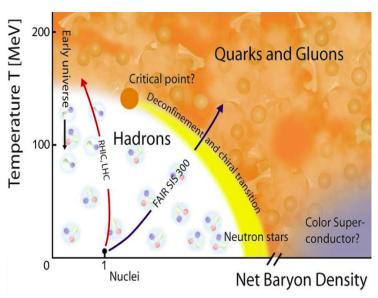
# Phase diagram of dense two-color QCD within lattice simulations

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ITEP

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# QCD phase diagram



# SU(3) QCD

- $Z = \int DUD\bar{\psi}D\psi \exp(-S_G \int d^4x\bar{\psi}(\hat{D} + m)\psi) =$ =  $\int DU \exp(-S_G) \times \det(\hat{D} + m)$
- Eigenvalues go in pairs  $\hat{D}$ :  $\pm i\lambda \Rightarrow$  det  $(\hat{D} + m) = \prod_{\lambda} (\lambda^2 + m^2) > 0$  i.e. one can use lattice simulation
- Introduce chemical potential:  $\det(\hat{D}+m) \to \det(\hat{D}-\mu\gamma_4+m) \Rightarrow$  the determinant becomes complex (sign problem)

#### SU(2) QCD

- Eigenvalues go in pairs  $\hat{D} \mu \gamma_4$ :  $\lambda, \lambda^*$
- For even  $N_f \det(\hat{D} \mu \gamma_4 + m) > 0 \Rightarrow$  free from sign problem



# Differences between SU(3) and SU(2) QCD

- The Lagrangian of the SU(2) QCD has the symmetry:  $SU(2N_f)$  as compared to  $SU_R(N_f) \times SU_L(N_f)$  for SU(3) QCD
- Goldstone bosons ( $N_f=2$ )  $\pi^+,\pi^-,\pi^0,d,\bar{d}$

#### Similarities:

- There are transitions: confinement/deconfinement, chiral symmetry breaking/restoration
- A lot of observables are equal up to few dozens percent:

Topological susceptibility (Nucl.Phys.B715(2005)461):

$$\chi^{1/4}/\sqrt{\sigma} = 0.3928(40) \ (SU(2)), \ \chi^{1/4}/\sqrt{\sigma} = 0.4001(35) \ (SU(3))$$

Critical temperature (Phys.Lett.B712(2012)279):

$$T_c/\sqrt{\sigma} = 0.7092(36) (SU(2)), \quad T_c/\sqrt{\sigma} = 0.6462(30) (SU(3))$$

#### Shear viscosity:

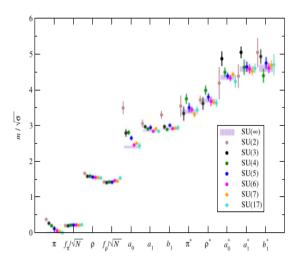
$$\eta/s = 0.134(57) (SU(2)), \quad \eta/s = 0.102(56) (SU(3))$$

JHEP 1509(2015)082

Phys.Rev. D76(2007)101701

#### Similarities:

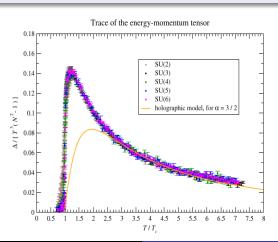
• Spectroscopy (Phys.Rep.529(2013)93)



#### Similarities:

- Thermodynamic properties (JHEP 1205(2012)135)
- Some properties of dense medium (Phys.Rev.D59(1999)094019):

$$\Delta \sim \mu g^{-5} \exp\left(-rac{3\pi^2}{\sqrt{2}g}
ight)$$



- Dense SU(2) QCD can be used to study dense SU(3) QCD
  - Calculation of different observables
  - Study of different physical phenomena
- Lattice study of SU(2) QCD contains full dynamics of real system (contrary to phenomenological models)

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#### Details of the simulation:

- Staggered fermions with rooting:  $N_f = 2$
- Lattice  $16^3 \times 32$ , a=0.11 fm,  $m_\pi=362(4)$  MeV, T=55 MeV
- Diquark source in the action  $\delta S \sim \lambda \psi^T (C\gamma_5) \times \sigma_2 \times \tau_2 \psi$

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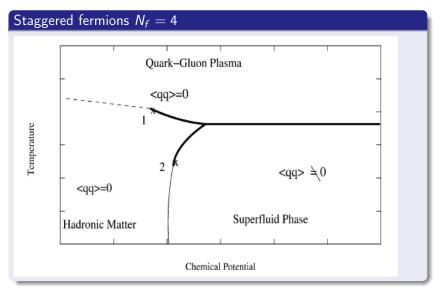


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- Talk of Lukas Holicki (15:40)

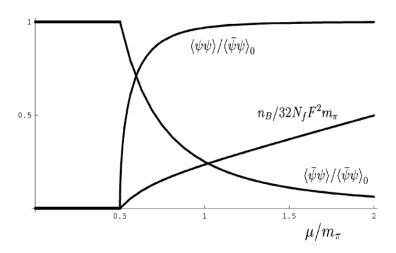




J.B. Kogut, D. Toublan, D.K. Sinclair, Nucl. Phys. B 642 (2002) 181-209

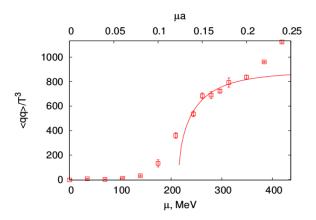
#### One can build CHPT for SU(2) QCD

#### Predictions of CHPT



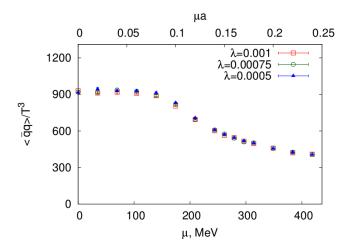
# Small chemical potential $\mu < 350$ MeV

# Diquark condensate



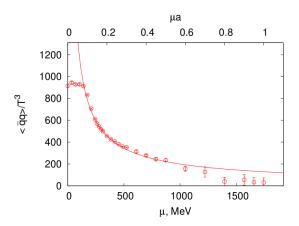
- Good agreement with CHPT  $\langle \psi \psi \rangle / \langle \bar{\psi} \psi \rangle_0 = \sqrt{1 \frac{m_\pi^4}{\mu^4}}$
- Phase transition at  $\mu \sim m_\pi/2$
- Bose Einstein condensate (BEC) phase  $\mu \in (200, 350)$  MeV

#### Chiral condensate



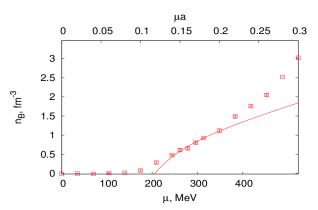
# Good agreement with CHPT

#### Chiral condensate



- CHPT prediction  $\langle \bar{\psi}\psi \rangle \sim \frac{m_\pi^2}{\mu^2}$
- We observe  $\langle \bar{\psi}\psi \rangle \sim \frac{1}{\mu^{\alpha}}, \alpha \sim 0.6-1.0$

# Baryon density



- Good agreement with CHPT  $n \sim \mu \frac{m_{\pi}^4}{u^3}$
- Phase transition at  $\mu \sim m_\pi/2$
- Departure from CHPT prediction starts from  $n \sim 1 \text{ fm}^{-3}$

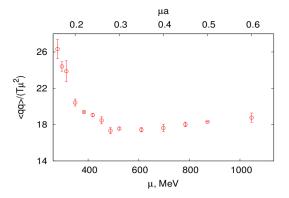
# Large chemical potential $\mu > 350$ MeV

### Phase diagram for $N_c ightarrow \infty$

(L. McLerran, R.D. Pisarski, Nucl. Phys. A796 (2007) 83-100)

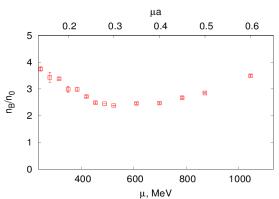
- Hadron phase  $\mu < M_N/N_c \ (p \sim O(1))$
- Dilute baryon gas  $\mu > M_N/N_c$  (width  $\delta \mu \sim \frac{\Lambda_{QCD}}{N_c^2}$ )
- Quarkyonic phase  $\mu > \Lambda_{QCD} \; (p \sim N_c)$ 
  - Degrees of freedom:
    - Baryons (on the surface)
    - Quarks (inside the Fermi sphere  $|p| < \mu$ )
  - No chiral symmetry breaking
  - The system is in confinement phase
- Deconfinement  $(p \sim N_c^2)$

#### Diquark condensate



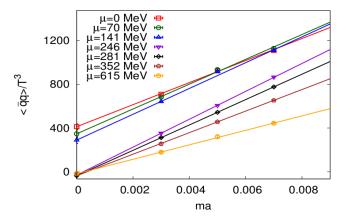
- Bardeen–Cooper–Schrieffer (BCS) phase  $\mu >$  500 MeV,  $\langle \psi \psi \rangle \sim \mu^2$
- Baryons (on the surface)

# Baryon density



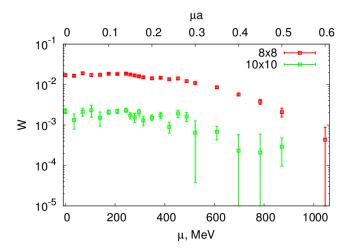
- Free quarks  $n_0=N_f imes N_c imes (2s+1) imes \int rac{d^3p}{(2\pi)^3} heta(|p|-\mu)=rac{4}{3\pi^2}\mu^3$
- Quarks inside Fermi sphere
- Quarks inside Fermi sphere dominate over the surface:  $\frac{4}{3}\pi\mu^3 > 4\pi\mu^2\Lambda_{QCD} \Rightarrow \mu > 3\Lambda_{QCD} \ (n \sim (5-10) \times \text{nuclear density})$

#### Chiral condensate (chiral limit $m \to 0$ )



### No chiral symmetry breaking

#### Wilson loop



# The system is in confinement phase

• Baryons (on the surface)

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✓

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 $\checkmark$ 

ullet Quarks (inside the Fermi sphere  $|{m p}|<\mu$ )

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#### We observe quarkyonic phase

One can expect that there is quarkyonic phase in SU(3) theory

#### Conclusion:

- We observe  $\mu < m_{\pi}/2$  hadronic phase
- ullet Transition to superfluid phase  $\mu \simeq m_\pi/2$  (BEC)
- ullet  $\mu > m_\pi/2, \mu < m_\pi/2 + 150$  MeV dilute baryon gas
- Hadronic phase and BEC phase are well described by CHPT
- Deviation from CHPT from  $\mu >$  350 MeV (dense matter)
- ullet BCS phase  $\mu\sim$  500 MeV, transition BECoBCS is smooth
- BCS phase is similar to quarkyonic phase

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# Predictions for SU(3) (estimation!):

- Quarkyonic phase starts from  $n \sim (5-10) \times$  nuclear density
- Restoration of chiral symmetry  $((5-10)\times nuclear density) \Rightarrow$  can be seen in experiment



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Monte-Carlo simulation of SU(2) QCD is the best approach to study properties of SU(3) QCD at large baryon density

