

Two-Colour QCD at finite Baryon density

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Motivation

Why QCD-like theories?

- testing effective theories
- $\mu > 0$ equation of state

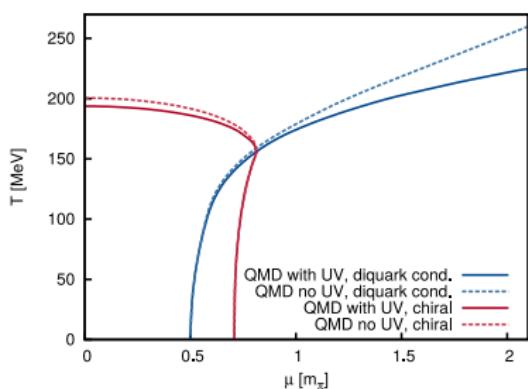
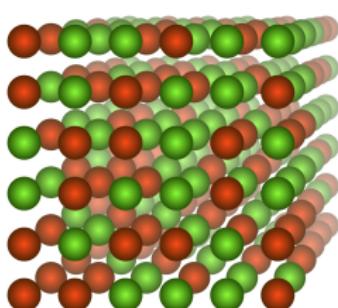


Figure: 2-colour Quark-Meson-Diquark model [Strodthoff, Smekal, Phys. Let. B.2014.03.008]

$$(\det \mathcal{M}(\mu))^* = \det \mathcal{M}(-\mu)$$

- Reweighting
- Taylor expansion
- Lefshetz thimbles
- Complex Langevin
- Effective theories

Outline



- 1 Motivation
- 2 QCD-like theories
- 3 Isospin chemical potential
- 4 G₂-QCD
- 5 QC₂D
- 6 Conclusion

QCD-like theories

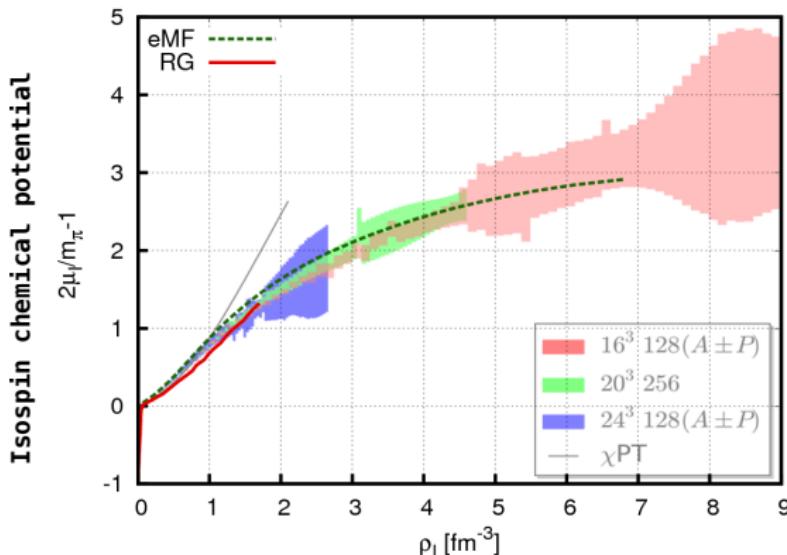
- generator isometry
 \Rightarrow **Anti-unitary sym.**

$$\begin{aligned} T_a^* &= -ST^aS^{-1} \\ \Rightarrow [A, D] &= [SCK, D] = 0 \end{aligned}$$

- Dyson classification
 - $\beta = 1$: $A^2 = +1$, $\det D \in \mathbb{R}$
 - $\beta = 2$: ev. $\in \mathbb{C}$
 - $\beta = 4$: $A^2 = -1$, $\det D > 0$, $\det D \in \mathbb{R}$

Isospin chemical potential

$$\det \mathcal{M}(\mu_I) = \det (D(\mu_I)D(-\mu_I))$$



[Kamikado, Strodthoff, Smekal, PLB 718 (2013) 1044]

[Detmold, Orginos, Shi, Phys. Rev. D86 (2012) 054507]

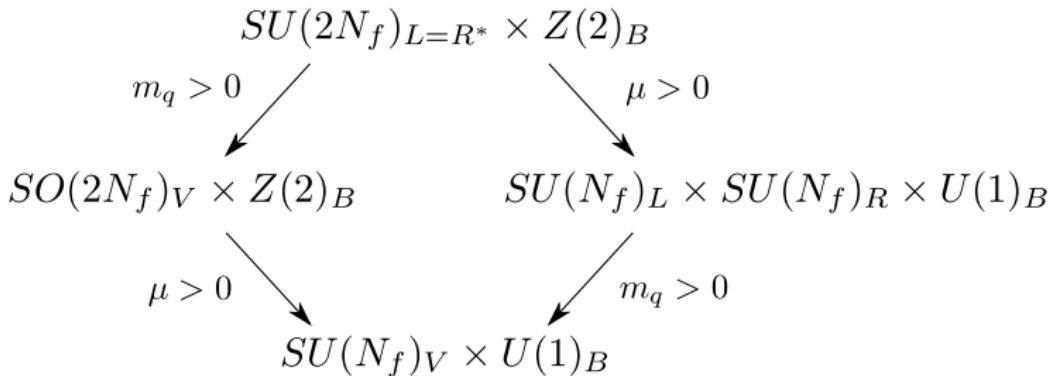
Symmetries of G₂ gauge theoryG₂-QCD

- 7 colours, 14 gluons
- deconf. 1st order

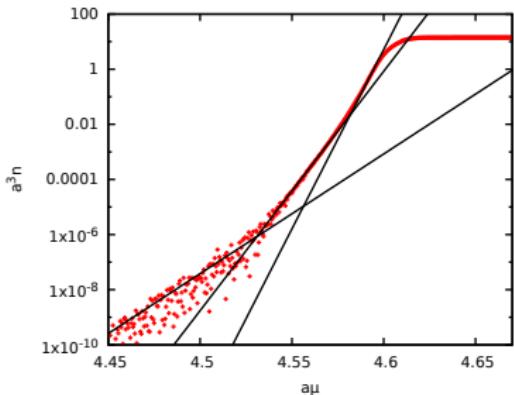
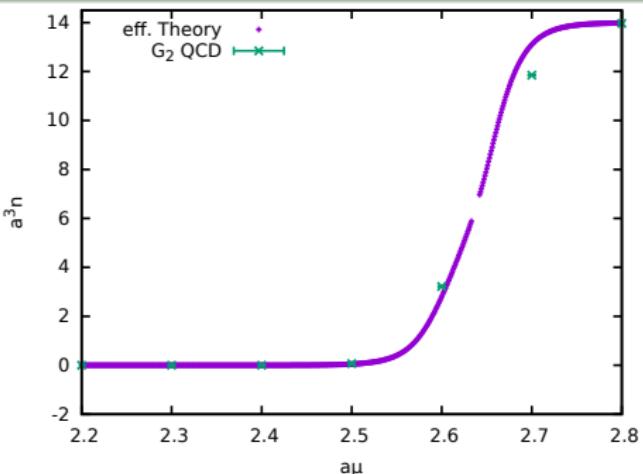
$$SU(3) \subset G_2 \subset SO(7)$$

$$c_{abc} = c_{def} U_{da} U_{eb} U_{fc}$$

$$c_{abc} = \frac{1}{\sqrt{3}} \psi_{abc}$$



Effective G₂ Polyakov loop theory



- diquarks $q^T q$
 - nucleons $(\bar{q}q)q, (q^T q)q$
 - hybrid states $qggg$
 \Rightarrow string breaking in G₂-YM

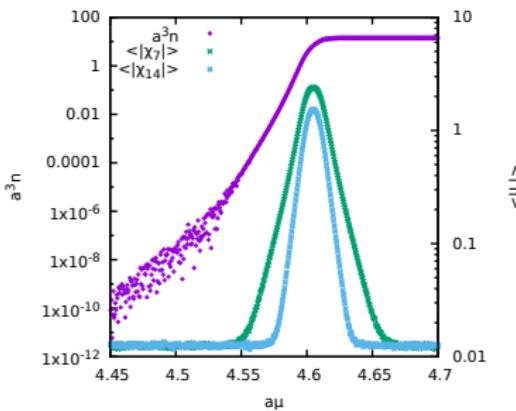


Figure: [P. Scior, PhD thesis, TU Darmstadt 2016]

Previous studies

QC,D

Previous lattice studies:

- Hands et al., Nucl. Phys. B558, 327-346, (1999)
 - Morrison et al., hep-lat/9902012, (1999)
 - Kogut et al., Phys. Let. B514, 77-87, (2001)
 - Kogut et al., Phys. Rev. D68, 1-32, (2003)
 - Boz et al., arXiv/1502.01219, (2015)
 - Braguta et al., arXiv/1605.04090, (2016)
 - **Talk by V. Braguta this morning**

Quark-Meson-Diquark model

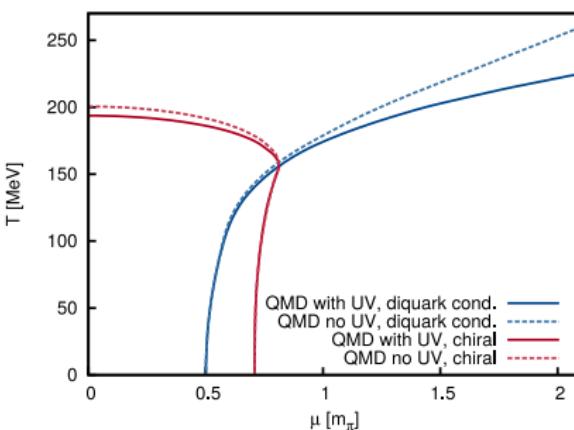
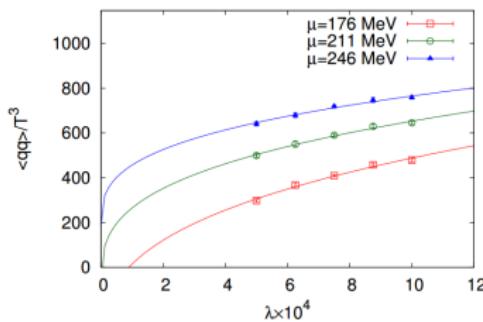
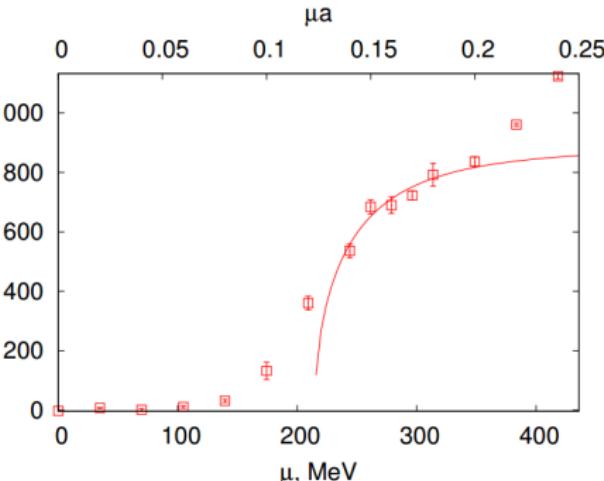
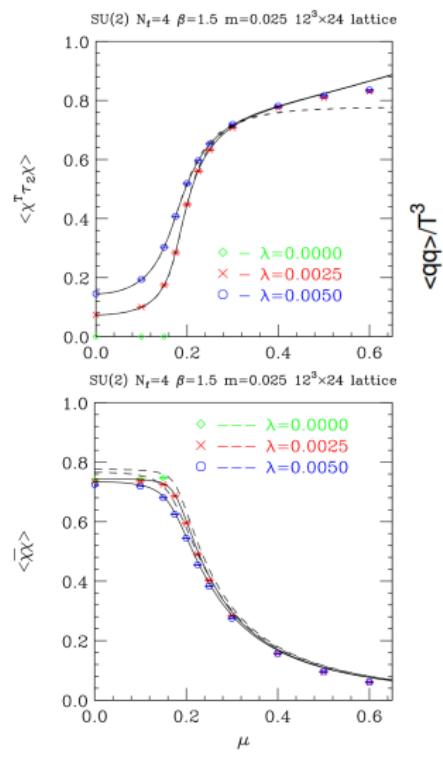


Figure: [Strodthoff, Smekal, Phys. Lett. B.2014.03.008]

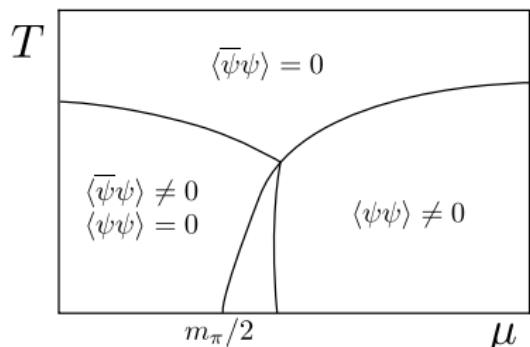
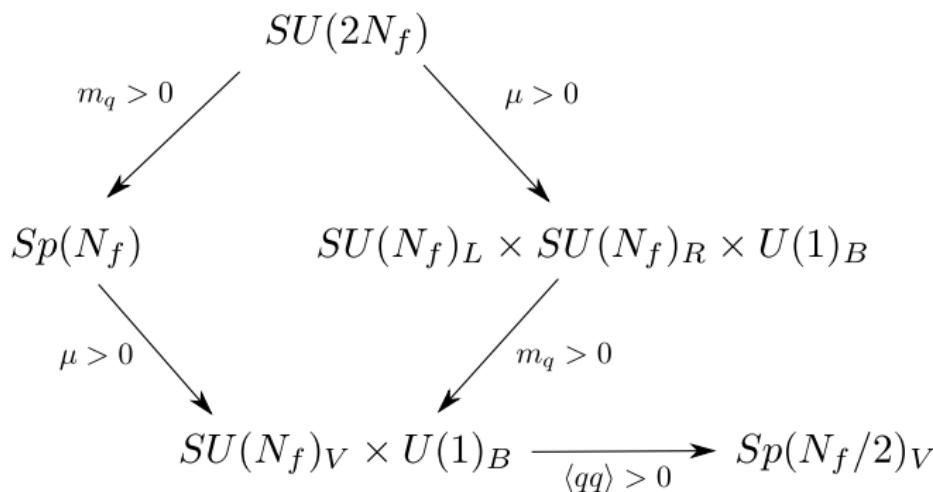
Previous studies



[Kogut, Toublan, PRD68,
054507 (2003)]

[Braguta, Ilgenfritz, Kotov, Molochkov, Nikolaev,
arXiv:1605.04090v3 (2016)]

Extended flavour symmetry



$$T_a^* = -ST^aS^{-1}$$

where $S = i\sigma_2$

q & \bar{q} in equiv. repr.

QC₂D on the lattice

$$S_f = \frac{1}{2} \left(\bar{\psi}, \psi^T \tau_2 \right) \begin{pmatrix} \lambda & D(\mu) \\ -D^\dagger(\mu) & \lambda \end{pmatrix} \begin{pmatrix} \tau_2 \bar{\psi}^T \\ \psi \end{pmatrix}$$

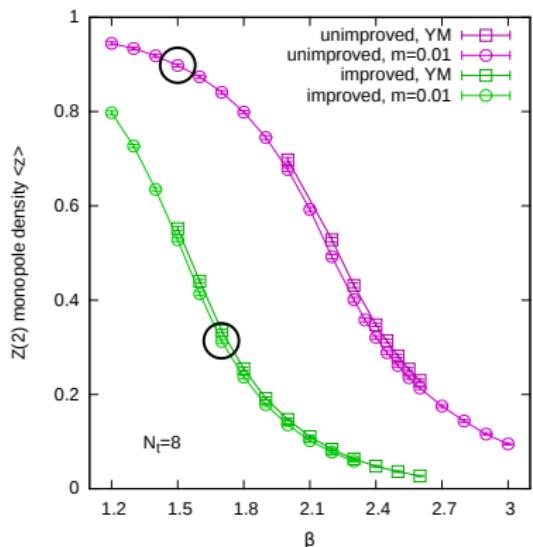


Figure:

$$\langle z \rangle = 1 - \frac{1}{N_\square} \sum_{C \in \square} \prod_{P \in \partial C} \operatorname{sgn} \operatorname{tr} P$$

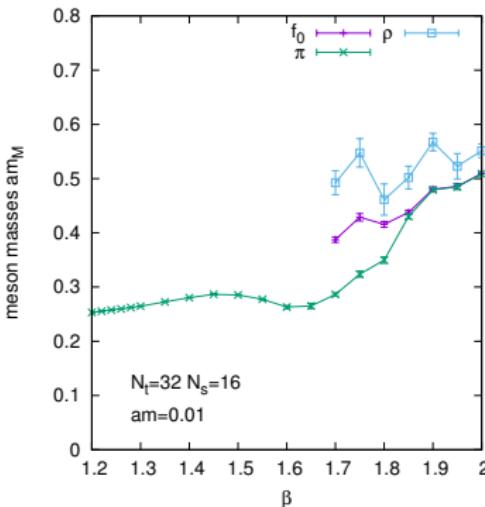


Figure: [D. Scheffler, PhD Thesis,
Technische Universität Darmstadt
(2015)]

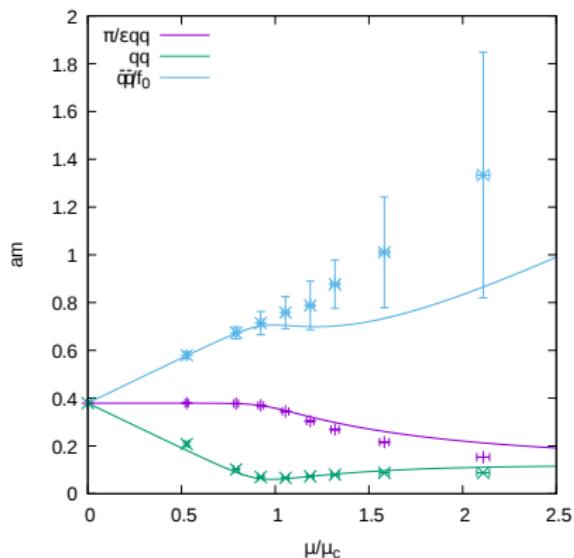
QC₂D with staggered quarks

Figure: $\beta = 1.5$: $\langle z \rangle \approx 0.88404(10)$
Dyson index: $\beta = 4$

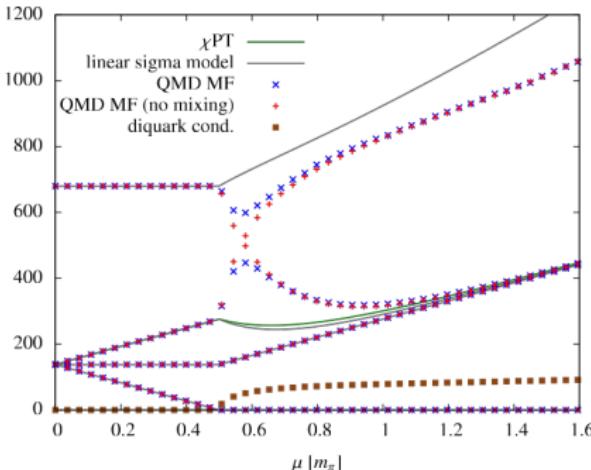


Figure: [Strodthoff, Schaefer, Smekal,
Phys. Rev. D.85.074007]

$$f_0/qq : \frac{1}{2} \left(\chi^T \tau_2 \chi + \bar{\chi} \tau_2 \bar{\chi}^T \right) \cos \alpha + \bar{\chi} \chi \sin \alpha$$

$$\pi/\epsilon qq : \bar{\chi} \epsilon \chi \cos \alpha + \frac{1}{2} \left(\chi^T \tau_2 \epsilon \chi + \bar{\chi} \tau_2 \epsilon \bar{\chi}^T \right) \sin \alpha$$

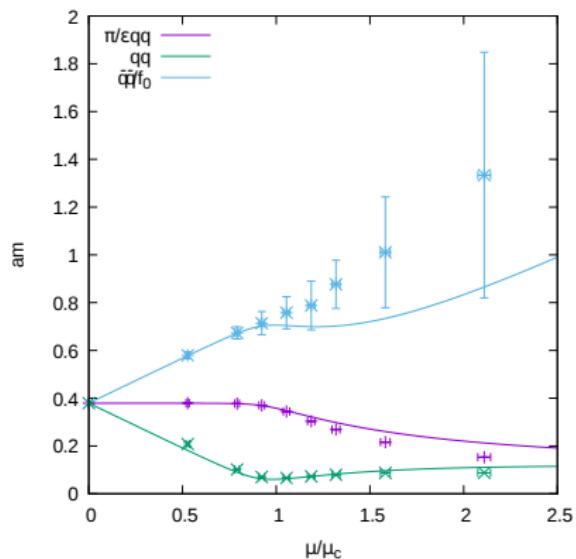
QC₂D with staggered quarks

Figure: $\beta = 1.5$: $\langle z \rangle \approx 0.88404(10)$
Dyson index: $\beta = 4$
any-colour, adjoint quarks

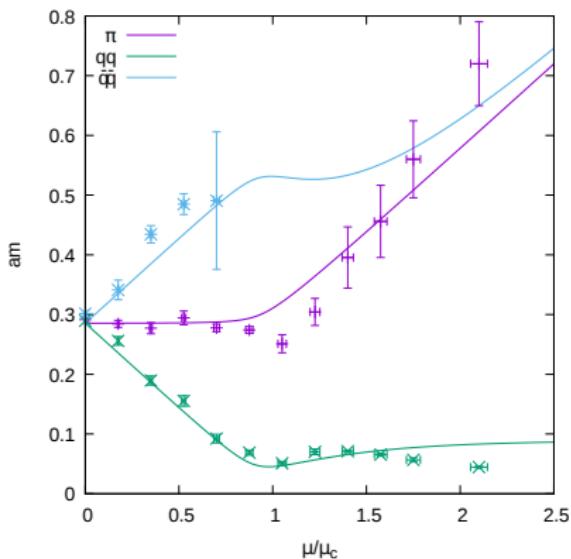
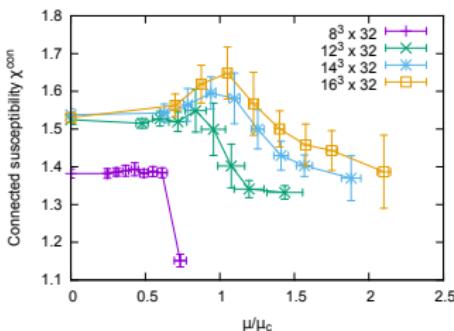
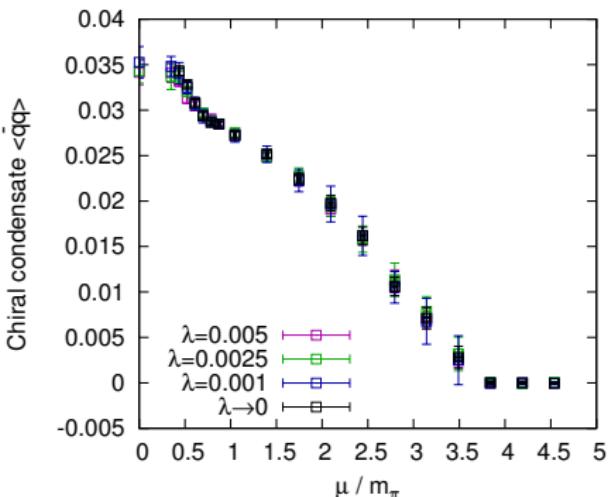
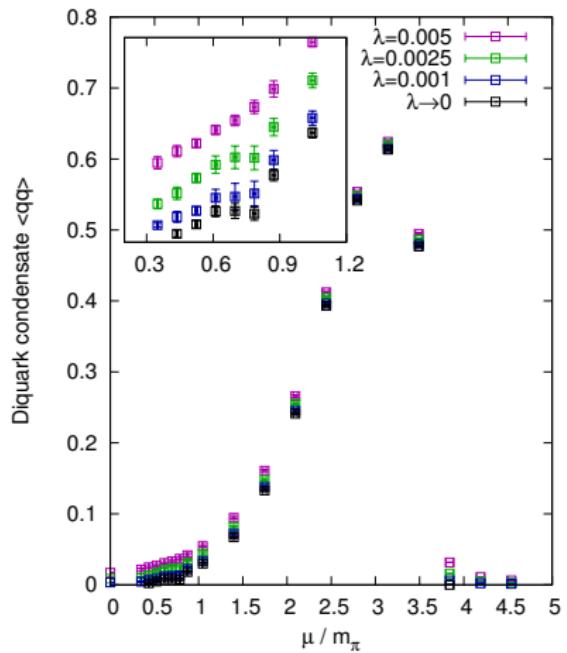
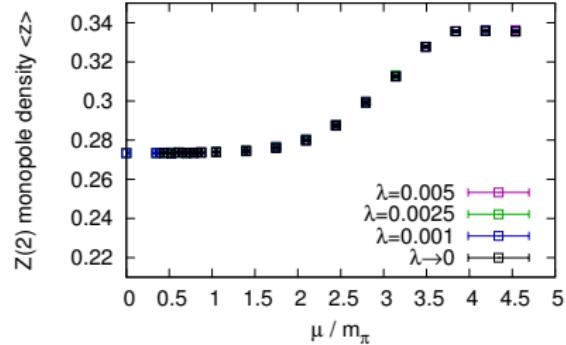
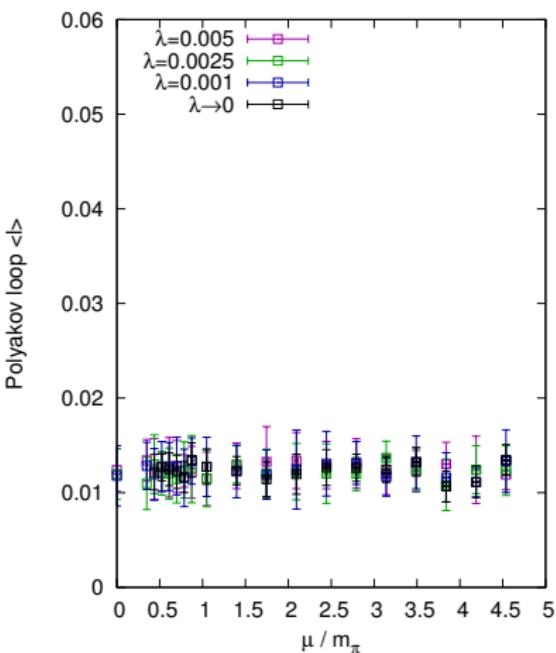
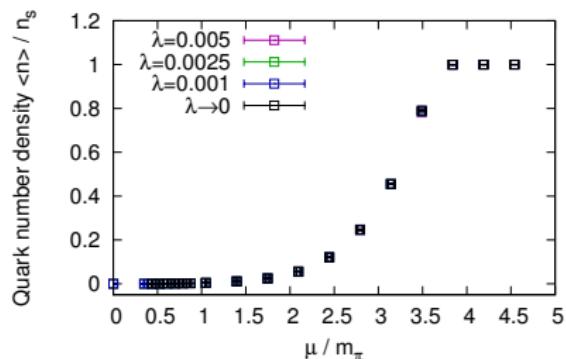
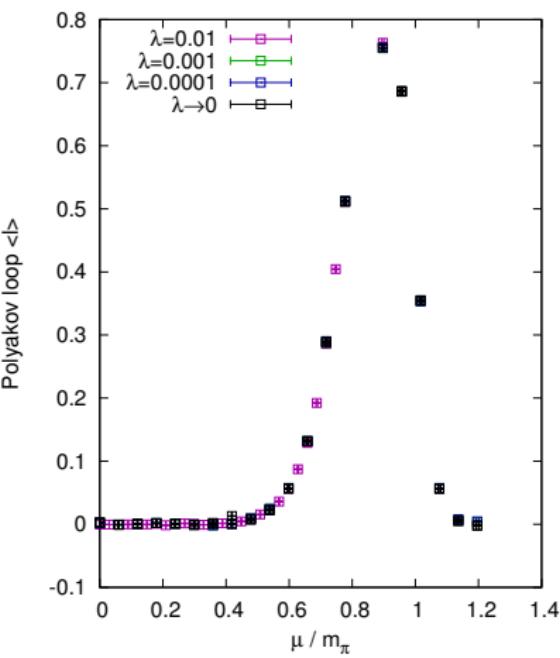
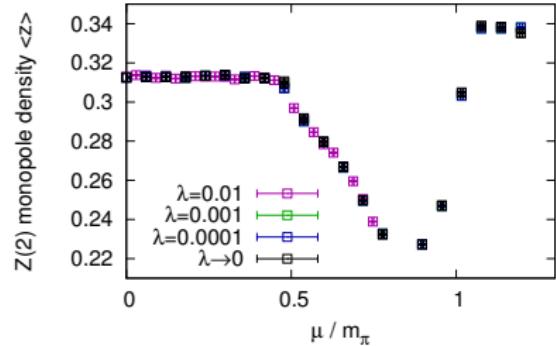
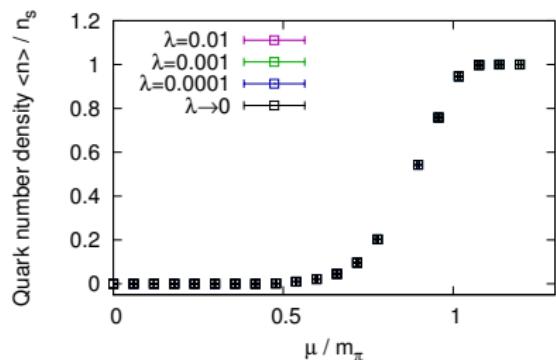


Figure: $\beta = 1.7$: $\langle z \rangle \approx 0.27340(66)$
Dyson index: $\beta = 1$
two-colour, fundamental quarks

QC₂D with staggered quarks

QC₂D with staggered quarks

QC₂D with Wilson quarks



Conclusion

- Leaving the bulk phase
- Continuum sym. breaking pattern $\beta = 4 \rightarrow 1$
- Discretization effects

Outlook:

- Renormalization of $\langle \bar{\psi} \psi \rangle$ at $\mu > 0$