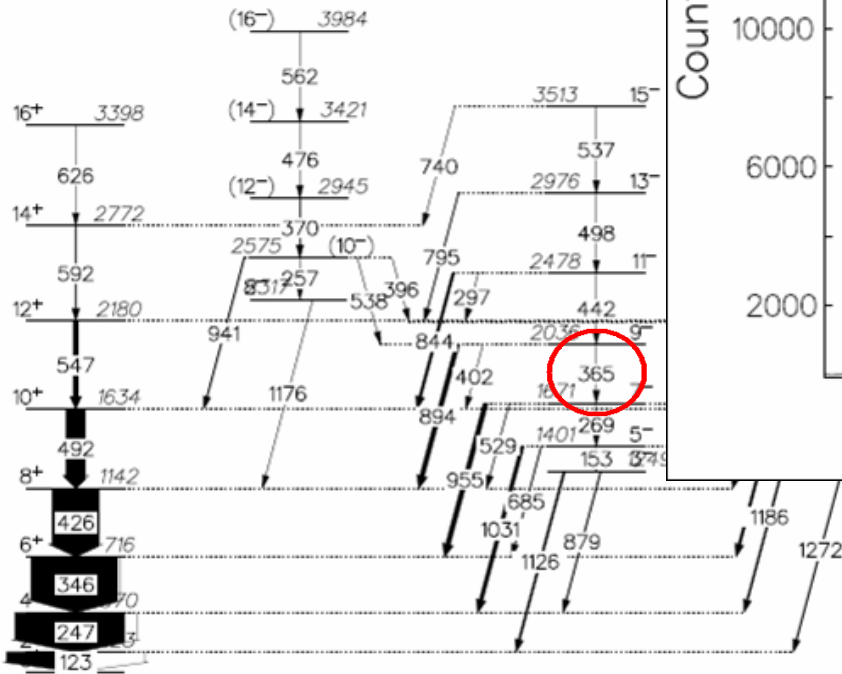
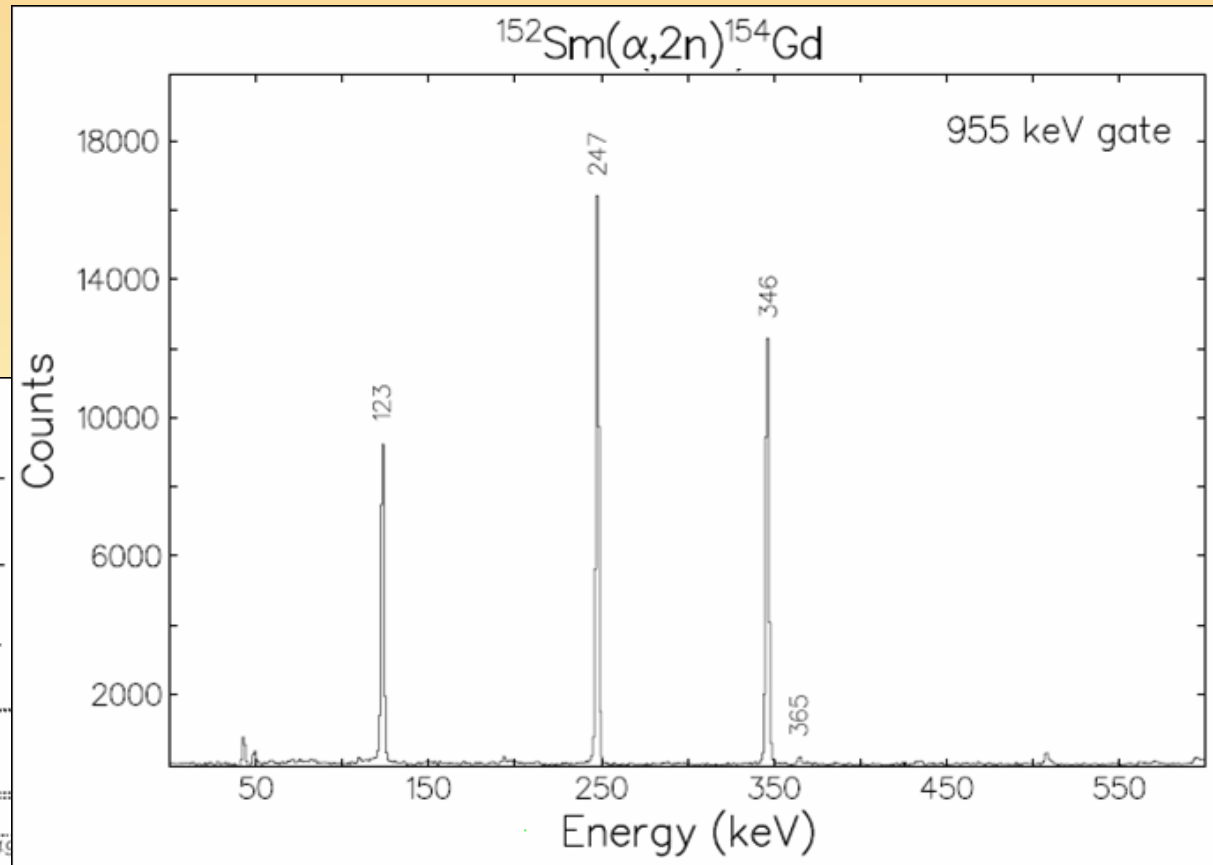


# $^{152}\text{Sm}(\alpha, 2n)^{154}\text{Gd}$ :



# Missing transitions?

- Is there a  $9 \rightarrow 7$ ?



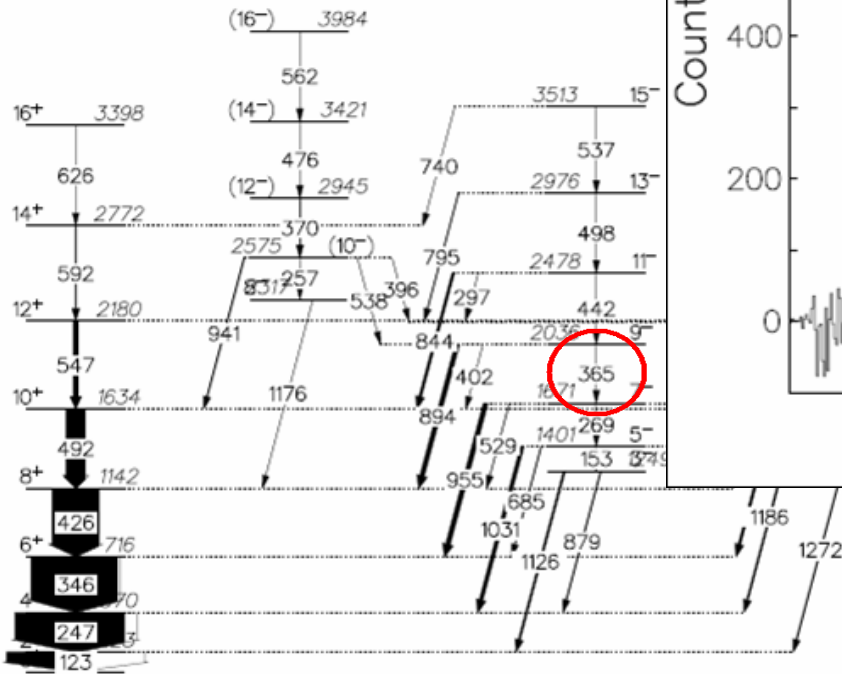
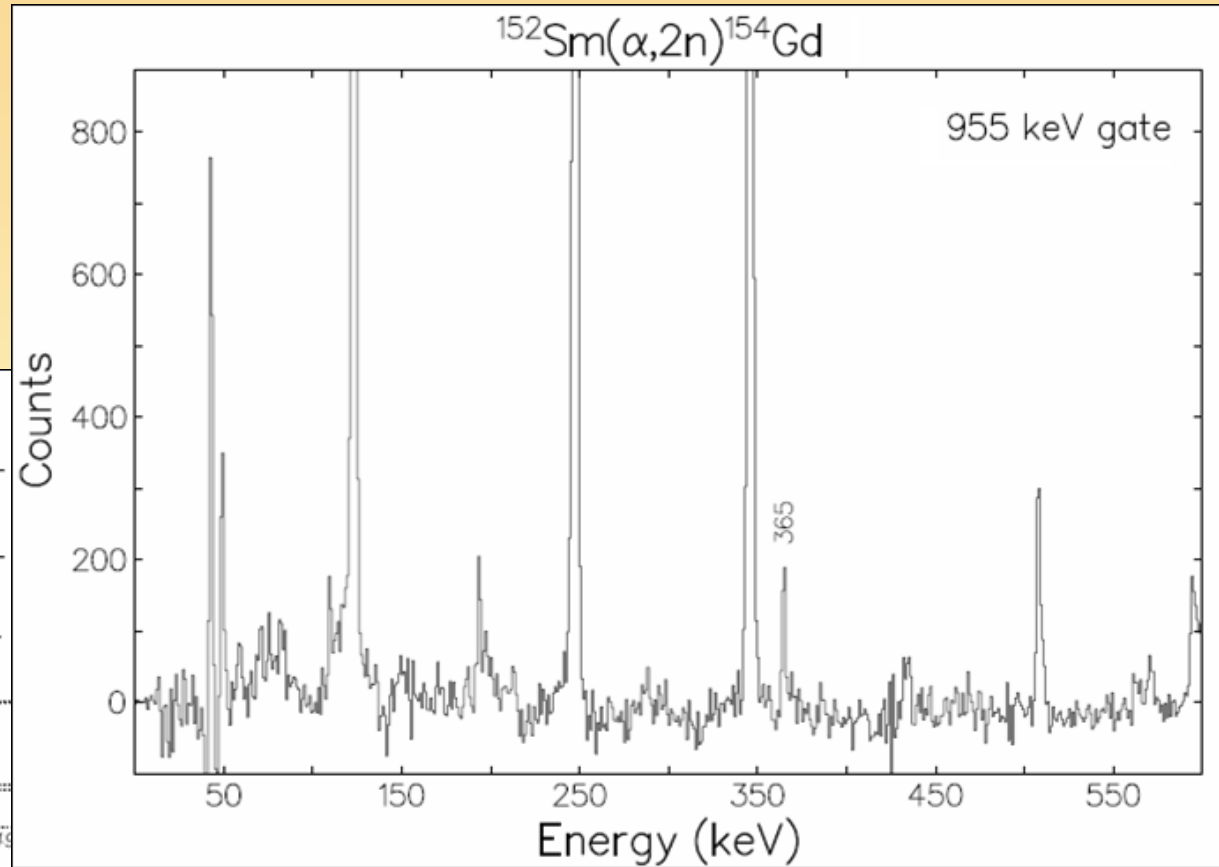
AF

tetra?



# Missing transitions...

■ Yes!



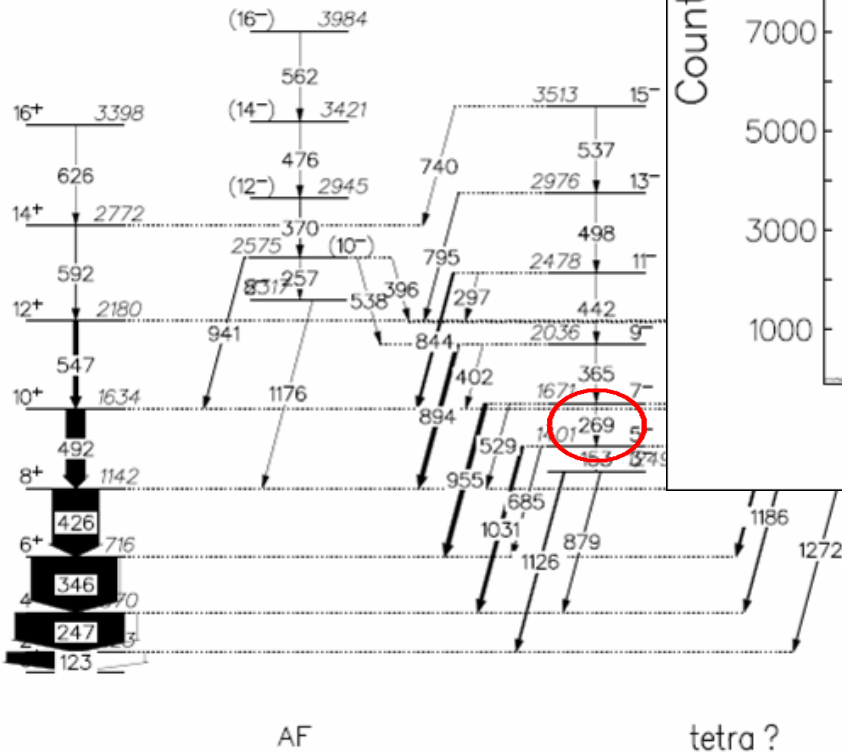
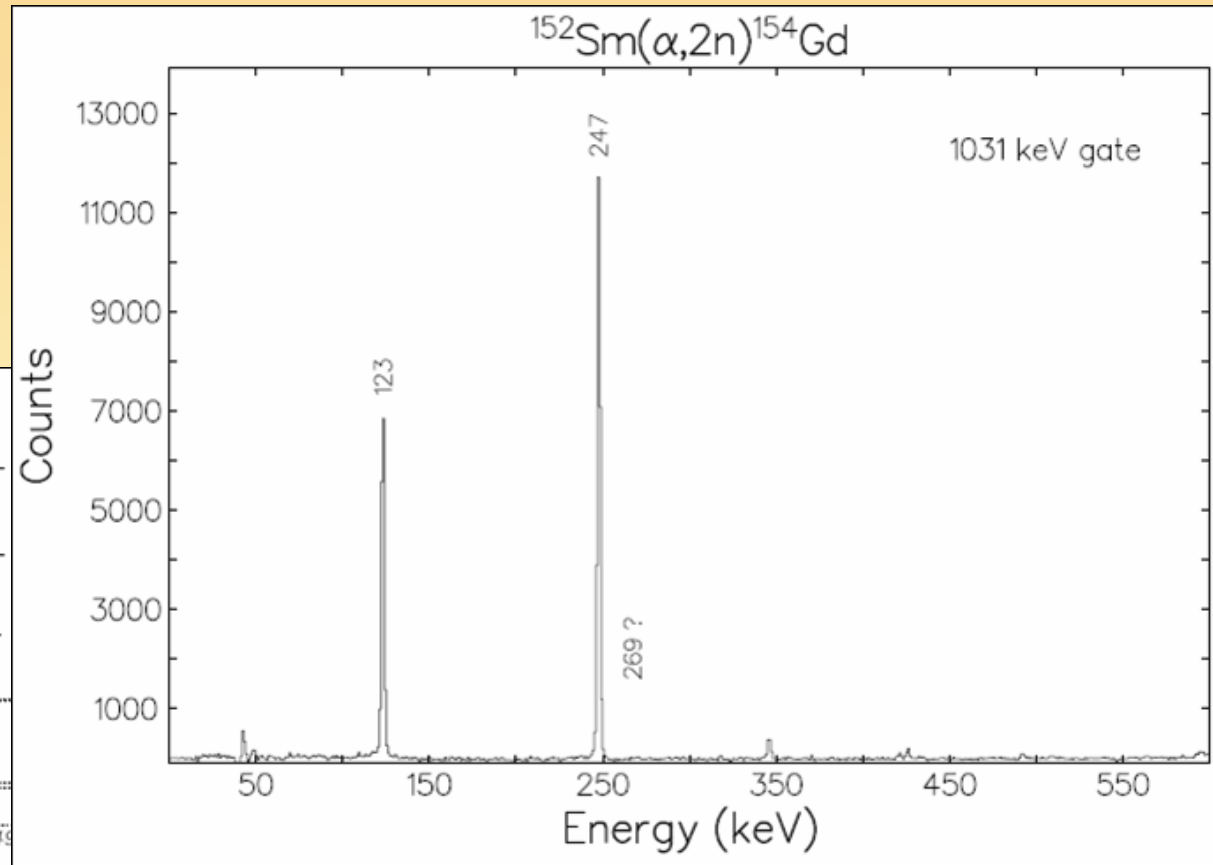
AF

tetra ?



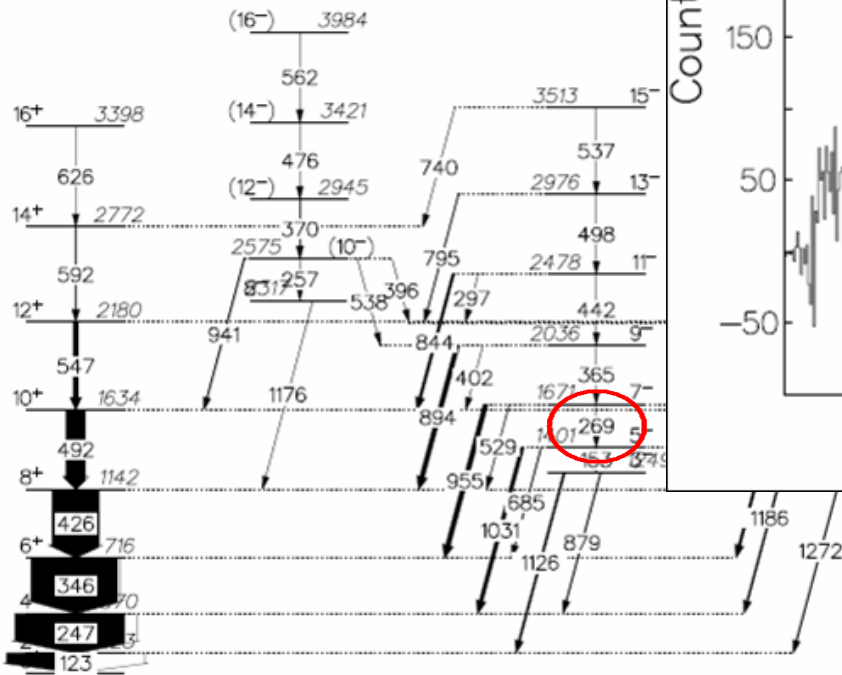
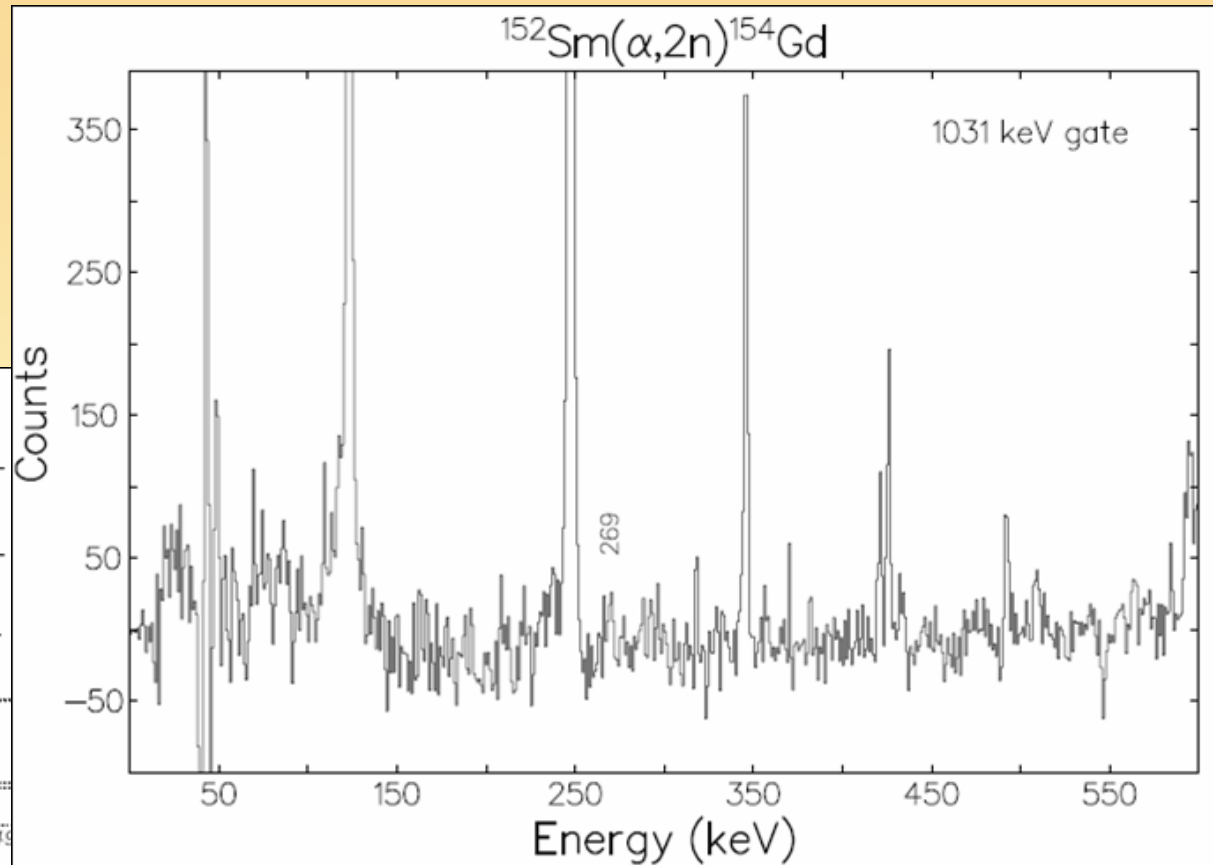
# Let's try again:

- How about  $7 \rightarrow 5$ ?



# And it seems we have it:

- Well, sort of  
Much fainter



AF

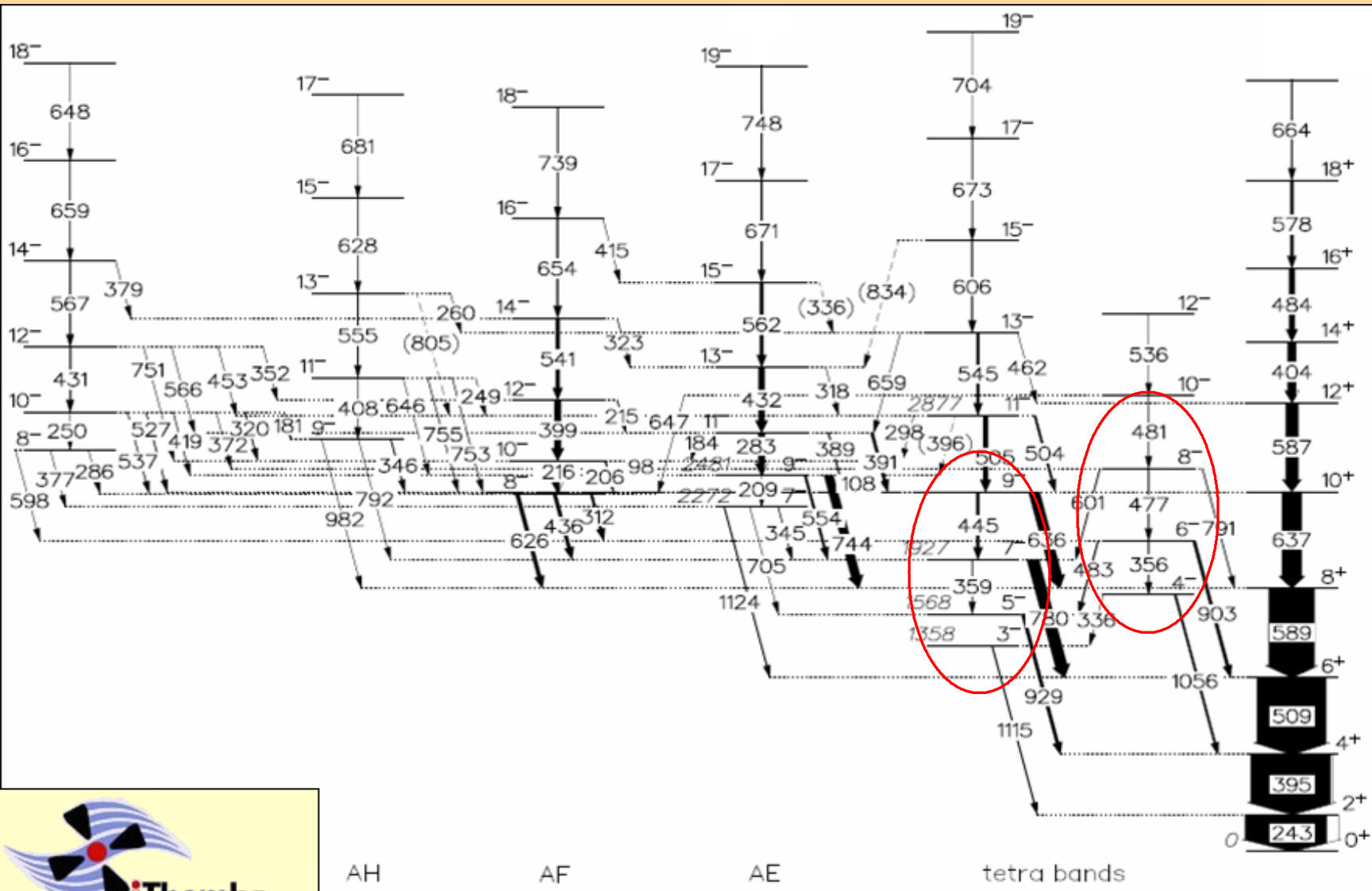
tetra ?



# $^{154}\text{Gd}$ update

- There are in-band E2 transitions
- The  $9 \rightarrow 7$  and  $7 \rightarrow 5$  transitions found, but getting very weak.
- $5 \rightarrow 3$  and  $3 \rightarrow 1$  unobserved
- Unlikely to be tetrahedral

# Next: $^{160}\text{Yb}$





# $^{160}\text{Yb}$ , continued

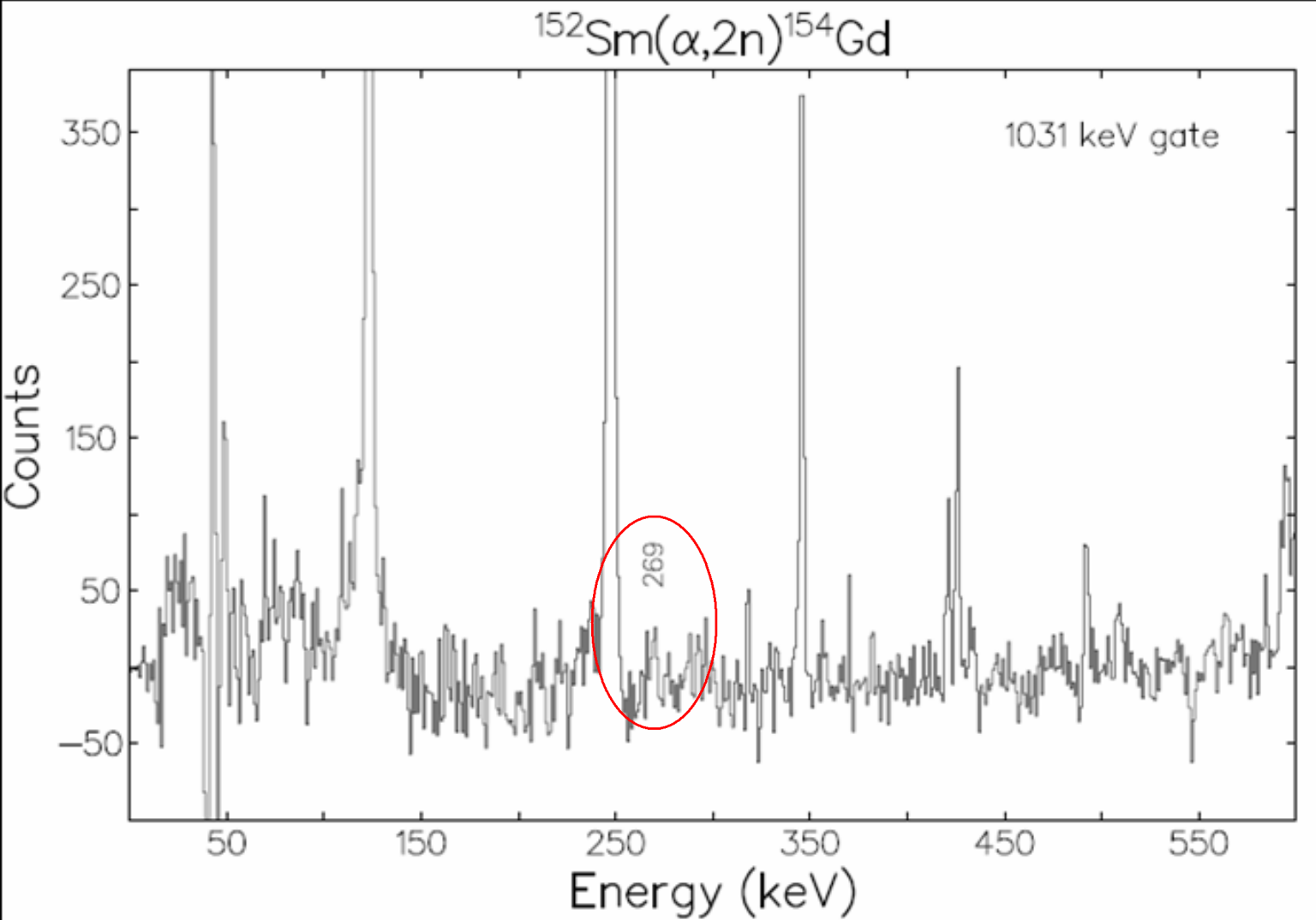
- Evidence of the in-band E2 transitions
- Again, have transitions down to  $5^-$  (and  $4^-$ ), but transitions very weak.
- Why?

# Branching ratios

- Choice in staying in-band or going to yrast
- Observed branching ratio (counts)

$$\lambda = \frac{P_{\gamma}(\text{E2}, I \rightarrow I - 2)}{P_{\gamma}(\text{E1}, I \rightarrow I - 1)} \sim \frac{E_{\gamma}(\text{E2}, I \rightarrow I - 2)^5}{E_{\gamma}(\text{E1}, I \rightarrow I - 1)^3}$$

- Low-energies gammas are suppressed, given preferential other option.



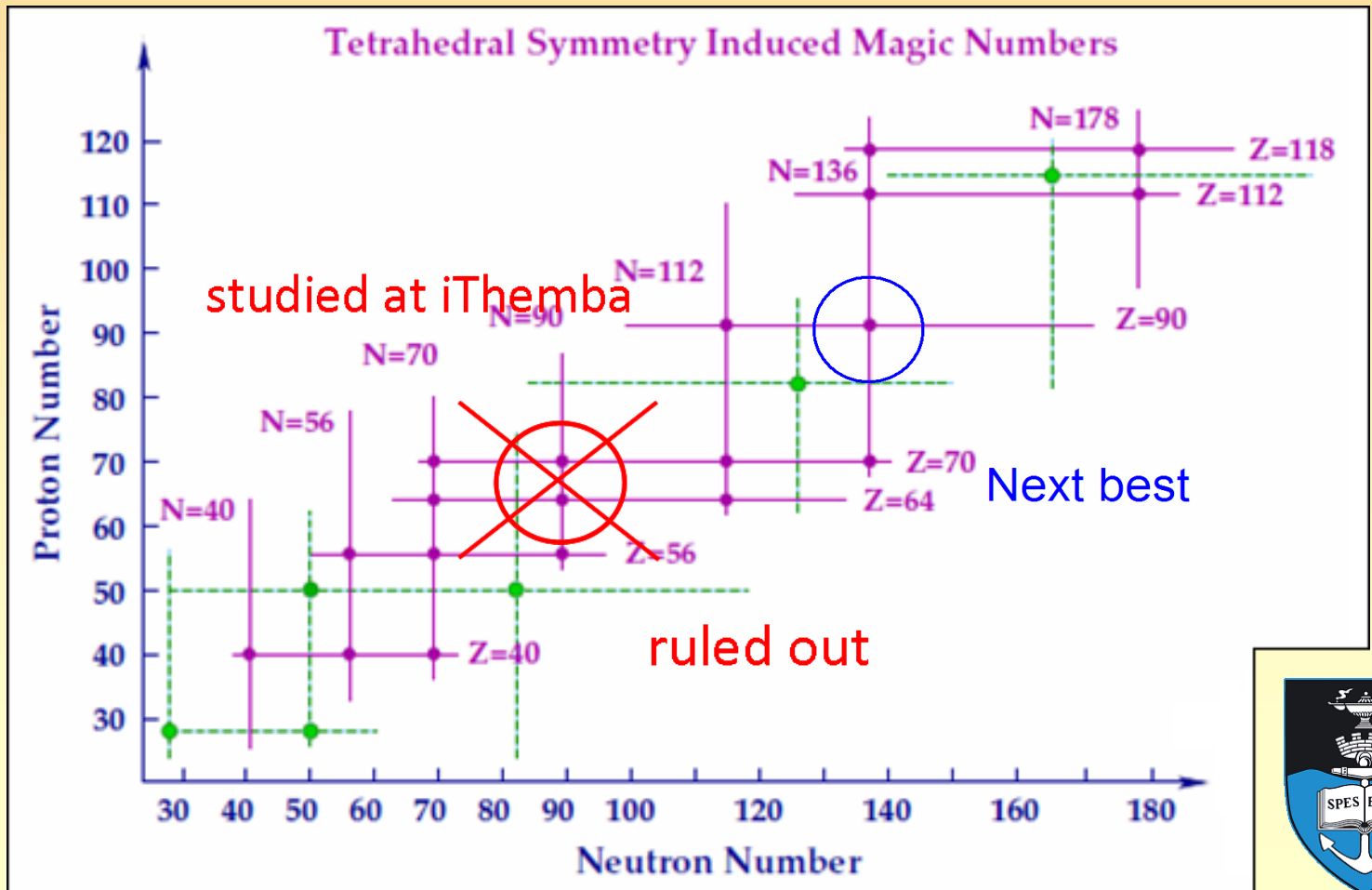
a

~ 0.08

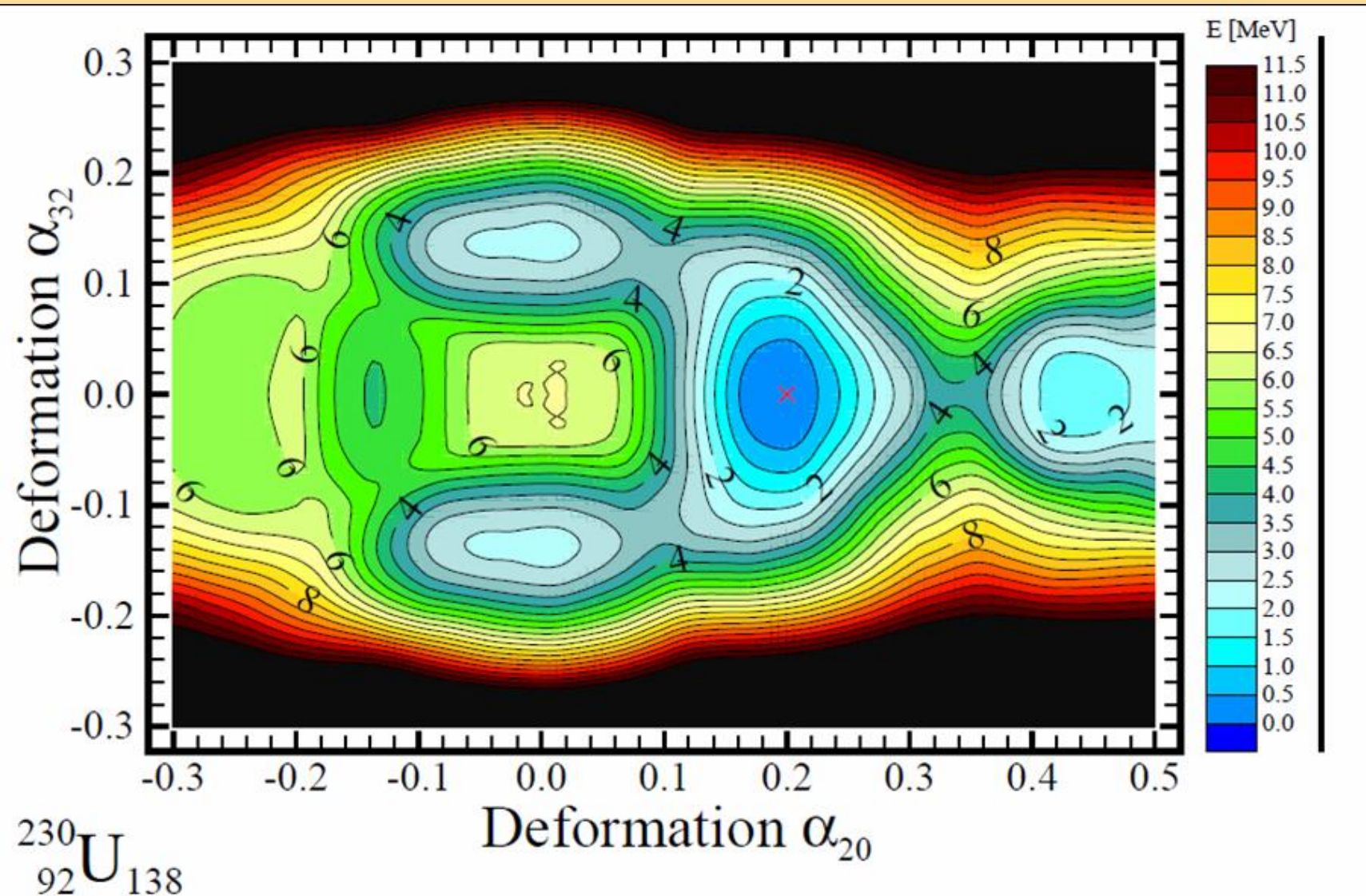
- Do not expect to be able to see it.

# Where to next?

- There are other doubly-magic points:



# Try look at region $Z \sim 90$





# Lack of in-band E2's

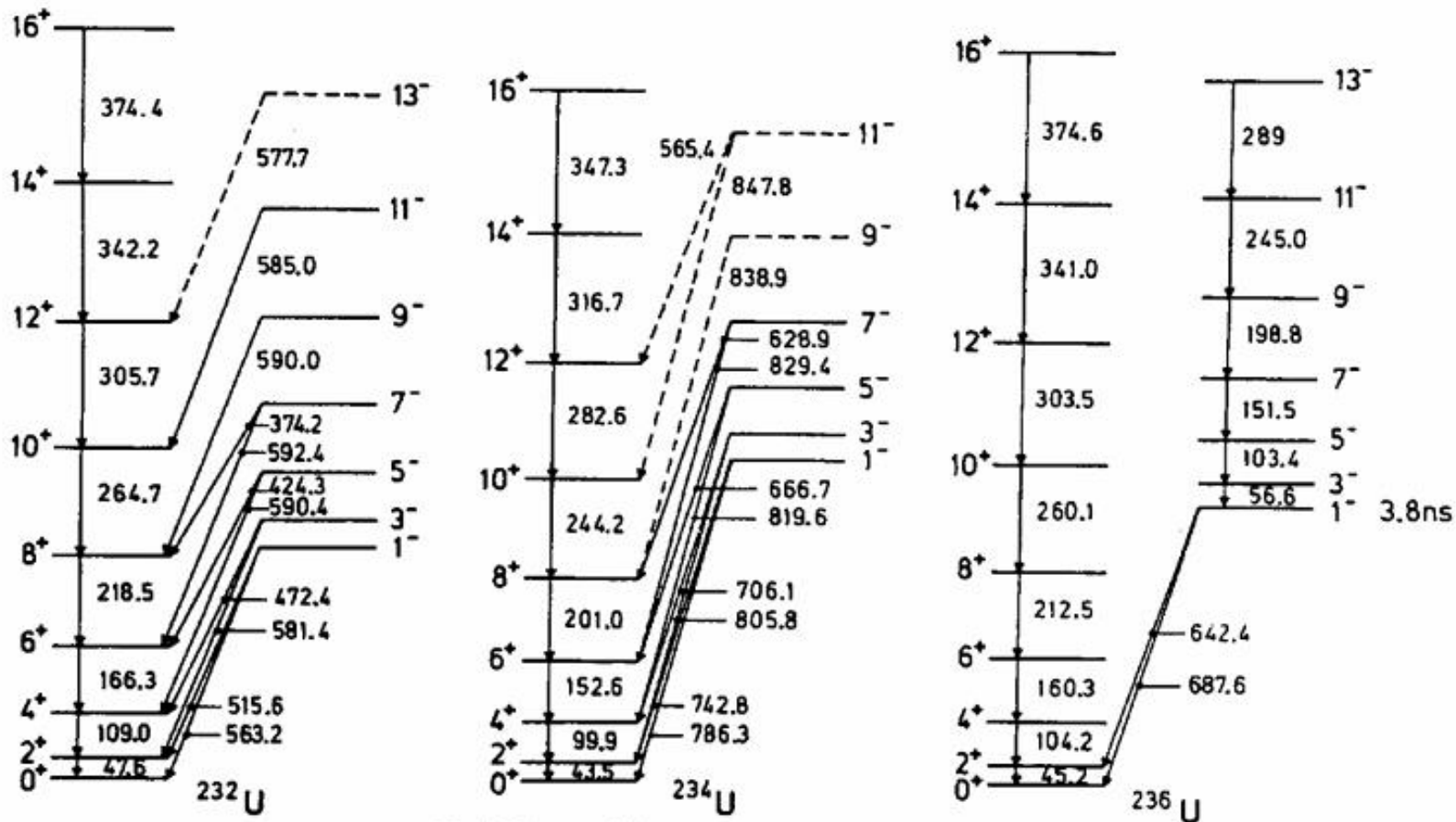


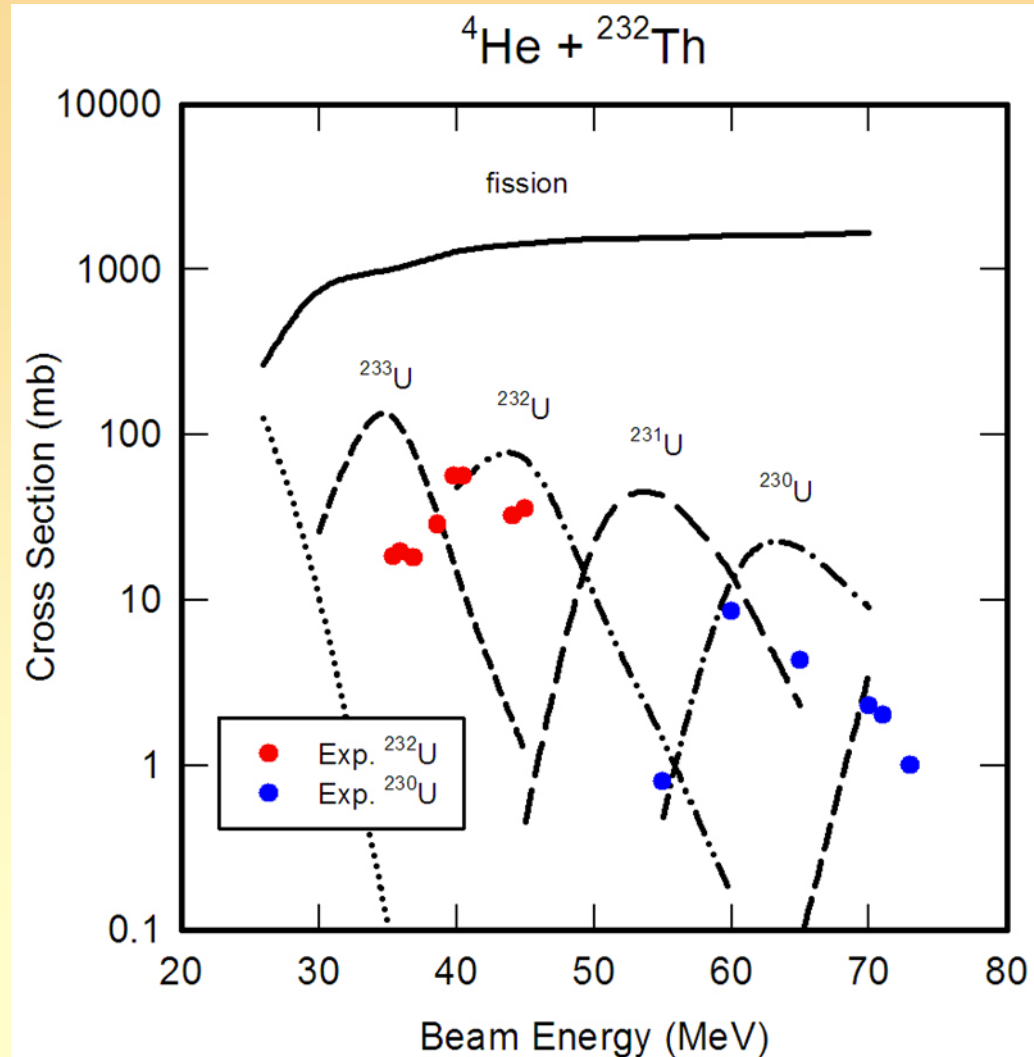
Fig. 9. Level schemes of the isotopes  $^{232}\text{U}$ ,  $^{234}\text{U}$  and  $^{236}\text{U}$



# Making U by fusion

$^{232}\text{Th}(\alpha, xn)$   
reactions

Have very low  
cross-sections



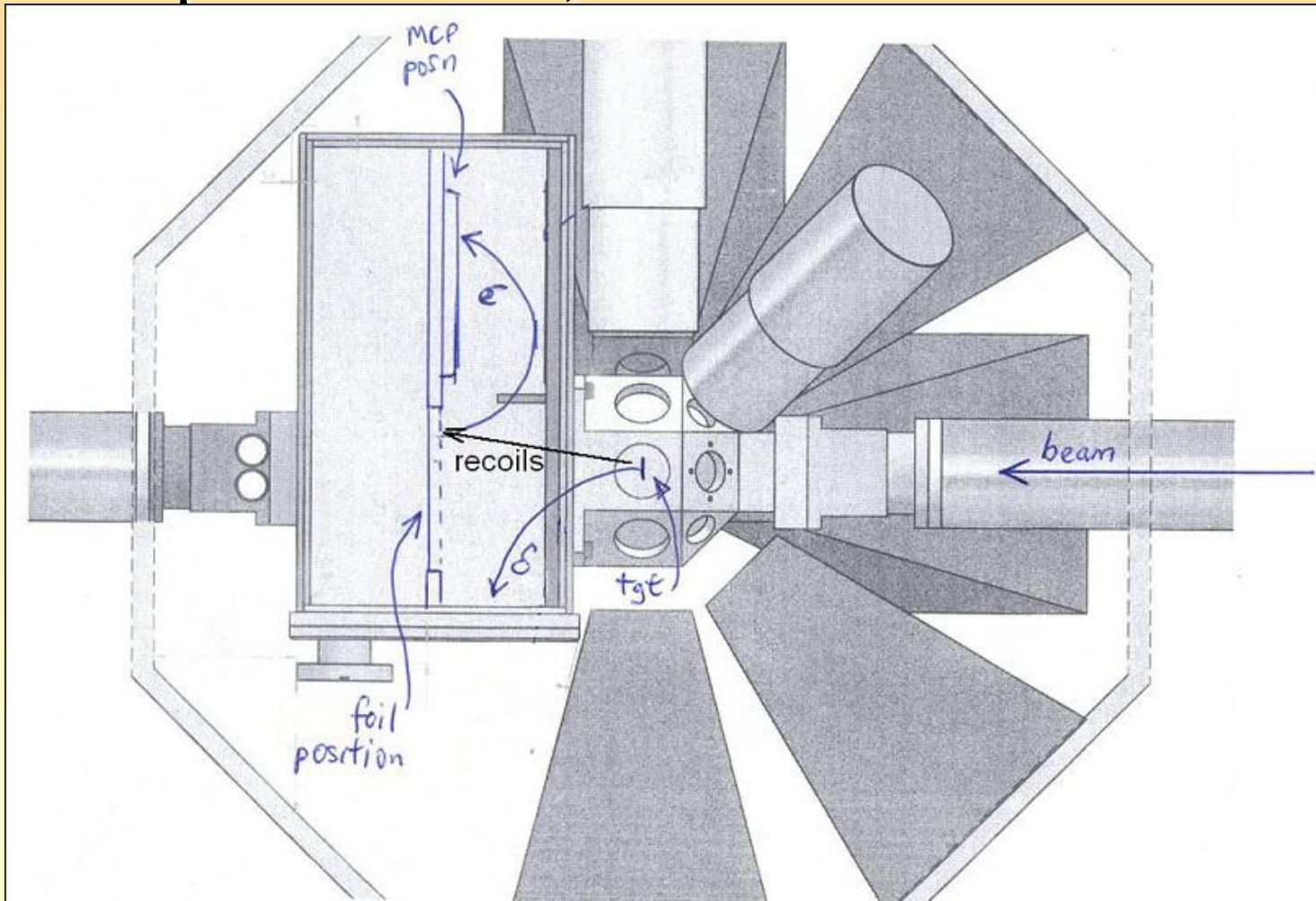


# Recoil detector

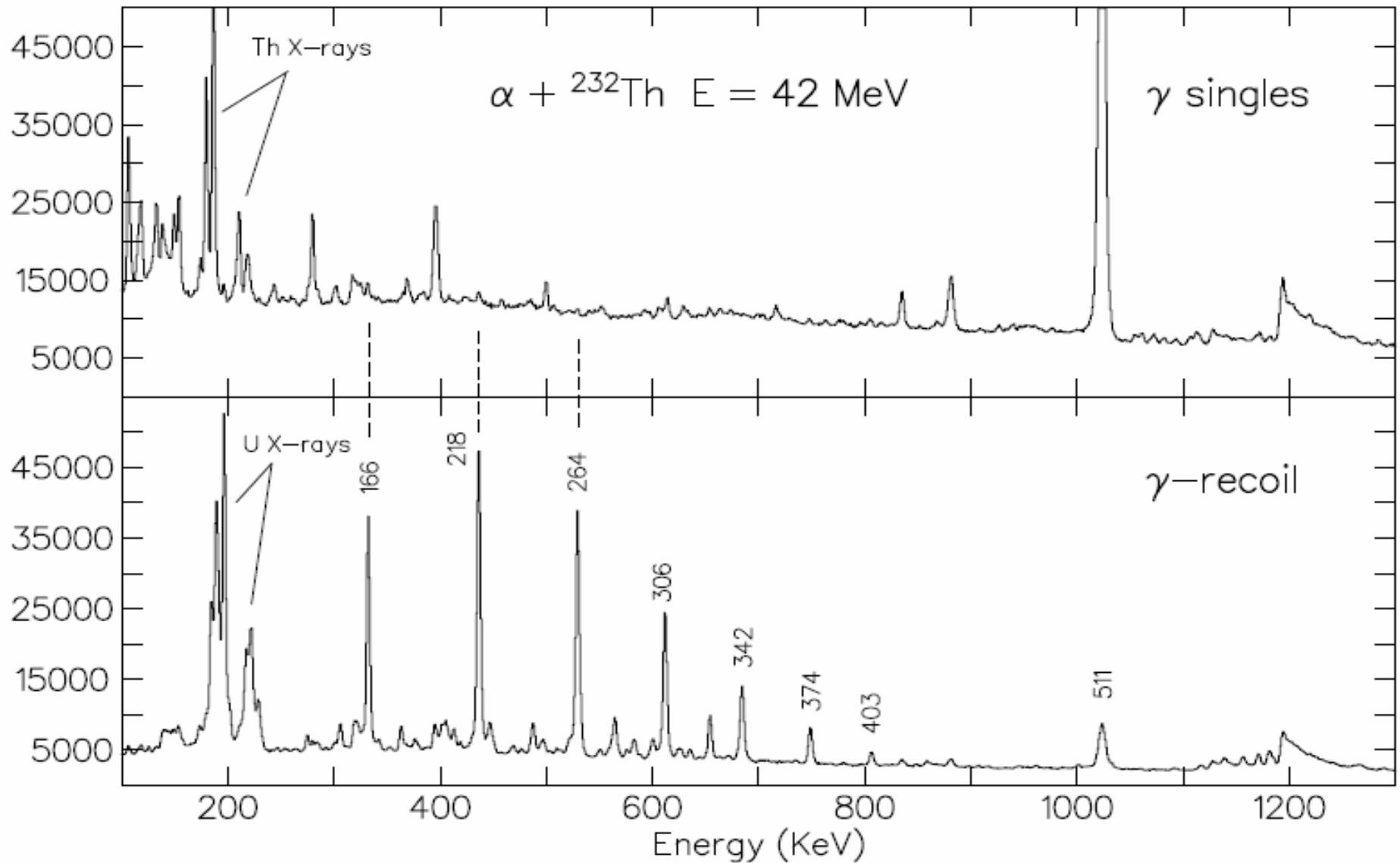
- Work with a pulsed beam, and careful TOF

Beam @  
340 ns

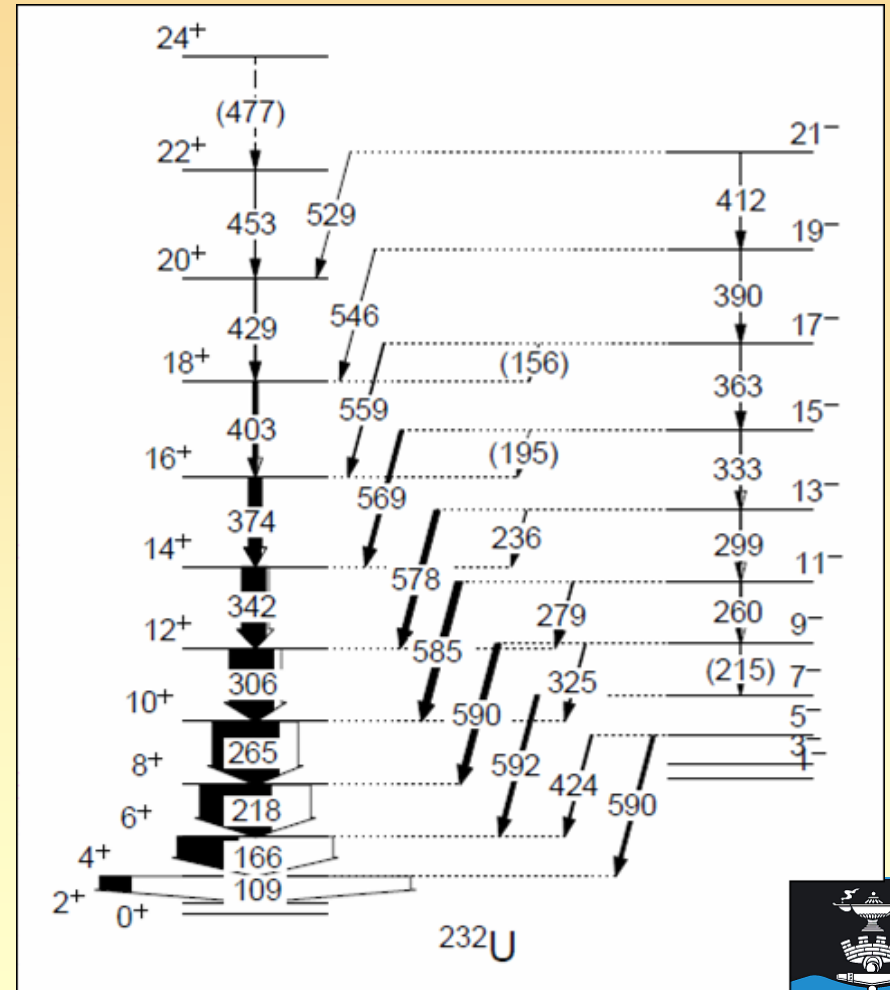
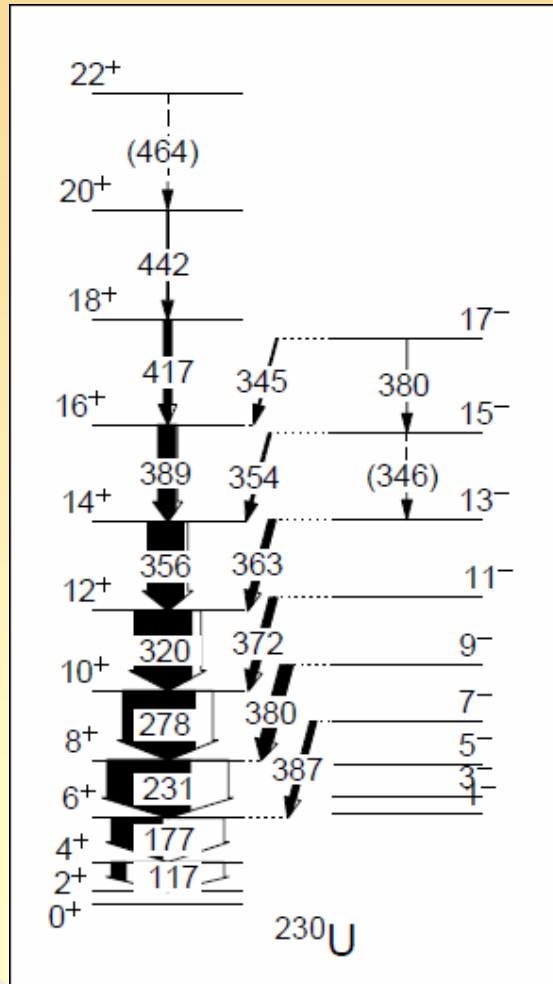
Recoils  
~150 ns



# Recoil gate invaluable



# Study $^{230}\text{U}$ , $^{232}\text{U}$ with AFRODITE

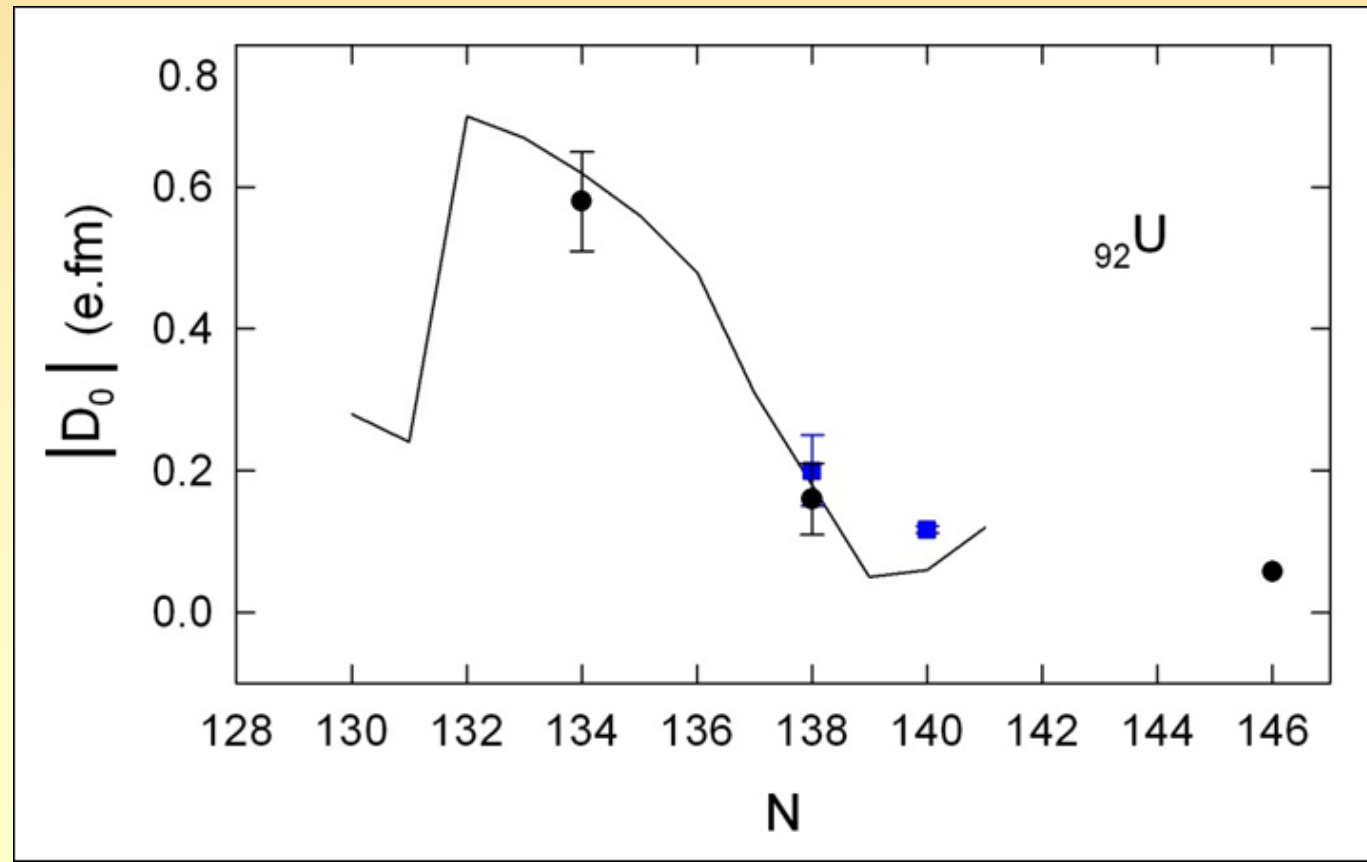


# U octupole bands

- $^{232}\text{U}$  there are known in band transitions
- $^{230}\text{U}$  has only a couple weak transitions

■ Compare to Skyrme mean-field results

Tsvetkov et al.  
(2002)



# Summary

- The octupole bands around  $A \sim 160$  have been studied, but do not support the tetrahedral idea
- The octupole bands in uranium have been studied, a little inconclusive. However, an indirect measurement of the dipole moment fits well with non-tetrahedral models.

# Way forward

- The iThemba LABS have array of tools for observing nuclear reactions
- Positive results for theory are best
- Octupole bands not tetrahedral
  - Still need to be understood
  - What is best way forward?
  - Currently working on RPA



# References

- Dudek et al., Phys. Rev. Lett. 88, 252502 (2002)
- Dudek et al., Phys. Rev. Lett. 97, 072501(2006)
- Schunck et al., Phys. Rev. C69, 061305 (2004)
- Bark et al., Phys. Rev. Lett., 104, 022501 (2010)
- Ntshangase et al., to be published
- Tsvetkov et al., J. Phys. G28, 2187 (2002)
  
- Thanks to Rob Bark for use of his presentations at Nuclear Structure 2009 and 2010.



# The End

(No frogs were harmed in these experiments)

To the best of my knowledge

