

Супермагнетизм:

свойства и приложения.

I Суперпарамагнетизм.

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- Thermodynamic Formalism
 mean field approximation
Noble & transitional metals
- **MAGNETIC Nano-Crystals**
 Transition metals if iron series
 Band Structure based shell model
- **FerroFluids**
 Lab on a Chip systems

Thermodynamic Formalism

Potential $\Omega = -T \cdot \ln \mathcal{Z},$

Partition function

$$\mathcal{Z} = \text{Tr}(\exp\{-\frac{1}{T}(\hat{\mathcal{H}} - \sum_{\mathbf{N}} \hat{N}_{\mathbf{N}} \lambda_{\mathbf{N}})\})$$

Magnetization

$$\mathcal{P} = M/V \quad M = -\left(\frac{\partial \Omega}{\partial H}\right)_{T,\lambda}$$

Magnetic susceptibility

$$\chi = (1/V) \left(\frac{\partial M}{\partial H} \right)_{T,\lambda} = -(1/V) \left(\frac{\partial^2 \Omega}{\partial H^2} \right)_{T,\lambda}$$

Number Density

$$N_N = - \frac{\partial \Omega}{\partial \lambda_N}$$

$$D_N = N_N / V$$

To Canonical ensemble

$$F \approx \sum_N N_N \lambda_N + \Omega$$

Mean Field approximation

$$\hat{h}_N = \frac{\hat{\mathbf{p}}_N^2}{2m_N} + V_N(\mathbf{r}) + V_{\text{so}}(\mathbf{r}) + \delta h_N^{\text{m}}$$

Magnetic field \mathbf{B}

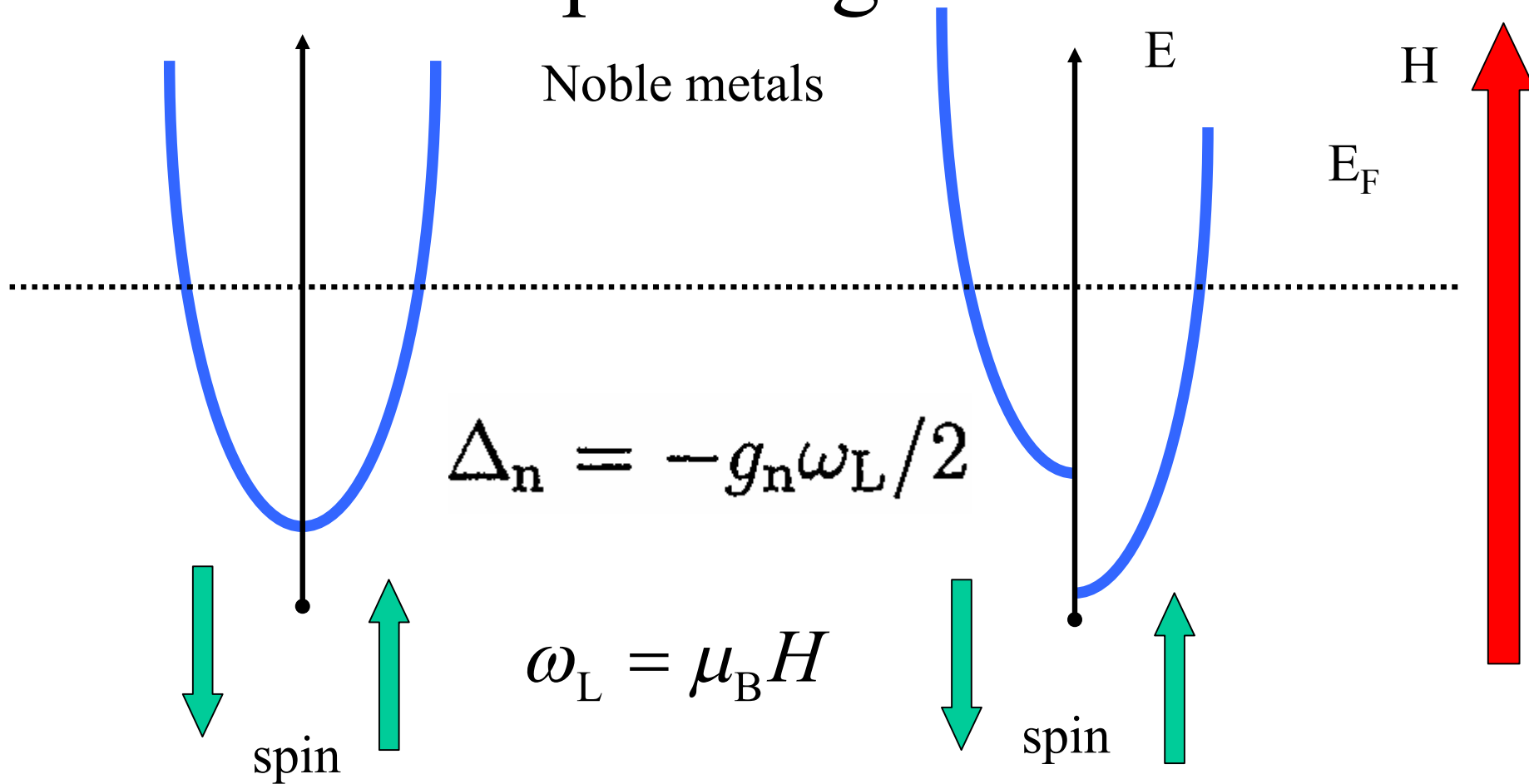
$$\delta h_N^{\text{m}} = -\mathbf{B} \hat{\mathcal{M}}_N + \delta h_o^{\text{m}},$$

Level deensity

$$\rho_N(\epsilon) = \sum_{\zeta} \delta(\epsilon - \epsilon_{\zeta}^N)$$

$$\Omega_N = -T \int_{-\infty}^{\infty} d\epsilon \rho_N(\epsilon) \cdot \ln[1 + \exp\{(\lambda_N - \epsilon)/T\}].$$

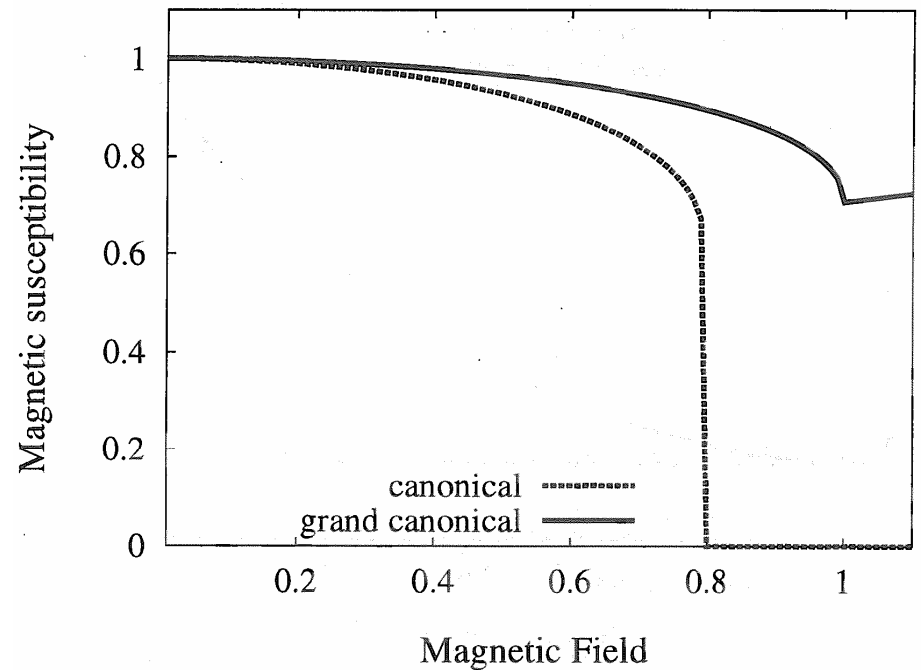
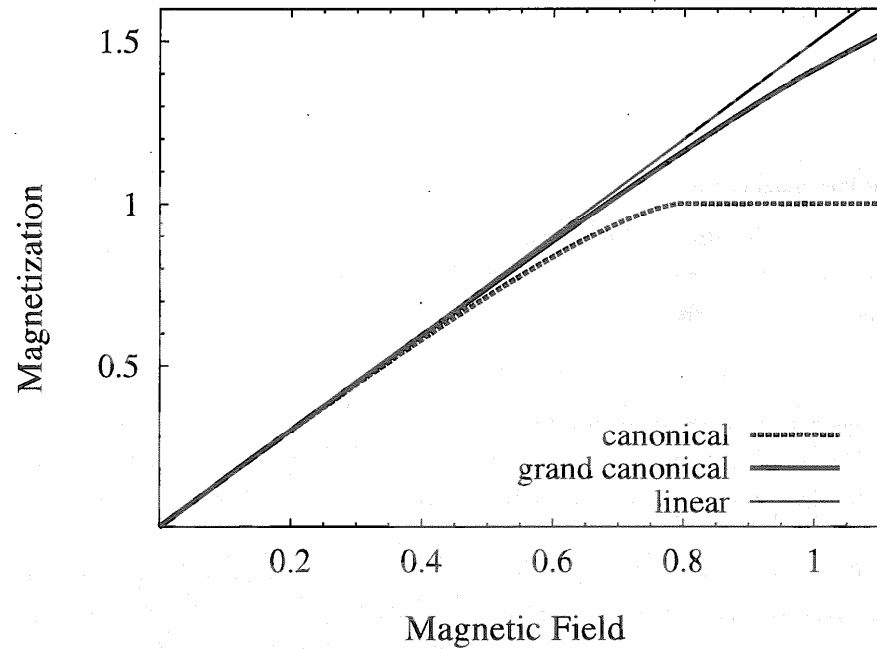
Pauli spin magnetization



$$M_n = \frac{1}{2} g_n \mu_N \mathcal{N},$$

$$\mathcal{N} = N_{n+} - N_{n-}$$

Magnetization & susceptibility



Landau Diamagnetism

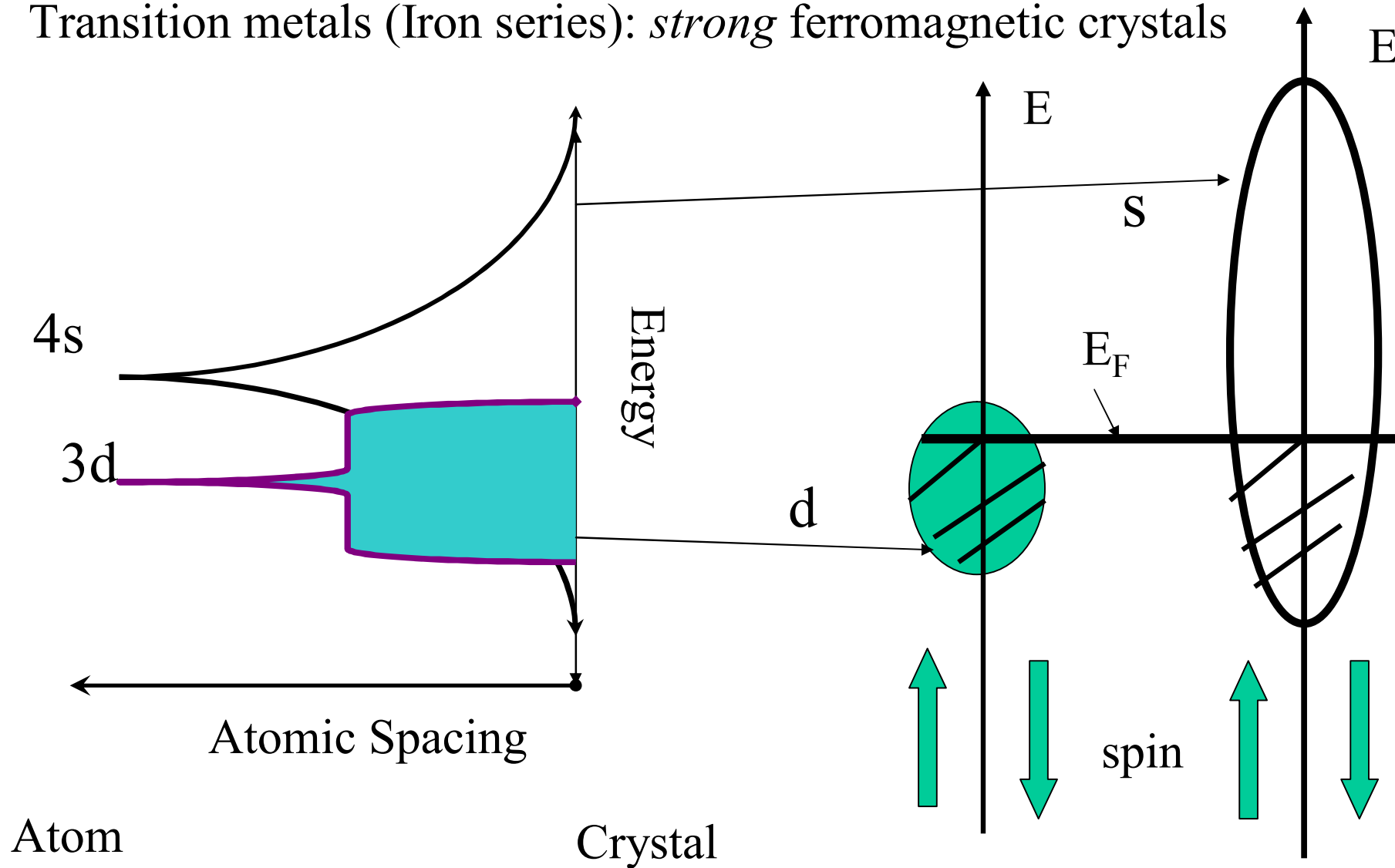
$$\epsilon_n \equiv \left(n + \frac{1}{2}\right)\hbar\omega_c$$

Landau levels

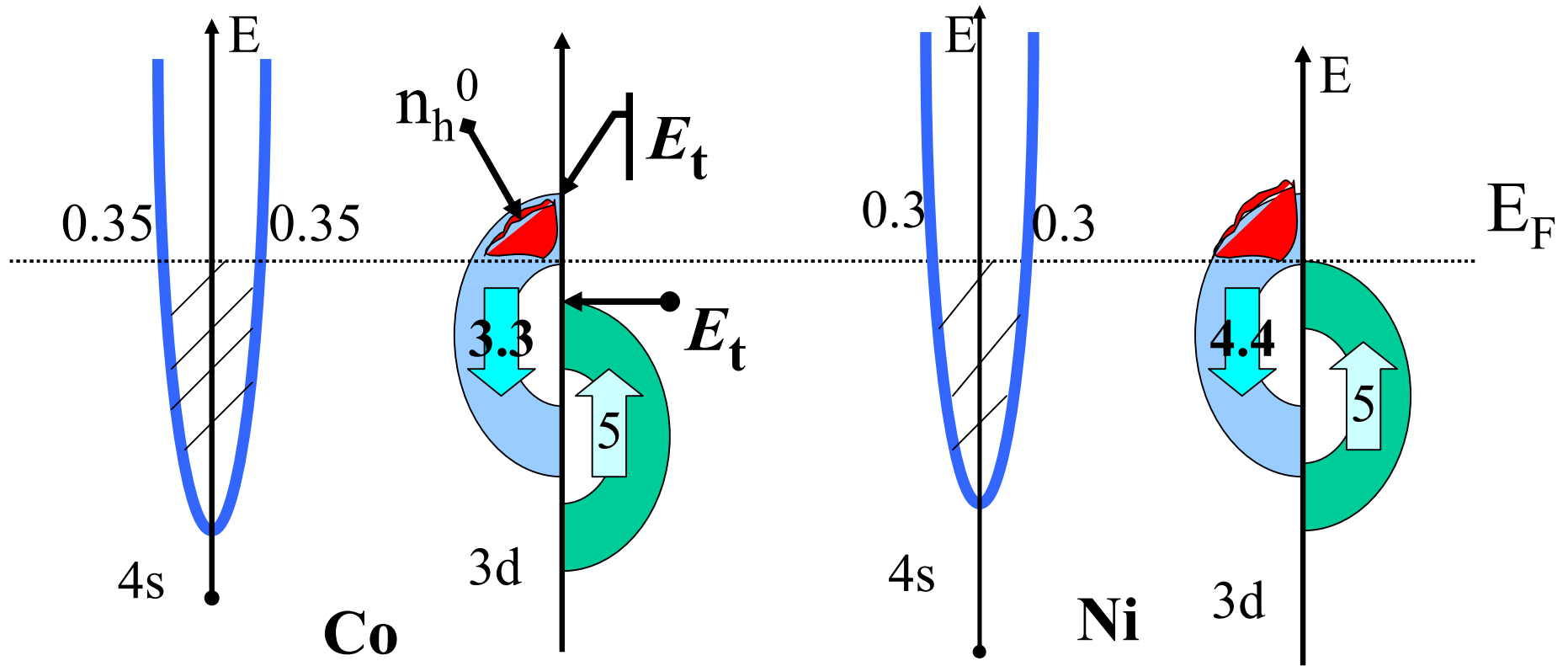
$$\Omega(H) = -k_B T \frac{Am}{\pi\hbar^2} \hbar\omega_c \sum_n \ln[1 + e^{\beta(\mu - \epsilon_n)}],$$

$$\chi_{dia}^{(3d)} = -\frac{e^2}{12\pi mc^2} \int_{-k_F}^{k_F} \frac{dk_z}{2\pi} = -\frac{e^2 k_F}{12\pi^2 mc^2}.$$

Transition metals (Iron series): *strong* ferromagnetic crystals



strong ferromagnets: Bulk



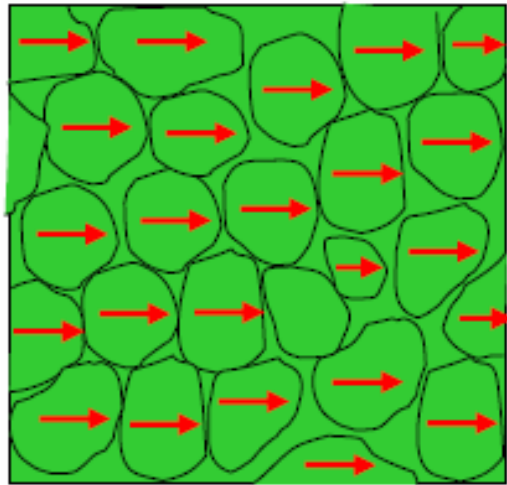
the *iron series* transition metals

$$n_h^0 = 10 - n_v + n_s^0$$

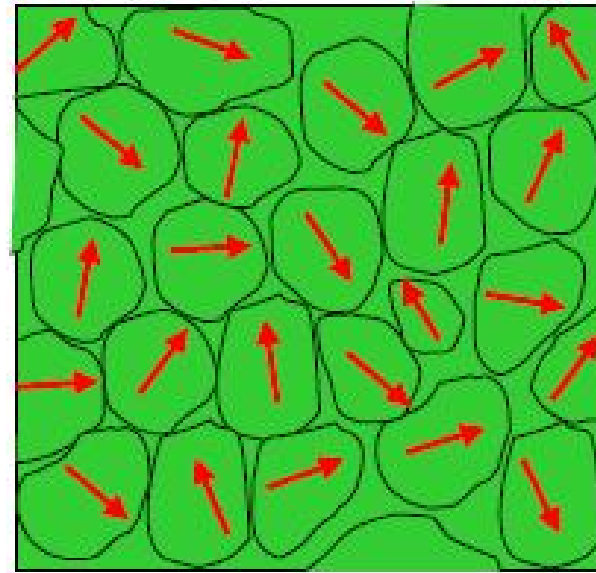
Magnetization

$$M \sim \mu_B n_h^0$$

Demagnetizing energy



$$E \sim M^2$$



Domain Radius

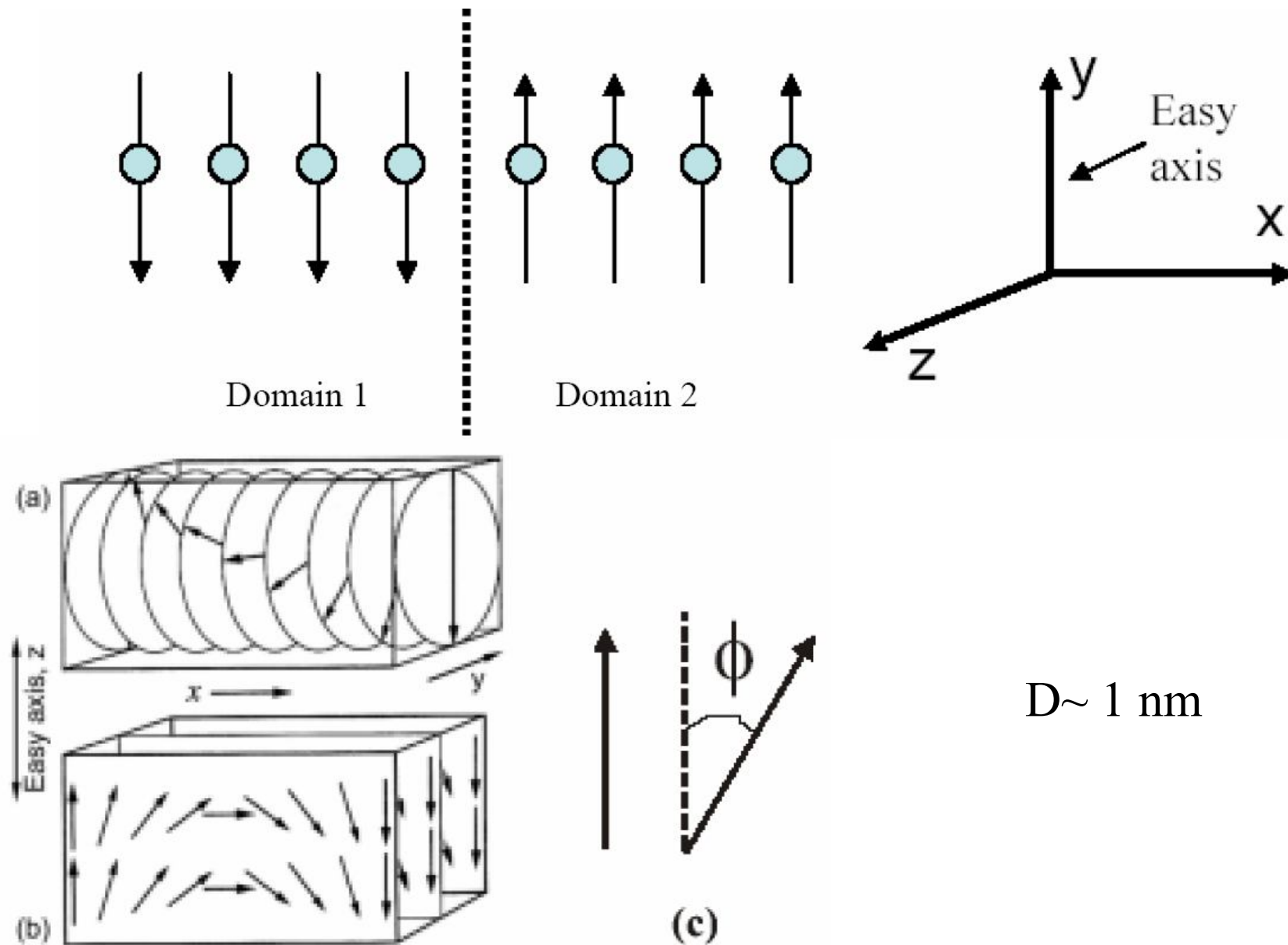
$$r_c \approx 9 \frac{(AK_u)^{1/2}}{\mu_0 M_s^2} \sim 10 \text{ nm}$$

A is the exchange

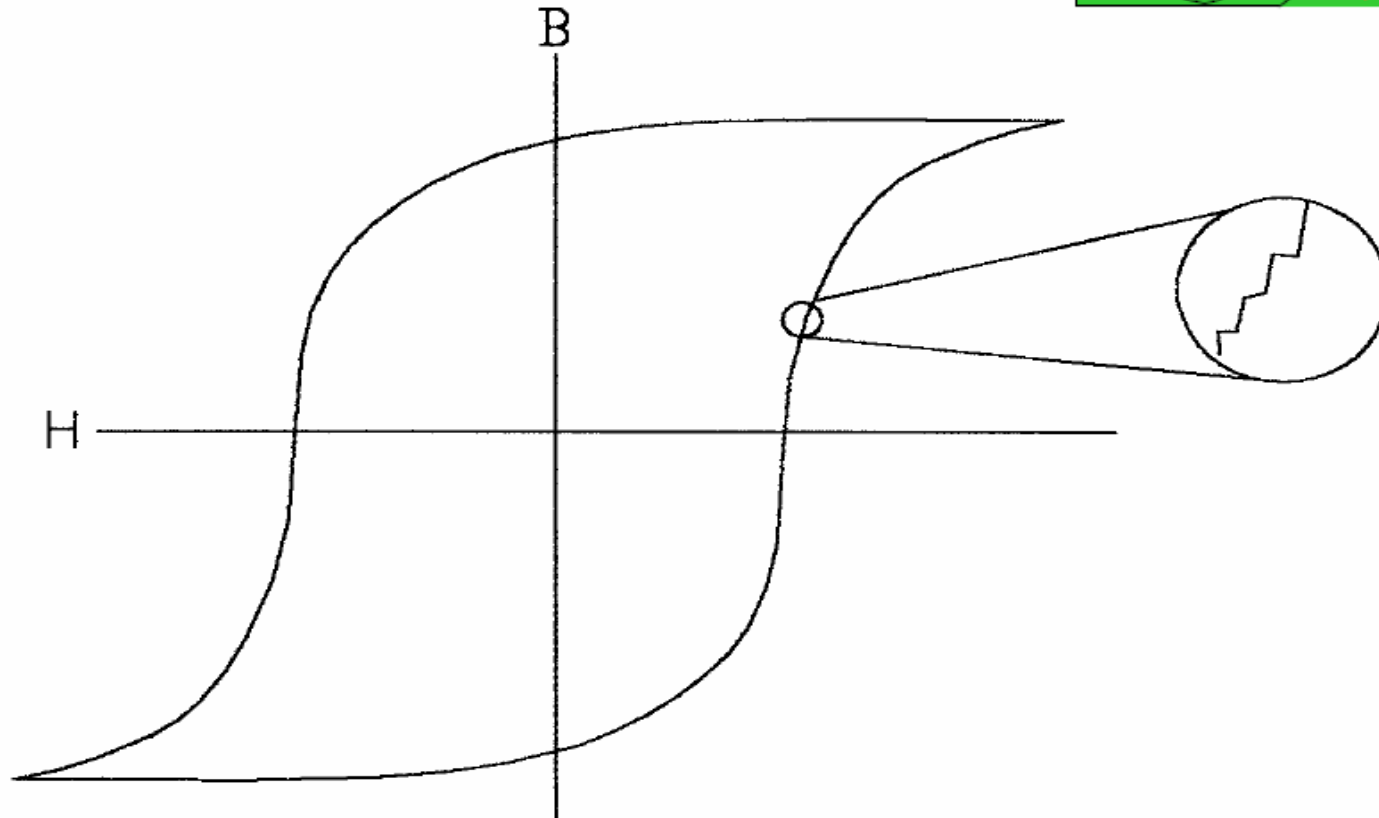
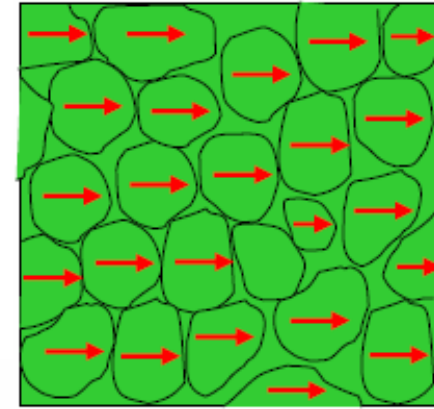
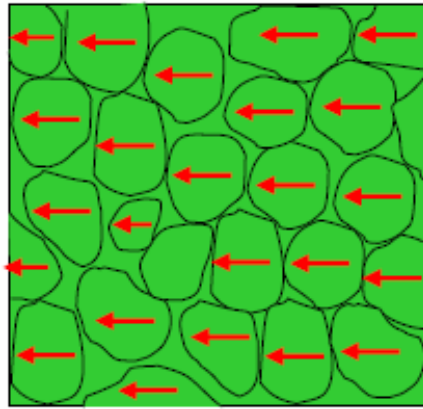
K_u the uniaxial anisotropy constant

μ_0 the vacuum permeability M_s the saturation magnetization.

Domain walls

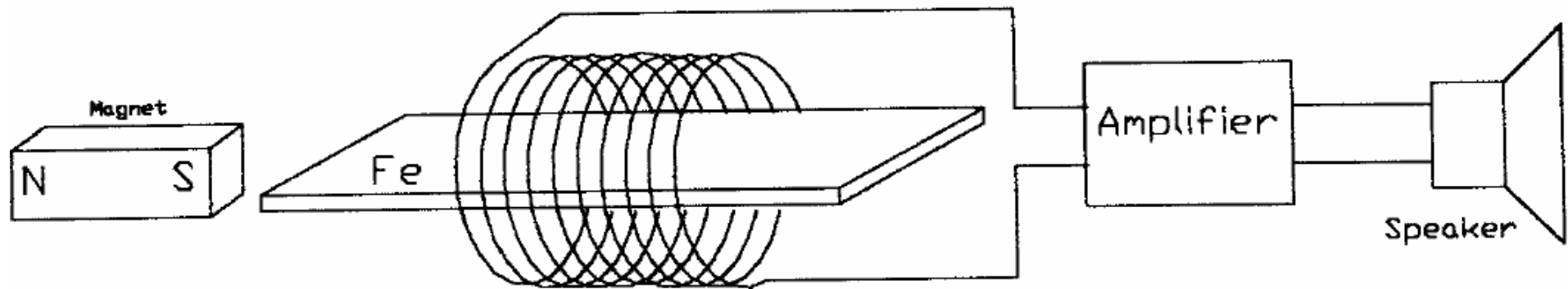


Magnetization reversal hysteresis loop



Barkhausen noise

originates from magnetization jumps

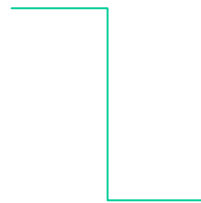


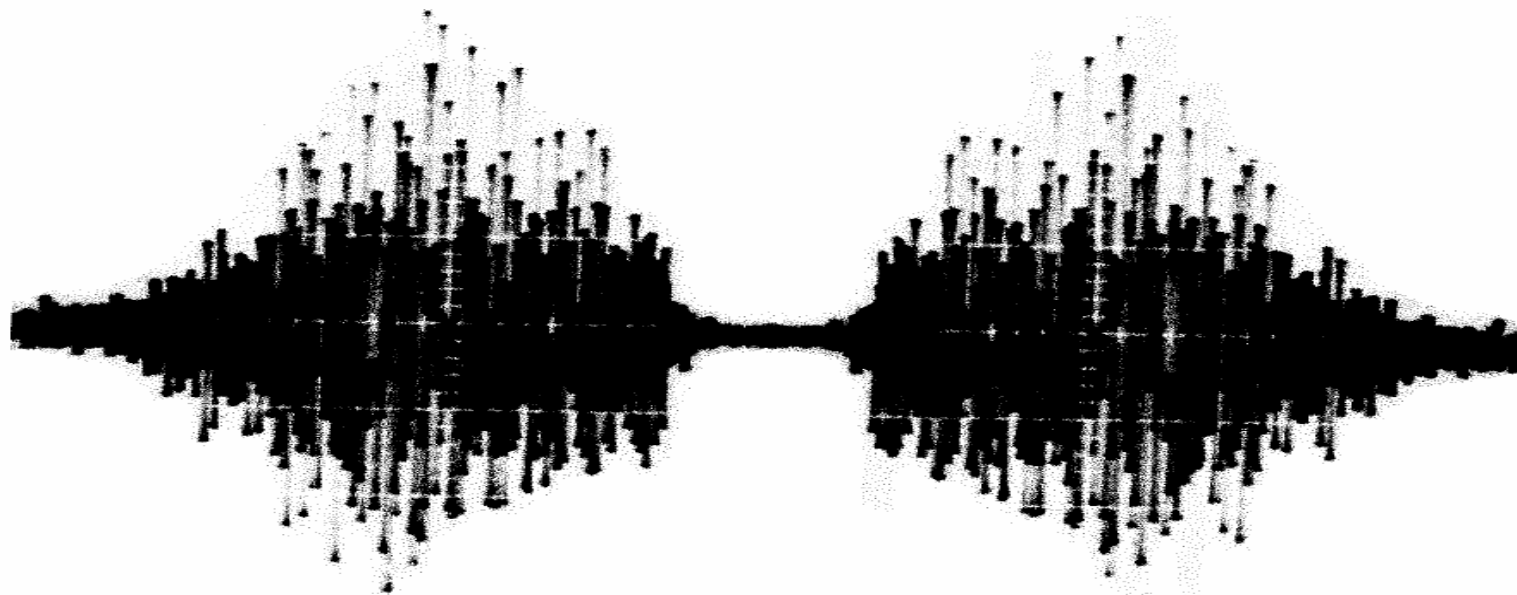
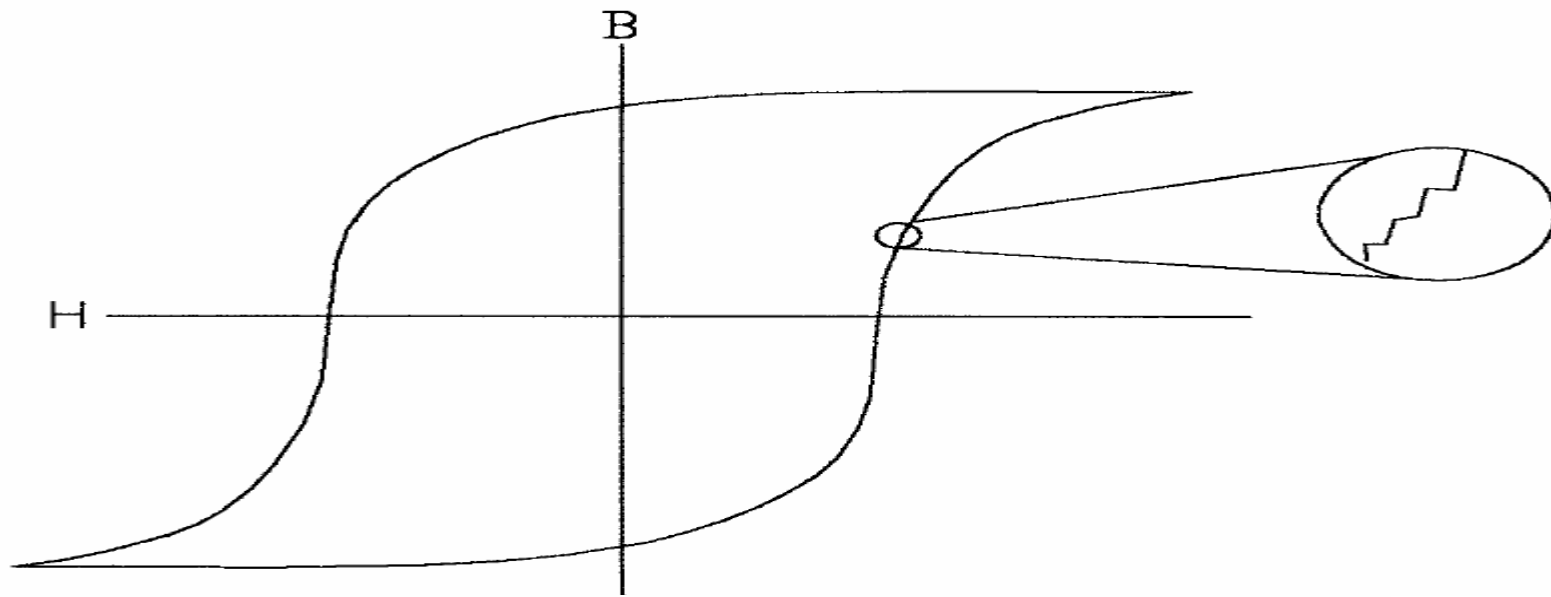
Simplified Barkhausen Noise Detection System

Field jump

Coil Current flux

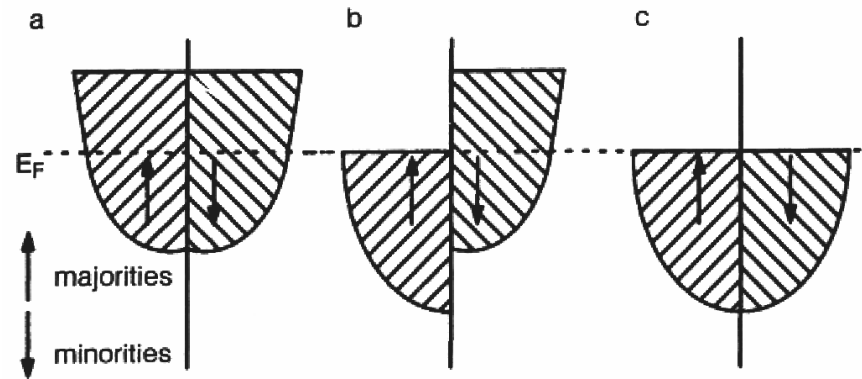
Speaker noise



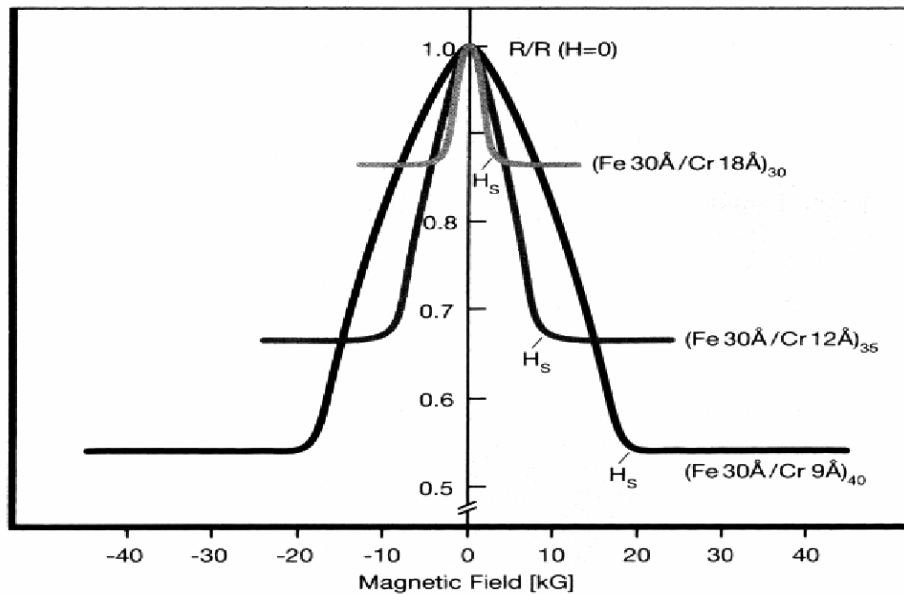


Photographic Scan of Barkhausen Emission Pulse

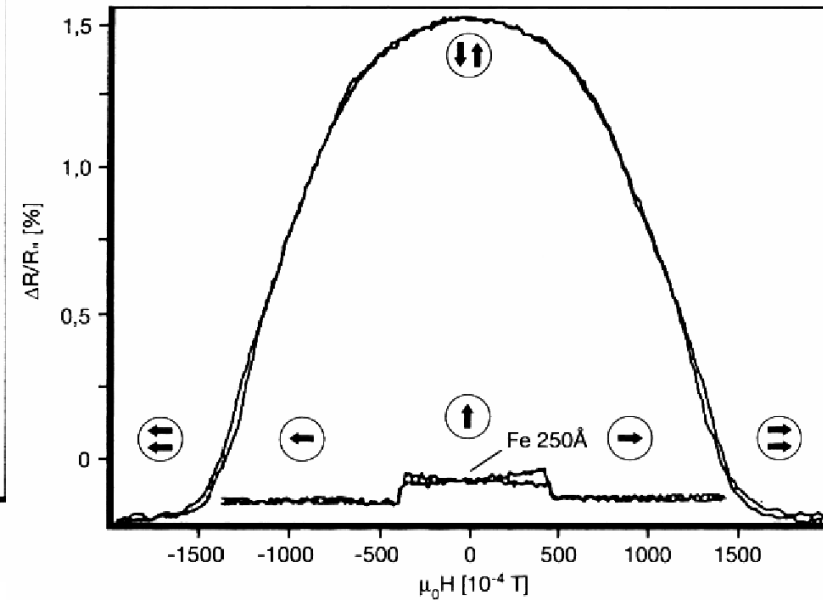
Giant magnetoresistance



Schematic representation of the matching of the d bands of the magnetic



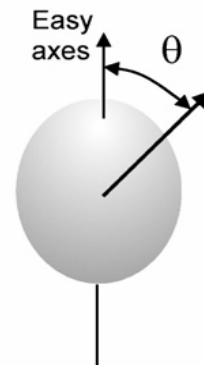
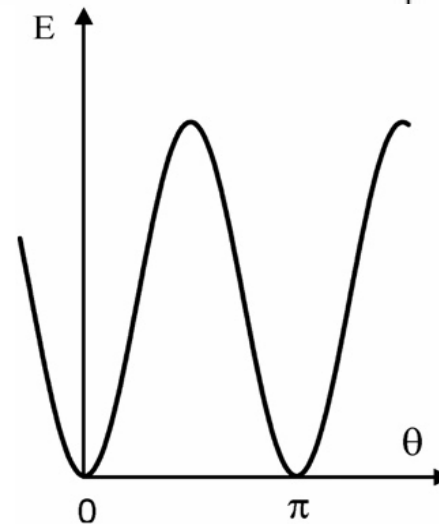
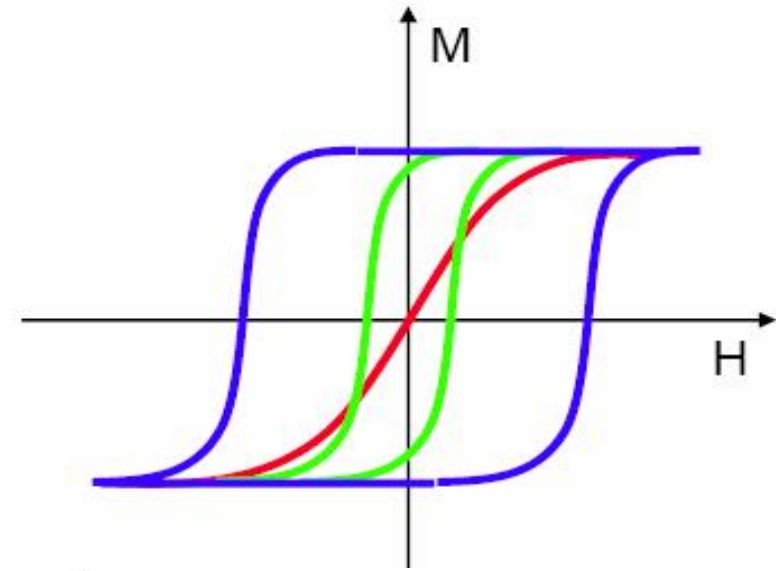
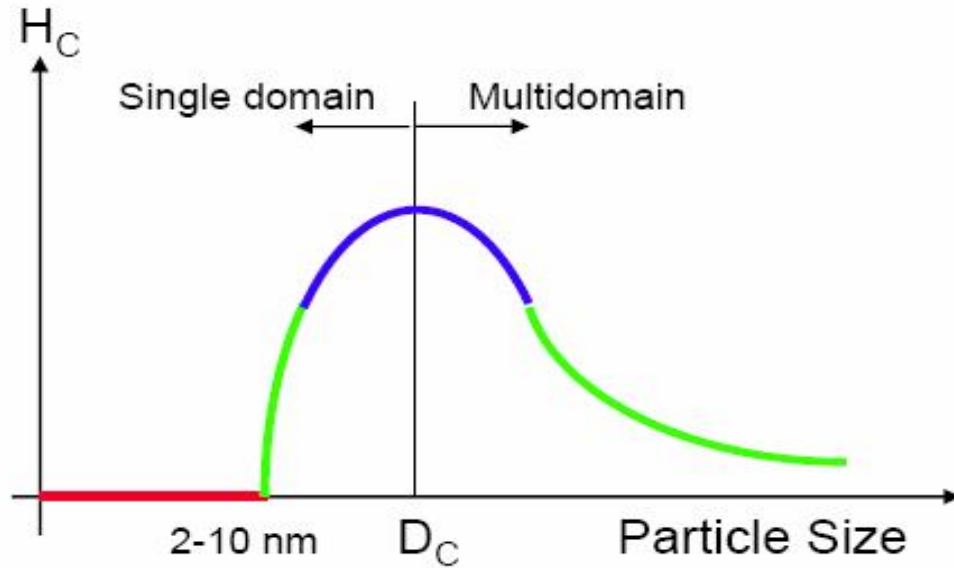
Resistivity versus applied field for Fe/Cr multilayers



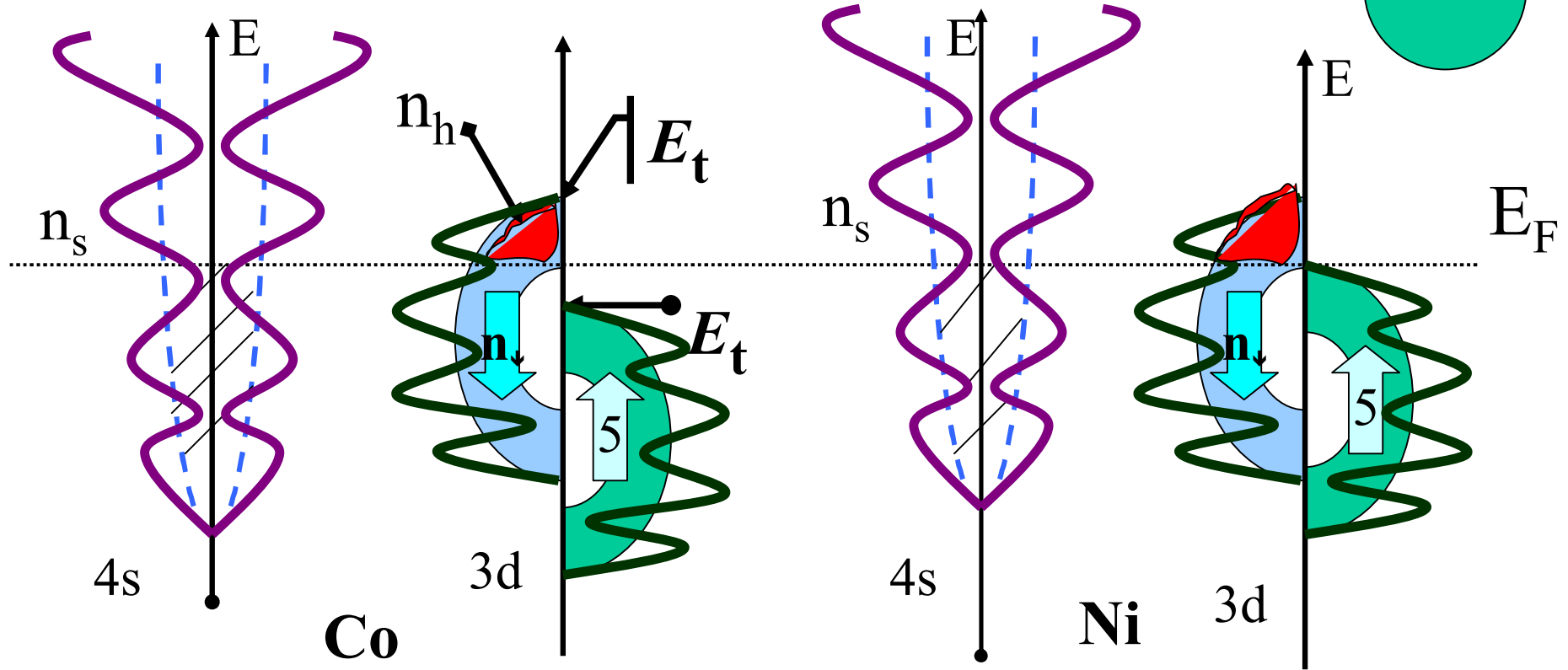
Relative resistance change as a function of the external magnetic field for Fe/Cr/Fe and 250Å thick Fe film

SUPERPARAMAGNETISM - A SIZE EFFECT

Magnetic Properties of Nanostructured Materials:



strong ferromagnets: Nanoparticle



the *iron series* transition metals

Superparamagnetic state

$$n_h = n_h^0 - \delta n_s^D$$

$$M \sim \mu_B n_h$$

VNK, H.O.Lutz, PRL **81** (1998) 4508

Shell Effects

at *Strong Magnetic Fields*

$$n_s(\mu) = \int d\varepsilon \rho_s(\varepsilon) f(\varepsilon - \mu)$$

Electrons

$$f(x) = \left[1 + \exp\{x / k_B T\} \right]^{-1}$$

Level density

$$\rho = \sum_n \delta(\varepsilon - \varepsilon_n) = \rho^{sm} + \rho^{sh}$$

With Single particle levels ε_n filled up to
the Fermi energy ε_F

the Hartree self-consistent mean field approach in magnetic field : \hbar

- Single particle Hamiltonian
- $\mathbf{H} = \mathbf{H}_{\text{MF}} + (\text{Magnetic terms})$
- Landau-orbital (l) \rightarrow $-\mathbf{M}(\hbar l)$

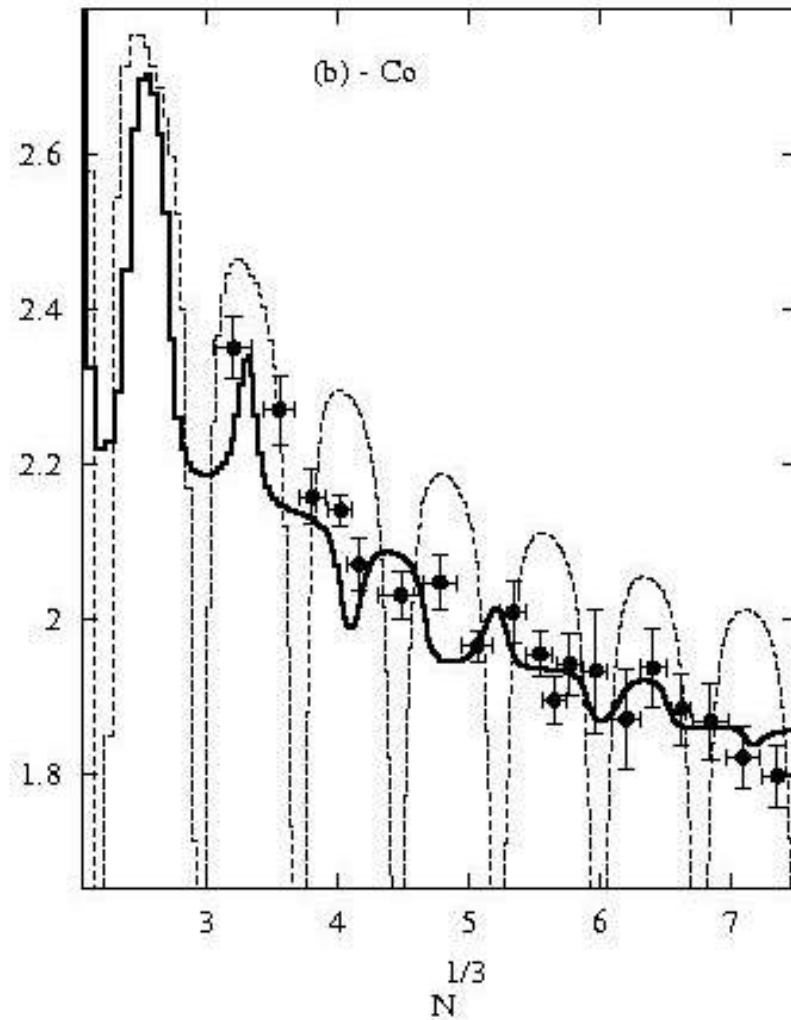
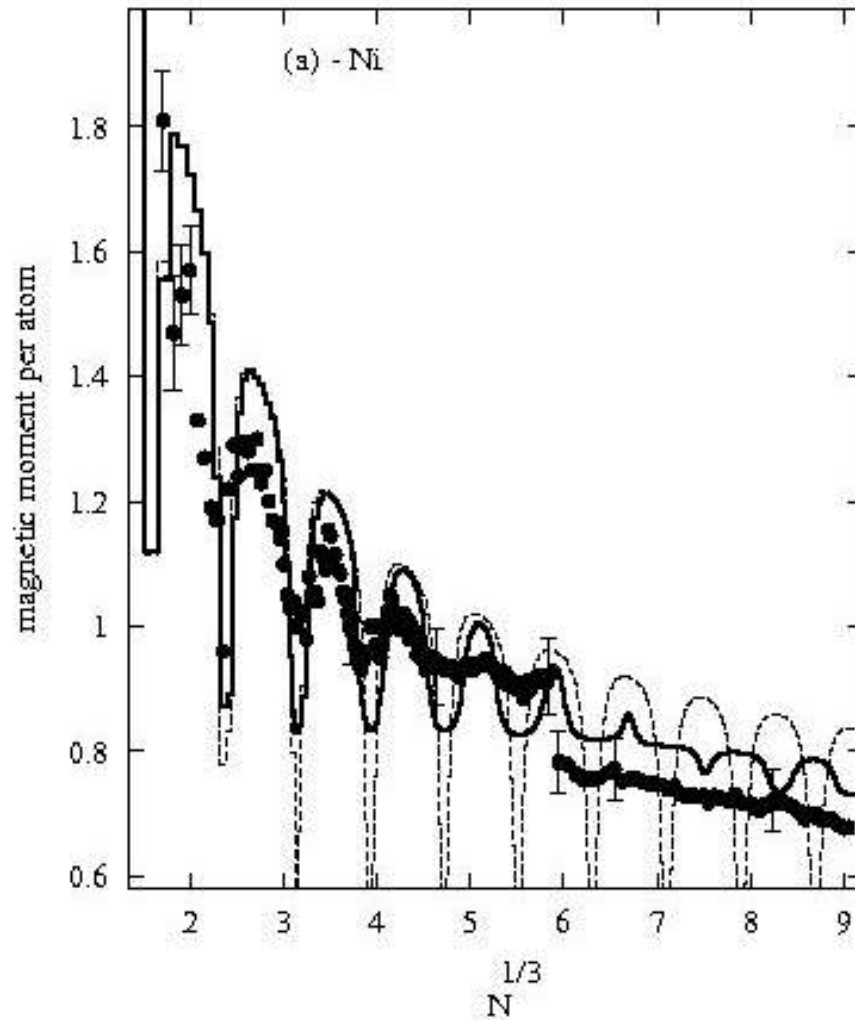
HO level density: $\mathbf{H}_{\text{MF}} = \mathbf{H}_{\text{HO}}$

$$\rho^{sh} = \sum_{k=1} \cos(2\pi k\varepsilon / \omega) j_0(2\pi\eta k\varepsilon / \omega) \times q^k$$

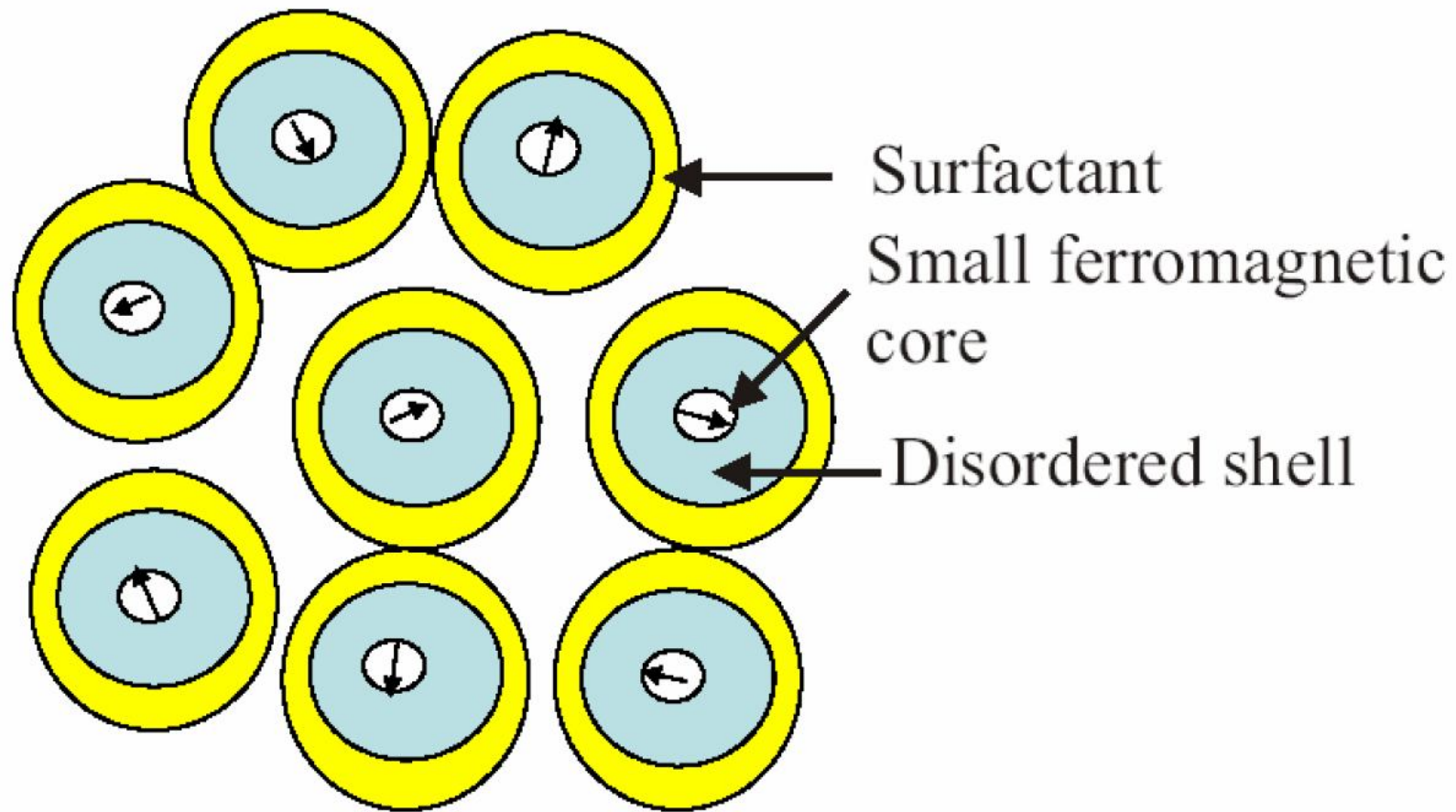
$$\eta = \omega_L / \omega \qquad \omega_L = \mu_B H$$

Size dependence of cluster magnetic moment per atom (measured in μ_B)

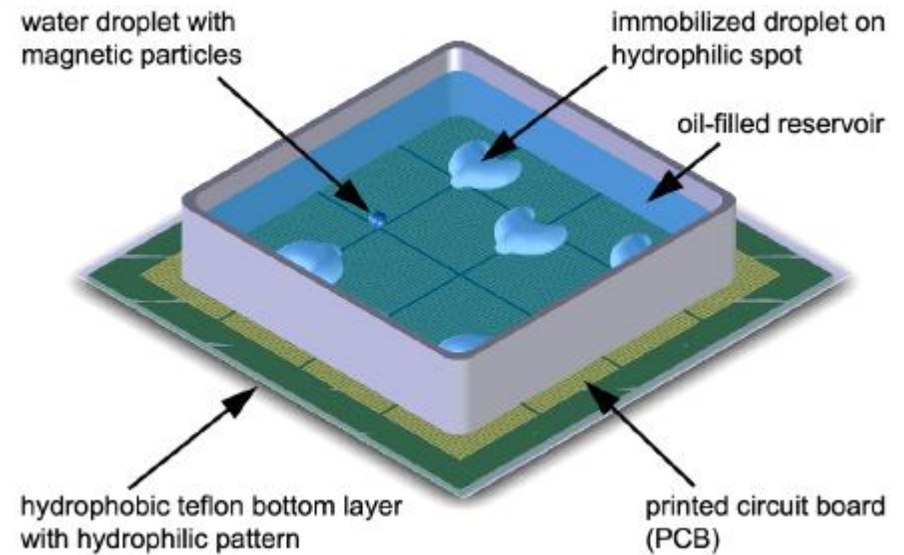
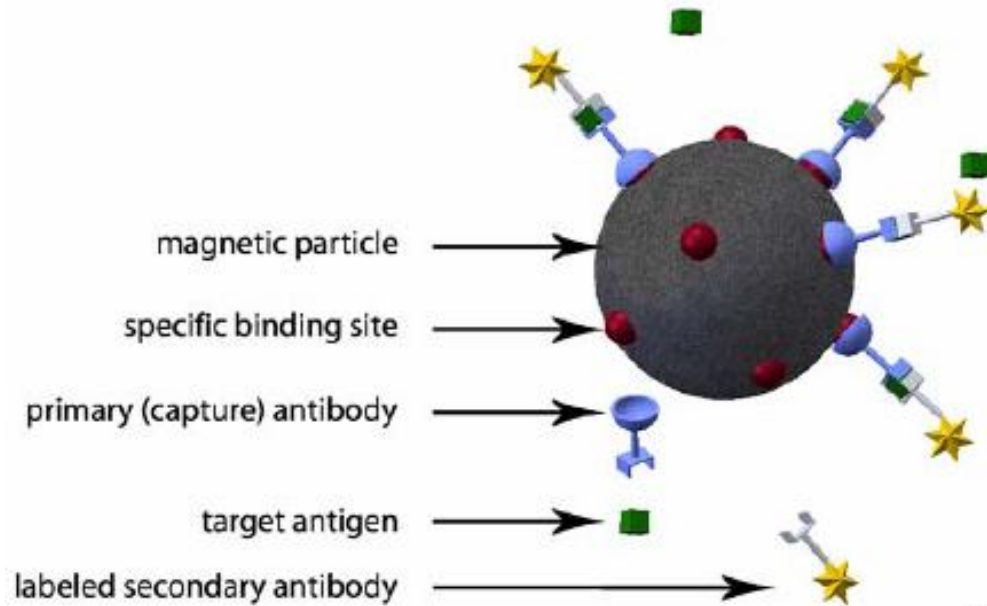
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FerroFluid



Lab on a chip Systems



APPLICATIONS OF SUPERPARAMAGNETISM

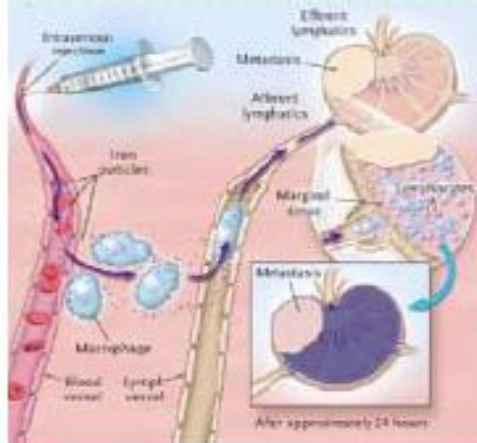
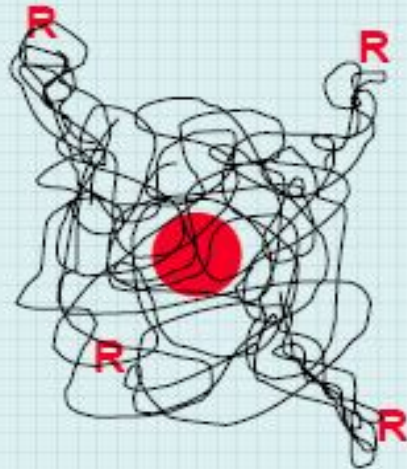
Biomedical applications

- **Detection:** MRI Magnetic Resonance Imaging
- **Separation:** Cell-, DNA-, protein- separation, RNA fishing
- **Treatment:** Drug delivery, hyperthermia, magnetofaction

Other applications:

- **Ferrofluid:** Tunable viscosity
- **Sensors:** high sensitivity (GMR, BARCIII)
- Self - Assambling

Drug Delivery:



Particles with attached drug can be injected and guided through the body by application of an external field.

??? WHY SUPERPARAMAGNETIC PARTICLES ???

Size of the superparamagnetic particle:

Magnetic active core = 2-3 nm

Coating (polymer, proteins, functional rest groups R) ~ 10 nm

Size of cell = 10 – 100 μm

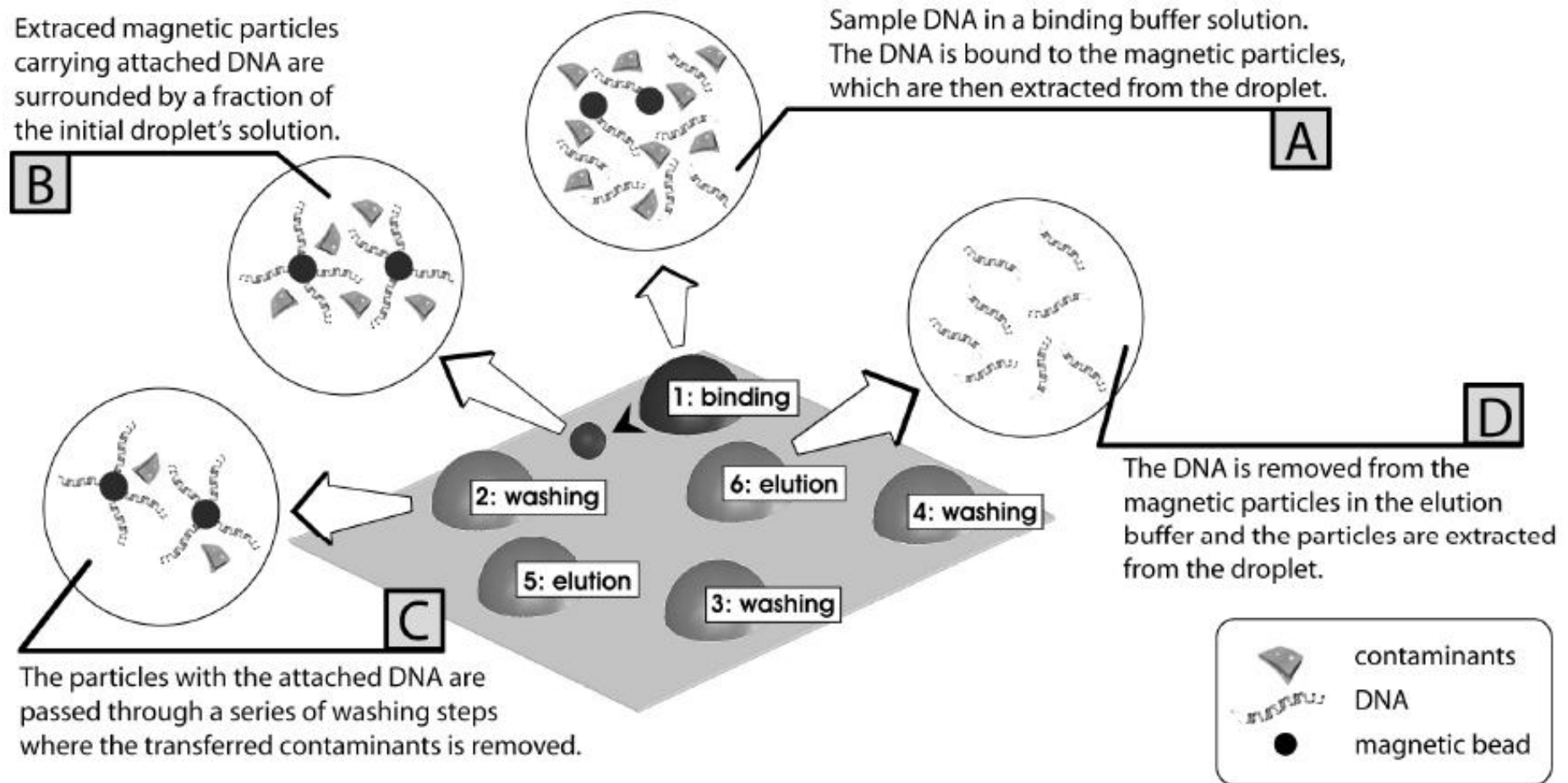
virus = 20 – 450 nm

protein = 5 – 50 nm

gene = $2^* (10 - 100) \text{ nm}^2$

Design of the particle:

- Attachment of R -> Particles entre the cells
Particles can be recognized by the organism
Drugs can be attached to the particle
R influences the toxicity for the organism



Schematic principle of the on-chip DNA purification protocol. The sample in the binding buffer solution is injected onto the chip and mixed with a droplet of magnetic particles. These are extracted and wash in three stages, before the DNA is again eluted in the steps 5 and 6