

Lecture 2: PENTAQUARKS UPDATE

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Heavy Quark Physics

Dubna, June 6-16, 2005

- Historical note
- Review of the new wave of exotics Θ^+ , Ξ^{--} , Ξ_c^0
- Latest experimental results
 - Trento Workshop February 2005, SPring-8, g10@JLAB
 - APS meeting, April 2005, g11@JLAB
- Theoretical approaches, short look
- Conclusions

References:

F.S. [hep-ph/0504284](#)

HISTORICAL NOTE

Light pentas: since 70' until 1984

Searches in the mass range 1.74 GeV to 2.16 GeV

Parity not important, in fact **negative**

Heavy pentas: Theory 1987 → E791 (Fermilab) 1998 **inconclusive**

Mass range below threshold

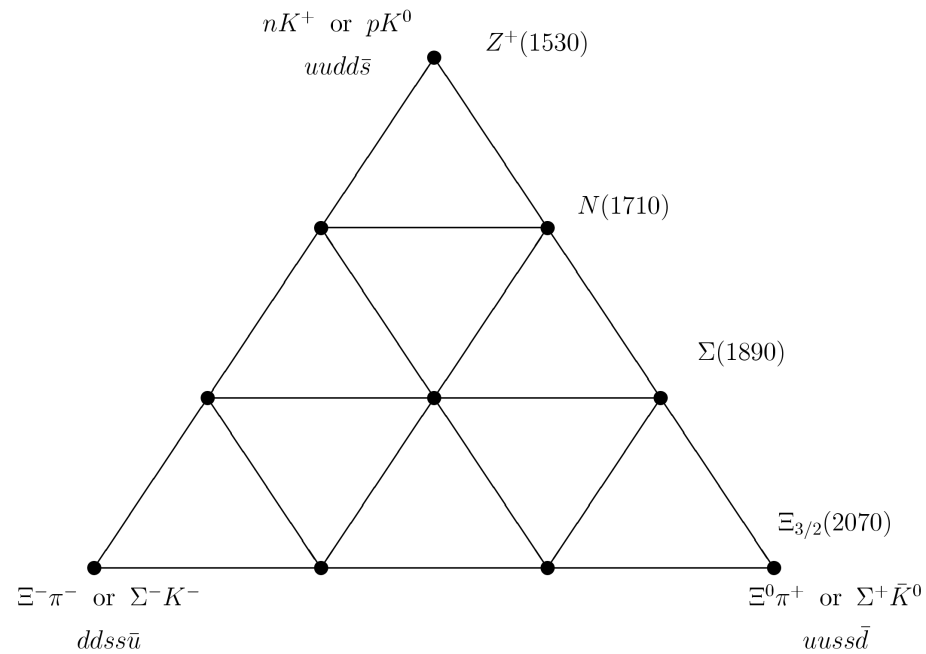
$N + D_s = 2908 \text{ MeV}$ or $\Lambda + D = 2982 \text{ MeV}$

Parity: **negative**

Positive parity heavy pentas $uudd\bar{c}$, F. S. PRD58(1998)

NEW WAVE

D.Diakonov, V.Petrov, M.Polyakov, Z. Phys. A359(1997)305



Chiral soliton model: Θ^+ is a collective excitation of the mean chiral field \rightarrow low mass and narrow width

PRESENT EXPERIMENTAL STATUS: LIGHT PENTAS

Θ^+ $M \simeq 1530 \text{ MeV}$, $\Gamma < 25 \text{ MeV}$, $I = 0$

*10 or more independent measurements report **confirmation**

*nearly as many report **null evidence** (HERA-B, PHENIX, BES)

*Deuterium results from **SPring-8** (background estimate)
(**T. Nakano** → encouraging)

***High statistics experiments** on hydrogen **g11** and deuterium **g10**,
CLAS detector

$\Xi_{3/2}^-$ $M \simeq 1862 \text{ MeV}, \Gamma \simeq 18 \text{ MeV}$

- **observed** and **not seen** at Na49 at CERN
confirmed at Trento 2005
- **not seen** WA89 (Σ^- -nucleus), CDF ($p\bar{p}$), BaBar (e^+e^-)

PRESENT EXPERIMENTAL STATUS: HEAVY PENTAS

Θ_c^0 $M \simeq 3100 \text{ MeV}, \Gamma \simeq 12 \text{ MeV}$

- **observed** by H1 Collaboration (HERA) March 2004
confirmed at Trento 2005
- **null evidence** from ZEUS ($e - p$ collisions), CDF ($p\bar{p}$) collisions,
Belle ($B - meson$ decay)

LEPS results presented by K. Hicks, Trento, February 2005

LEPS New LD2 and LH2 runs

- Data taken from Oct. 2002 to Jun. 2003.
- $\sim 2 \cdot 10^{12}$ photons on a 15cm-long LD2 target.
- LH2 data were taken in the same period with $\sim 1.4 \cdot 10^{12}$ photons on the target.

of photons: LH2:LD2 \approx 2:3

of events from a proton: LH2:LD2 \approx 2:3
(e.g. KKp from ϕ production)

of events from a nucleon: LH2:LD2 \approx 1:3

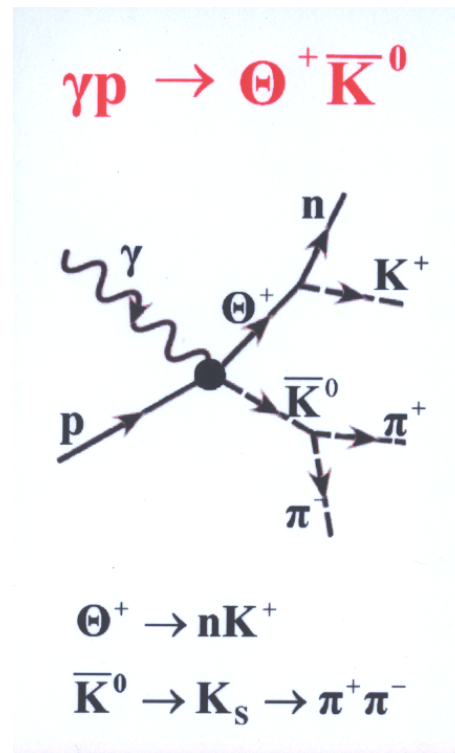
Search for Pentaquarks at CLAS

- **g10**
deuteron, $E_\gamma \sim 1.0 - 3.5$ GeV , completed 2004
- **g11**
proton, $E_\gamma \sim 1.6 - 3.8$ GeV , completed 2004, see APS05
- **eg3**
deuteron, $E_\gamma \sim 4.0 - 5.4$ GeV , data taking completed 2005
- **Super-g**
proton, $E_\gamma \sim 3.8 - 5.7$ GeV , planned 2006

g11@JLAB

Collect more than 10 times the statistics of previous measurements

Run in May - July 2004, preliminary at APS meeting, April 2005



Comparison with SAPHIR results

Observed Yields

SAPHIR

$$N(\Theta^+)/N(\Lambda^*) \sim 9\%$$

CLAS

$$N(\Theta^+)/N(\Lambda^*) < 0.5\% \text{ (95\%CL)}$$

Cross Sections

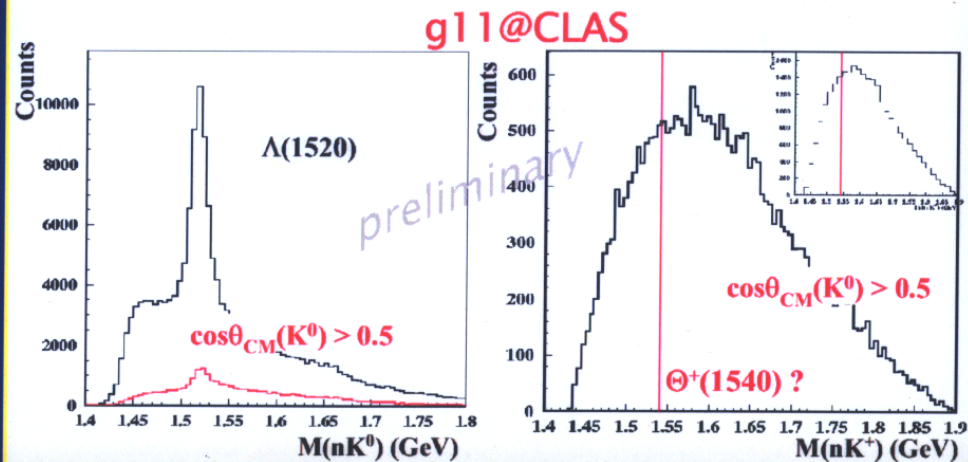
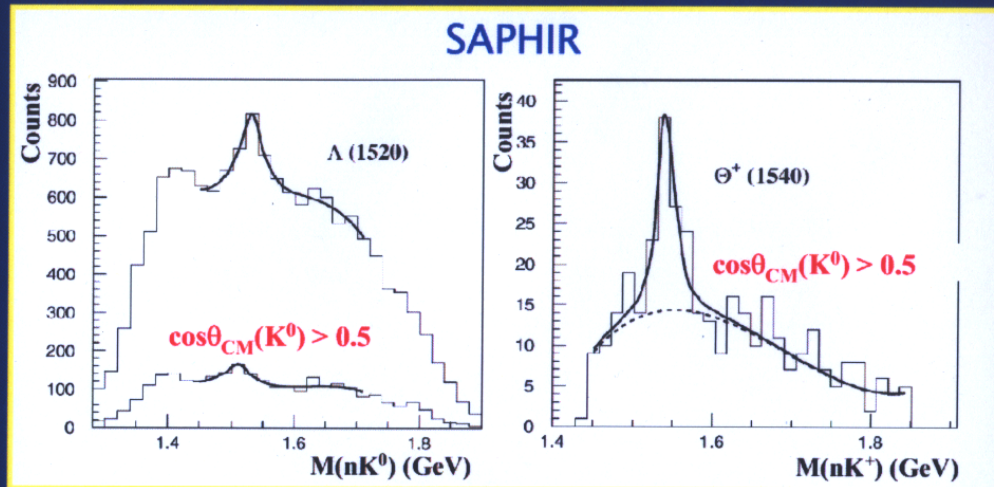
SAPHIR

$$\sigma_{\gamma p \rightarrow \Theta^+ K^0} \sim 300 \text{ nb}$$

reanalysis 50 nb

CLAS

$$\sigma_{\gamma p \rightarrow \Theta^+ K^0} < 1\text{-}4 \text{ nb}$$



PRESENT APPROACHES to the ANTIDECUPLER

- Spin and parity of Θ^+ \rightarrow polarization experiments
- Consistency with partial wave analysis
- Photoproduction cross sections on proton, neutron
- Chiral soliton model revisited, masses & widths
- Constituent quark models, masses & widths
- Octet-antidecuplet or higher representation mixing
- Group theoretical classification of $q \times q \times q \times q \times \bar{q}$ states \rightarrow mass formulae
- Heptaquarks or $K\pi N$ molecular picture
- Skyrme model (bound state or rigid rotator)
- Description of pentaquarks in the instanton model
- QCD sum rules
- Lattice calculations
- Magnetic moments of pentaquarks
- Θ^+ in relativistic heavy ion collisions

MAIN ISSUES

- The mass of Θ^+
- The strong decay width
- Spin and Parity
- Splitting between isomultiplets
- SU(3)- flavour representation mixing
- Production mechanism

Lattice QCD results

- Quenched approximation → dynamical effects are omitted, but correct picture for narrow states
- Action chirally symmetric at vanishing quark mass
→ one can reach light quark masses
- Choice of operators is crucial to have the best overlap with Θ^+
→ Kaon-Nucleon type or diquark-diquark-antiquark structure
- Difficult to distinguish the resonance from the continuum
→ controversy about the existence of a resonant state
- Presently - consensus ? - lowest state has negative parity

QCD sum rules

Lowest state has negative parity, $M \sim 1.5 \text{ GeV}$

S. L. Zhu, PRL 91 (2003) [hep-ph/0307345]

Sugyama, Doi, Oka

Kwon, Hosaka, S. H. Lee, hep-ph/0505040

Wang, Yang, Wan, hep-ph/0501015

CONSTITUENT QUARK MODELS

TWO STANDARD MODELS

Colour-Spin (CS)

$$V_{CS} = - \sum_{i < j}^5 C_{ij}^{CS} \lambda_i^c \cdot \lambda_j^c \vec{\sigma}_i \cdot \vec{\sigma}_j$$

Lowest resonant state has $J^P = 3/2^-$

Flavour-Spin (FS)

$$V_{FS} = - \sum_{i < j}^4 C_{ij}^{FS} \lambda_i^F \cdot \lambda_j^F \vec{\sigma}_i \cdot \vec{\sigma}_j$$

Lowest resonant state has $J^P = 1/2^+$

How important is spontaneous breaking of chiral symmetry ?

PENTAQUARK SPECTRUM in the FS MODEL

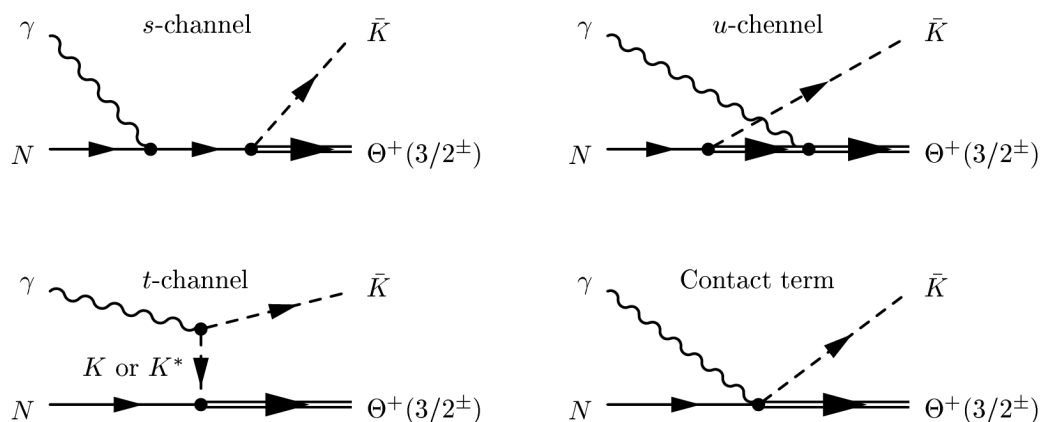
nearly ideal mixing

F. S. PLB595,269(2004);erratum PLBB598,295(2004).

	Σ_5 _____ 2046	Ξ^{--} _____ 2070
Ξ^{--} _____ 1962	Ξ^{--} _____ 1962	
		Σ _____ 1890
$\Sigma_{\overline{10}}$ _____ 1829	N_5 _____ 1801	
		N _____ 1710
$N_{\overline{10}}$ _____ 1684		
Θ^+ _____ 1540	Θ^+ _____ 1540	Θ^+ _____ 1530
a) pure antidecuplet	b) mixed with the octet	c) DPP 1997

Production mechanism on nucleon, $J^P = 1/2^+, 3/2^\pm$

Nam, Hosaka, Kim, hep-ph/0505134



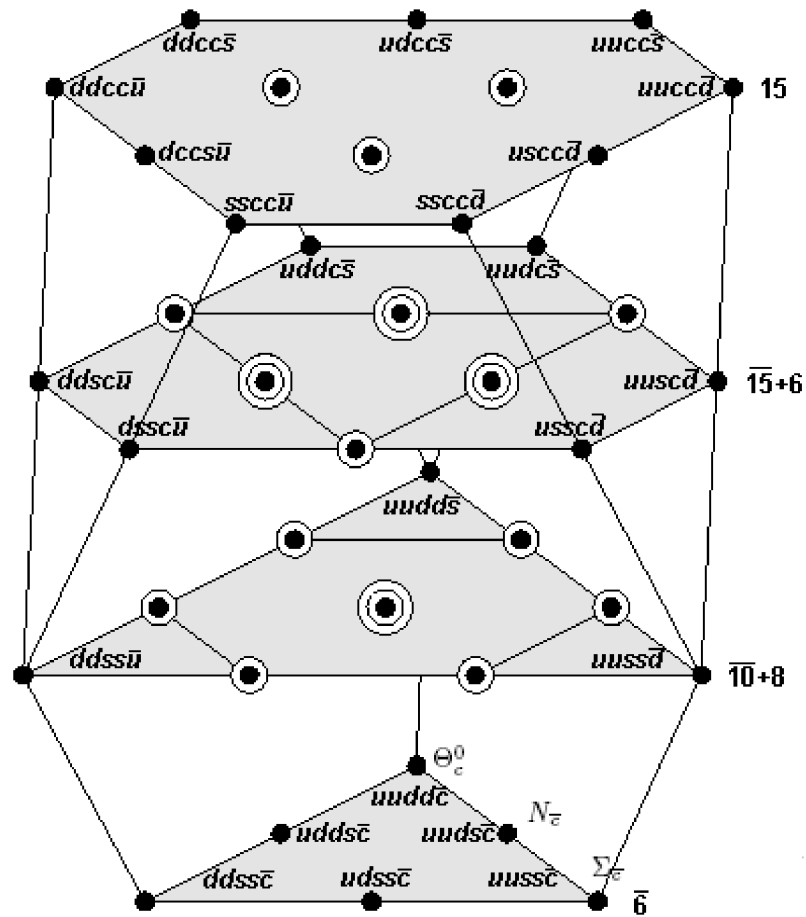
State dependent result

$$J^P = 1/2^+ \quad \sigma \sim 1 \text{ nb for } n \text{ and } p$$

$$J^P = 3/2^- \quad \text{Proton } \sigma \sim 4 \text{ nb, Neutron } \sigma \sim 200 \text{ nb}$$

CHARMED PENTAQUARKS in the $\bar{6}_0$ -plet of SU(4)

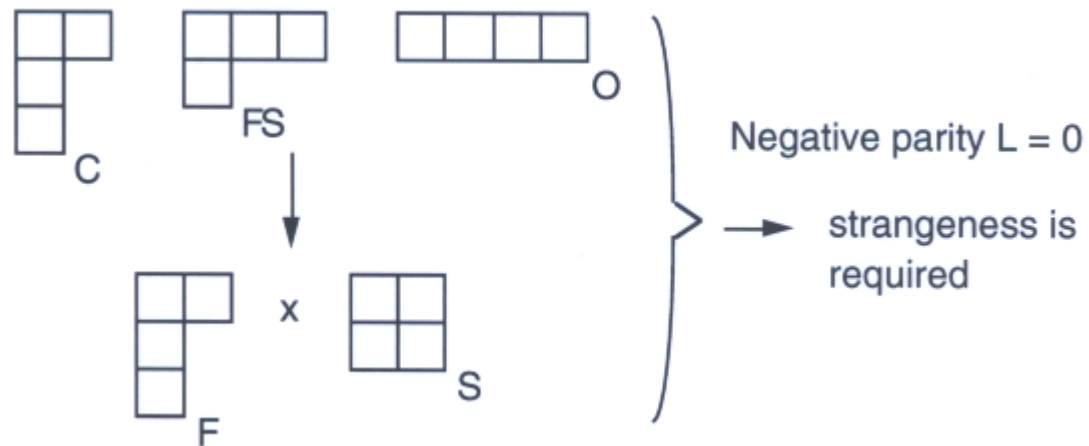
Bin Wu & Bo-Qiang Ma, hep-ph/0402244



Negative parity pentaquarks

C. Gignoux et al., PLB193(1987)323

H. J. Lipkin, PLB195(1987)484

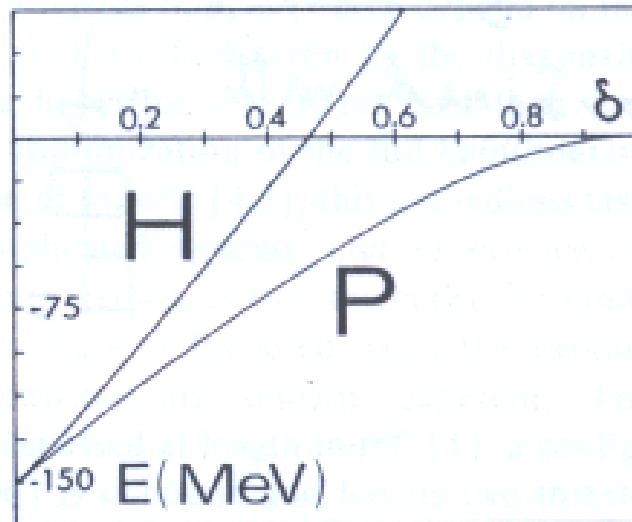


Negative parity pentaquarks

C. Gignoux et al., PLB193(1987)323

$$V_{CS} = -C_{CS} \sum_{i < j}^5 \lambda_i^c \cdot \lambda_j^c \vec{\sigma}_i \cdot \vec{\sigma}_j$$

$$\Delta E = E(q^4 \bar{Q}) - E(q^3) - E(q \bar{Q})$$



$$\langle V_{CS}/C_{CS} \rangle = -16; \quad \delta = 1 - m_u/m_s$$

Skyrme model (Callan-Klebanov version)
Riska & Scoccola, PLB299,338(1993)

1. strangeness is not required
2. the lowest states have positive parity ($\ell = 1$)

———— ($\ell = 2$)

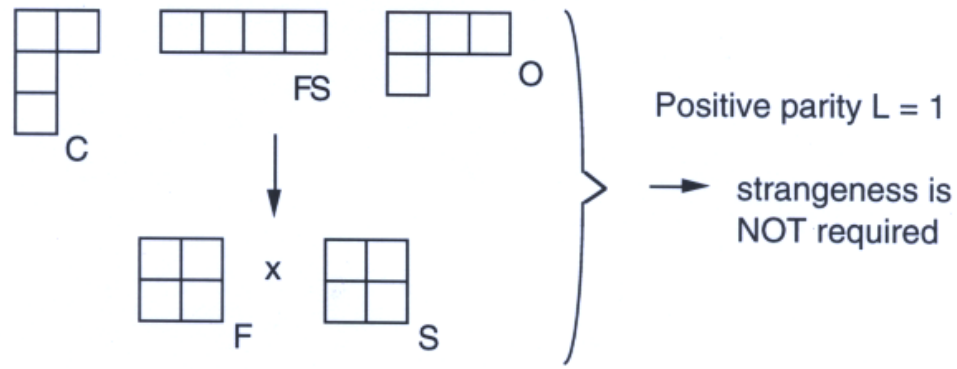
———— ($\ell = 0$)

———— ($\ell = 1$)

$$M(q^4\bar{c}) \simeq 2.6 - 2.7 \text{ GeV}$$

Flavour-spin model

F. S. PRD58,111501(1998)



$$V_{FS} = -C_{FS} \sum_{i < j}^4 \lambda_i^F \cdot \lambda_j^F \vec{\sigma}_i \cdot \vec{\sigma}_j$$

$P = +1$	V_{FS}/C_{FS}	$P = -1$	V_{FS}/C_{FS}
$[22]_F [22]_S [4]_{FS}$	- 28	$[211]_F [22]_S [31]_{FS}$	- 16
$[31]_F [31]_S [4]_{FS}$	- 64/3	$[211]_F [31]_S [31]_{FS}$	- 40/3

MASSES (MeV) of the antisextet charmed pentaquarks $P = +1$

Penta	I	Content	FS model FS 1998	D – D – \bar{c} JW 2003	CS model KM2004
Θ_c^0	0	u u d d \bar{c}	2902	2710	2835 ± 30
N_c^0	1/2	u u d s \bar{c}	3161		
Ξ_c^0	1	u u s s \bar{c}	3403		

Predictions

FS 1988: F.S. PRD58(1998)111501

JW 2003: Jaffe & Wilczek PRL 91 (2003) 232003

Postdictions. K. Maltman, PLB604 (2004) 175

NB. $N + D = 2808 \text{ MeV}$

CONCLUSIONS

- **g11 results do not exclude the existence of pentaquarks. There are about 10 positive exp.**
- **Need of a deeper understanding of the production mechanism of Θ^+ and high statistics/resolution exp.**
- **New pentaquark meeting at JLAB autumn, 2005**

WHY THE FS MODEL ?

- **Good** description of baryon spectra,
- **Previous experience** in heavy pentaquarks,
F. S. PRD58(1998)111501
- Symmetry consistent with the **large N_c limit** of QCD
→ naturally small width for Θ^+
(Jenkins & Manohar, hep-ph/0402024)
N. B. The irreducible representations are referred to as Skyrme representations
- Support from **lattice calculations**,
F. Lee, PENTAQUARK04, SPring-8

STABLE $uudd\bar{s}$

F. S. & D. O. Riska, PLB575,242(2003)

1) qq pairs, schematic **Flavour-Spin** interaction

Glozman & Riska, PR268(1996)263

$$V_{\chi} = - C_{\chi} \sum_{i < j}^4 \lambda_i^F \cdot \lambda_j^F \tilde{\sigma}_i \cdot \tilde{\sigma}_j$$

$$C_{\chi} \sim 30 \text{ MeV} \quad (\Delta - N \text{ splitting})$$

enough if the antiquark is heavy

2) $q\bar{s}$ pairs, schematic η -meson exchange

Pion decay $D_s^* \rightarrow D_s \pi^0$ requires $\pi^0 - \eta$ mixing
 $\rightarrow \eta$ meson couples to s or \bar{s} (Laehde and Riska, '02)

$$V_\eta = V_0 \sum_i^4 \tilde{\sigma}_i \cdot \tilde{\sigma}_j$$

$V_0 = 2C_\chi$ lowers the binding energy by 350 MeV

Conclusion: $V_\chi + V_\eta$ makes $uudd\bar{s}$ $J^P=1/2^+$, $I=0$, $S=+1$ stable

REALISTIC FLAVOUR-SPIN HAMILTONIAN

Graz parametrization, Glozman, Papp & Plessas, PLB '96

$$H = \sum_i m_i + \sum_i \frac{\vec{p}_i^2}{2m_i} - \frac{\vec{P}^2}{2M} + \sum_{i<j} V_{conf}(r_{ij}) + \sum_{i<j} V_\chi(r_{ij})$$

$$V_{conf}(r_{ij}) = -\frac{3}{8} \lambda_i^c \cdot \lambda_j^c C r_{ij}$$

$$V_\chi(r_{ij}) = \left\{ \sum_{F=1}^3 V_\pi(r_{ij}) \lambda_i^F \lambda_j^F + \sum_{F=4}^7 V_K(r_{ij}) \lambda_i^F \lambda_j^F + V_\eta(r_{ij}) \lambda_i^8 \lambda_j^8 + V_{\eta'}(r_{ij}) \lambda_i^0 \lambda_j^0 \right\} \vec{\sigma}_i \cdot \vec{\sigma}_j$$

N. B. Parameters (m_i , meson masses, etc) fitted to baryon spectra
→ good level order

Internal Jacobi coordinates

$$\begin{aligned}\vec{x} &= \vec{r}_1 - \vec{r}_2, \\ \vec{y} &= (\vec{r}_1 + \vec{r}_2 - 2\vec{r}_3)/\sqrt{3} \\ \vec{z} &= (\vec{r}_1 + \vec{r}_2 + \vec{r}_3 - 3\vec{r}_4)/\sqrt{6}, \\ \vec{t} &= (\vec{r}_1 + \vec{r}_2 + \vec{r}_3 + \vec{r}_4 - 4\vec{r}_5)/\sqrt{10}\end{aligned}$$

Basis states of **POSITIVE** parity:

assume s^3p content for $[31]_O$

$$\psi_1 = \begin{array}{|c|c|c|} \hline 1 & 2 & 3 \\ \hline 4 & & \\ \hline \end{array} = \langle \vec{x} | 000 \rangle \langle \vec{y} | 000 \rangle \langle \vec{z} | 010 \rangle$$

$$\psi_2 = \begin{array}{|c|c|c|} \hline 1 & 2 & 4 \\ \hline 3 & & \\ \hline \end{array} = \langle \vec{x} | 000 \rangle \langle \vec{y} | 010 \rangle \langle \vec{z} | 000 \rangle$$

$$\psi_3 = \begin{array}{|c|c|c|} \hline 1 & 3 & 4 \\ \hline 2 & & \\ \hline \end{array} = \langle \vec{x} | 010 \rangle \langle \vec{y} | 000 \rangle \langle \vec{z} | 000 \rangle$$

to be multiplied by $\langle \vec{t} | 000 \rangle$

Gaussian Ansatz

$$\psi_1^5 = \psi_0 z Y_{10}(\hat{z})$$

$$\psi_2^5 = \psi_0 y Y_{10}(\hat{y})$$

$$\psi_3^5 = \psi_0 x Y_{10}(\hat{x})$$

$$\psi_0 = \left[\frac{1}{48\pi^5 \alpha \beta^3} \right]^{1/2} \exp \left[-\frac{1}{4\alpha^2} (x^2 + y^2 + z^2) - \frac{1}{4\beta^2} t^2 \right]$$

Variational parameters α , β

Expectation values (MeV) and total energy

$$E = \sum_{n=1}^5 m_i + \langle T \rangle + \langle V_c \rangle + \langle V_\chi \rangle$$

$q^4\bar{q}$	$\sum_{n=1}^5 m_i$	$\langle T \rangle$	$\langle V_c \rangle$	$\langle V_\chi \rangle$	E	M	$\alpha(\text{fm})$	$\beta(\text{fm})$
uudd \bar{d}	1700	1864	442	-2044	1962	1452	0.42	0.92
uudd\bar{s}	1800	1848	461	-2059	2050	1540	0.42	1.01
uuds \bar{d}	1800	1535	461	-1563	2233	1732	0.45	0.92
uuds \bar{s}	1900	1634	440	-1663	2310	1800	0.44	0.87
ddss\bar{u}	1900	1418	464	-1310	2472	1962	0.46	0.92
uuss \bar{s}	2000	1410	452	-1310	2552	2042	0.46	0.87

The antidecuplet members with $Y = 1$ and $Y = 0$

$$M(N_{\overline{10}}) = \frac{1}{3}M(uudd\bar{d}) + \frac{2}{3}M(uuds\bar{s}),$$
$$M(\Sigma_{\overline{10}}) = \frac{2}{3}M(uuds\bar{d}) + \frac{1}{3}M(uuss\bar{s})$$

The octet members with $Y = 1$ and $Y = 0$

$$M(N_8) = \frac{2}{3}M(uudd\bar{d}) + \frac{1}{3}M(uuds\bar{s}) = 1568 \text{ MeV},$$
$$M(\Sigma_8) = \frac{1}{3}M(uuds\bar{d}) + \frac{2}{3}M(uuss\bar{s}) = 1936 \text{ MeV}.$$

THE ANTIDECUPLET MASS SPECTRUM (MeV) $P = +1$

Penta	Y, I, I ₃	Present results	Carlson et al.
Θ^+	2, 0, 0	1540	1540
$N_{\overline{10}}$	1, 1/2, 1/2	1684	1665
$\Sigma_{\overline{10}}$	0, 1, 1	1829	1786
Ξ^{--}	-1, 3/2, -3/2	1962	1906

Carlson et al. [PLB579\(2004\)52](#)

NO kinetic energy, NO η' -meson exchange

NO symmetry breaking in η -meson exchange

NO orbital excitation in the radial matrix elements

→ conflict with POSITIVE parity

N.B. Updated partial wave analysis gives 1680 MeV or 1730 MeV,

Arndt et al., [nucl-th/0312126](#)

N.B. Smaller splitting in the CS model

V. Dmitrasinovic & F. S.

- * **Totally antisymmetric q^4 wave fct., NO $\bar{3}$ $S=0, I=0$ diquarks**
- * **Full CS interaction**
- * **Broken SU(3) by the quark masses**

$$M = M_0 - 58 Y$$

M_0 is fixed by the Θ^+ mass $\rightarrow M(\Xi^{--}) \simeq 1710$ MeV

THE MIXING IN THE FLAVOUR-SPIN MODEL

$$V = \begin{cases} \frac{2\sqrt{2}}{3}(m_s - m_u) + \frac{\sqrt{2}}{3} [S(uuds\bar{s}) - S(uudd\bar{d})] = 166 \text{ MeV} & \text{for } N \\ \frac{2\sqrt{2}}{3}(m_s - m_u) + \frac{\sqrt{2}}{3} [S(uuss\bar{s}) - S(uuds\bar{d})] = 155 \text{ MeV} & \text{for } \Sigma \end{cases}$$

$$S = \langle T \rangle + \langle V_\chi \rangle$$

Physical states

$$\begin{aligned} |N^*\rangle &= |N_8\rangle \cos \theta_N - |N_{10}\rangle \sin \theta_N, \\ |N_5\rangle &= |N_8\rangle \sin \theta_N + |N_{10}\rangle \cos \theta_N \end{aligned}$$

$\theta_N = 35.34^\circ \rightarrow M(N_5) = 1801 \text{ MeV}$ is 67 % antidecuplet

$\theta_\Sigma = -35.48^\circ \rightarrow M(\Sigma_5) = 2046 \text{ MeV}$ is 67 % antidec.

N. B. Ideal mixing $\theta_N = 35.26^\circ$, $\theta_\Sigma = -35.26^\circ$

$M(N^*) = 1451 \text{ MeV}$ is 67 % pentaquark octet

Also a q^3 state $N(1440) = 1495 \text{ MeV} \rightarrow$

TWO resonances in the Roper region (P. Morsch et al. PRL '99)

$M(\Sigma^*) = 1719 \text{ MeV}$ is 67 % pentaquark octet

SOME RECENT CONSTITUENT QUARK MODEL RESULTS

Takeuchi & Shimizu, hep-ph/0411016

FS model - semirelativistic version - Graz

The lowest state is $J^P = 1/2^+$

CS model - nonrelativistic one gluon exchange

1) The lowest resonant state is $J^P = 3/2^-$

2) The $J^P = 1/2^-$ states is lower, but in the continuum

CONSTITUENT QUARK MODELS

- * One can accommodate Θ^+ and partners
- * absolute mass is not determined

- * $\Xi^{--} - \Theta^+$ mass difference is model dependent
- * Coupling $\overline{10}_F$ & 8_F due to $SU_F(3)$ breaking \rightarrow IDEAL mixing

- * 2 states: q^3 and $q^4\bar{q}$ in the Roper mass region \rightarrow higher Fock components for baryon q^3 states

- * small width: $\langle \Theta | KN \rangle$ flavour-spin or orbital space
- * spin-orbit partners