Дубненская международная школа современной теоретической физики

НА БОЛЬШОМ АДРОННОМ КОЛЛАЙДЕРЕ

Х Зимняя школа по теоретической физике

The Standard Model of Fundamental Interactions

ONZNK

Dmitry Kazakov (JINR)



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ЛТФ ОИЯИ, Дубна, Россия





Quarks – "the building blocks of the Universe"





The number of quarks increased with discoveries of new particles and have reached 6



For unknown reasons Nature created 3 copies (generations) of quarks and leptons





Now we have a beautiful pattern of three pairs of quarks and three pairs of leptons. They are shown here with their year of discovery.

Matter and Antimatter

The first generation is what we are made of



Antimatter was created together with matter during the "Big bang"

Antiparticles are created at accelerators in ensemble with particles but the visible Universe does not contain antimatter

Quark's Colour

Baryons are "made" of quarks



 $\Delta^{-}(d \uparrow d \uparrow d \uparrow)$ $\Omega^{-}(s \uparrow s \uparrow s \uparrow) ?$ $\Delta^{++}(u \uparrow u \uparrow u \uparrow)$

To avoid Pauli principle veto one can antisymmetrize the wave function introducing a new quantum number - "colour", so that

$$\Delta^{-} = \varepsilon^{ijk} (d_i \uparrow d_j \uparrow d_k \uparrow)$$

The Number of Colours



The x-section of electron-positron annihilation into hadrons is proportional to the number of quark colours. The fit to experimental data at various colliders at different energies gives

 $N_c = 3.06 \pm 0.10$

The Number of Generations



 $N_g = 2.982 \pm 0.013$

> Z-line shape obtained at LEP depends on the number of flavours and gives the number of (light) neutrinos or (generations) of the Standard Model

Quantum Numbers of Matter



The group structure of the SM



 $\sum_{a=1}^{N_A} \left(T^a T^{\dagger a} \right)_{ij} = \delta_{ij} C_F \quad , \quad \sum_{i,j=1}^{N_F} T^a_{ij} T^{\dagger b}_{ji} = \delta^{ab} T_F \quad , \quad \sum_{a,b=1}^{N_A} f^{abc} f^{*abd} = \delta^{cd} C_A$ a,b=1**Casimir Operators** $C_A = N_C$, $C_F = \frac{N_C^2 - 1}{2N_C}$, $T_F = 1/2$ For SU(N) Γ_Γ/C_Γ 1.4 ALEPH 68% CL contour 95% CL contour 1.2 QCD = SU(3)SO(3),E8 ✿ massless gluino 1 0.8 SO(4) SU(2), SP(2) 0.6 G2 0.4 F6 0.2 0 OPAL 68% CL DELPHI prelim 68% Cl -0.21.25 1.5 1.75 2 2.25 2.5 2.75 3 3.25 3.5 C_A/C_F

QCD analysis definitely singles out the SU(3) group as the symmetry group of strong interactions

Electro-weak sector of the SM SU(2) x U(1) versus O(3) 3 gauge bosons 1 gauge boson 3 gauge bosons After spontaneous symmetry breaking one has

3 massive gauge bosons $(W^{+}\ ,\ W^{-}\ ,\ Z^{0})\ \ and\ 1\ massless\ (\gamma)$



2 massive gauge bosons (W+ , W-) and 1 massless ($\gamma)$



- Discovery of neutral currents was a crucial test of the gauge model of weak interactions at CERN in 1973
- The heavy photon gives the neutral current without flavour violation

Gauge Invariance

 $\psi_i(x) \to \widehat{U}_{ij}(x) \psi_j = \exp[i\alpha^a(x)T_{ij}^a] \psi_j \qquad a = 1, 2, ..., N$ Gauge transformation $\overline{\psi}_{i}(x) \rightarrow \overline{\psi}_{i} \widehat{U}_{ji}^{+}(x)$ matrix parameter matrix $\hat{U}^{\dagger}\hat{U}=1$ $i\overline{\psi}(x)\gamma^{\mu}\partial_{\mu}\psi(x) \rightarrow i\overline{\psi}(x)\widehat{U}^{\dagger}(x)\gamma^{\mu}\partial_{\mu}\left(\widehat{U}(x)\psi(x)\right)$ Fermion Kinetic term $=i\overline{\psi}(x)\gamma^{\mu}\partial_{\mu}\psi(x)+\overline{\psi}(x)\gamma^{\mu}\widehat{U}^{\dagger}(x)\partial_{\mu}\widehat{U}(x)\psi(x)$ $\partial_{\mu} \rightarrow D_{\mu} = \partial_{\mu}I + gA_{\mu}^{a}T^{a} = \partial_{\mu}\hat{I} + g\hat{A}_{\mu} \quad \longleftarrow \quad \text{Gauge field}$ Covariant derivative $\widehat{A}_{\mu}(x) \to \widehat{U}(x)\widehat{A}_{\mu}(x)\widehat{U}^{\dagger}(x) - \frac{1}{g}\partial_{\mu}\widehat{U}(x)\widehat{U}^{\dagger}(x) \longrightarrow D_{\mu}\psi(x) \to \widehat{U}(x)D_{\mu}\psi(x)$ Gauge invariant kinetic term $i\psi(x)\gamma^{\mu}D_{\mu}\psi(x)$ $[D_{\mu}, D_{\nu}] = g\widehat{G}_{\mu\nu} = g\left(\partial_{\mu}\widehat{A}_{\nu} - \partial_{\nu}\widehat{A}_{\mu} + g[\widehat{A}_{\mu}, \widehat{A}_{\nu}]\right)\widehat{G}_{\mu\nu}(x) \rightarrow \widehat{U}(x)\widehat{G}_{\mu\nu}(x)\widehat{U}^{\dagger}(x)$ Gauge field kinetic term $-\frac{1}{4}Tr \ \widehat{G}_{\mu\nu} \widehat{G}^{\mu\nu}$ Field strength tensor 12

Lagrangian of the SM $SU_{c}(3) \otimes SU_{I}(2) \otimes U_{v}(1)$ $L = L_{gauge} + L_{Yukawa} + L_{Higgs}$ $L_{gauge} = -\frac{1}{4} G^{a}_{\mu\nu} G^{a}_{\mu\nu} - \frac{1}{4} W^{i}_{\mu\nu} W^{i}_{\mu\nu} - \frac{1}{4} B_{\mu\nu} B_{\mu\nu}$ $+i\overline{L}_{\alpha}\gamma^{\mu}D_{\mu}L_{\alpha}+i\overline{Q}_{\alpha}\gamma^{\mu}D_{\mu}Q_{\alpha}+i\overline{E}_{\alpha}\gamma^{\mu}D_{\mu}E_{\alpha}$ $+i\overline{U}_{\alpha}\gamma^{\mu}D_{\mu}U_{\alpha}+i\overline{D}_{\alpha}\gamma^{\mu}D_{\mu}D_{\alpha}+(D_{\mu}H)^{\dagger}(D_{\mu}H)$ $L_{Yukawa} = y_{\alpha\beta}^{L} L_{\alpha} E_{\beta} H + y_{\alpha\beta}^{D} Q_{\alpha} D_{\beta} H + y_{\alpha\beta}^{U} Q_{\alpha} U_{\beta} H$ $L_{Higgs} = -V = m^2 H^{\dagger} H - \frac{\lambda}{2} (H^{\dagger} H)^2 \qquad \qquad \widetilde{H} = i\tau_2 H^{\dagger}$ $\alpha,\beta=1,2,3$ - generation index

Fermion Masses in the SM

Direct mass terms are forbidden due to SU(2)_L invariance !



Spontaneous Symmetry Breaking $SU_{c}(3) \otimes SU_{L}(2) \otimes U_{Y}(1) \rightarrow SU_{c}(3) \otimes U_{FM}(1)$ Introduce a scalar field with quantum numbers: (1,2,1) $H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$ With potential $V = -m^2 H^{\dagger} H + \frac{\lambda}{2} (H^{\dagger} H)^2$ Unstable maximum At the minimum scalar v.e.v. Stable minimum lm φ $H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix} = \begin{pmatrix} H^+ \\ V + \frac{S+iP}{\sqrt{2}} \end{pmatrix} = \exp(i\frac{\vec{\xi}\vec{\sigma}}{2}) \begin{pmatrix} 0 \\ V + \frac{S}{\sqrt{2}} \end{pmatrix}$ pseudoscalar Gauge transformation liggs boson $H \to H' = \exp(i\frac{\vec{\alpha}\vec{\sigma}}{2})H \xrightarrow{(\vec{\alpha}=-\vec{\xi})} H' = \begin{pmatrix} 0 \\ v + \frac{h}{\sqrt{2}} \end{pmatrix}$ 15

The Higgs Mechanism Q: What happens with missing d.o.f. (massless goldstone bosons P,H⁺ or $\vec{\xi}$)? A: They become longitudinal d.o.f. of the gauge bosons W_{μ}^{i} , i=1,2,3 $\widehat{W}_{\mu} \rightarrow e^{i\alpha^{a}\sigma^{a}} \widehat{W}_{\mu} e^{-i\alpha^{a}\sigma^{a}} - \frac{1}{g} \partial_{\mu} \left(e^{i\alpha^{a}\sigma^{a}} \right) e^{-i\alpha^{a}\sigma^{a}}$ Longitudinal components Gauge transformation $\alpha^a = -\xi^a$ Higgs field kinetic term $\left|D_{\mu}H\right|^{2} = \left|\partial_{\mu}H - \frac{g}{2}\widehat{W}_{\mu}H - \frac{g'}{2}\widehat{B}_{\mu}H\right|^{2} \leftarrow H = \begin{pmatrix} 0 \\ \mathbf{v} \end{pmatrix}$ $\rightarrow \frac{1}{4} (0 v) \begin{pmatrix} gW_{\mu}^{3} + g'B_{\mu} & \sqrt{2}gW_{\mu}^{-} \\ \sqrt{2}gW_{\mu}^{+} & -gW_{\mu}^{3} + g'B_{\mu} \end{pmatrix} \begin{pmatrix} gW_{\mu}^{3} + g'B_{\mu} & \sqrt{2}gW_{\mu}^{-} \\ \sqrt{2}gW_{\mu}^{+} & -gW_{\mu}^{3} + g'B_{\mu} \end{pmatrix} \begin{pmatrix} 0 \\ \sqrt{2}gW_{\mu}^{+} & -gW_{\mu}^{3} + g'B_{\mu} \end{pmatrix} \begin{pmatrix} 0 \\ v \end{pmatrix}$ $\Rightarrow \frac{g^2}{2} v^2 W_{\mu}^+ W_{\mu}^- + \frac{1}{4} v^2 (-g W_{\mu}^3 + g' B_{\mu})^2 \qquad W_{\mu}^{\pm} = \frac{W_{\mu}^1 \mp W_{\mu}^2}{\sqrt{2}}$ $M_W^2 = \frac{1}{2}g^2 v^2 \qquad \tan \theta_W = g' / g$ $M_Z^2 = \frac{1}{2}(g^2 + g'^2) v^2 \qquad M_\gamma = 0$ $Z_{\mu} = -\sin\theta_{W}B_{\mu} + \cos\theta_{W}W_{\mu}^{3}$ $\gamma_{\mu} = \cos \theta_{W} B_{\mu} + \sin \theta_{W} W_{\mu}^{3}$



Quark/Lepton Mixing

• The mass matrix is non-diagonal in generation space

It can be diagonalized by field rotation Q -> Q'= V Q

$$\overline{U}M_{U}U \rightarrow \overline{U}'V_{U}^{+}M_{U}V_{U}U' = \overline{U}'M_{U}^{Diag}U'$$
$$\overline{D}M_{D}D \rightarrow \overline{D}'V_{D}^{+}M_{D}V_{D}D' = \overline{D}'M_{D}^{Diag}D'$$

• Neutral Current:

$$\overline{U}Z_{\mu}U - > \overline{U}'V_{U}^{+}Z_{\mu}V_{U}U' = \overline{U}'Z_{\mu}U' \ V_{U}^{+}V_{U} = \overline{U}'Z_{\mu}U'$$

Charged Current

$$\overline{U}W_{\mu}D - > \overline{U}'V_{U}^{+}W_{\mu}V_{D}D = \overline{U}'W_{\mu}V_{U}^{+}V_{D}D'$$

 $K = V_{U}^{+}V_{D}$

Cabibbo-Kobayashi-Maskawa mixing matrix

The (only) source of flavour mixing in the SM

Unitarity: K⁺K=1

CKM Matrix and Unitarity Triangle

$$K = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

Two important properties

- 1. CP-violation due to a complex phase δ !
- 2. Unitarity triangle

$$V_{ud}V_{ub}^{*} + V_{cd}V_{cb}^{*} + V_{td}V_{tb}^{*} = 0$$

$$\Rightarrow V_{ub}^{*} + V_{td} = s_{12}V_{cb}^{*}$$



The Unitarity Triangle: all constraints



A consistent picture across a huge array of measurements

²⁰

Comparison with Experiment

Global Fit to Data

	Measurement	Pull	Pull -3 -2 -1 0 1 2 3
m _z [GeV]	91.1875 ± 0.0021	.05	
Г _Z [GeV]	2.4952 ± 0.0023	42	-
σ ⁰ hadr [nb]	41.540 ± 0.037	1.62	
R _i	20.767 ± 0.025	1.07	_
A ^{0,I}	0.01714 ± 0.00095	.75	-
A _e	0.1498 ± 0.0048	.38	-
A _r	0.1439 ± 0.0042	97	-
sin²θ ^{lept}	0.2321 ± 0.0010	.70	- 1
m _w [GeV]	80.427 ± 0.046	.55	-
R _b	0.21653 ± 0.00069	1.09	_
R _c	0.1709 ± 0.0034	40	-
A ^{0,b}	0.0990 ± 0.0020	-2.38	
A ^{0,c}	0.0689 ± 0.0035	-1.51	_
A _b	0.922 ± 0.023	55	-
A _c	0.631 ± 0.026	-1.43	
sin²θ ^{lept}	0.23098 ± 0.00026	-1.61	_
sin²θ _w	0.2255 ± 0.0021	1.20	
m _w [GeV]	80.452 ± 0.062	.81	_
m _t [GeV]	174.3 ± 5.1	01	
$\Delta \alpha_{had}^{(5)}(m_Z)$	0.02804 ± 0.00065	29	•
			-3 -2 -1 0 1 2 3

Remarkable agreement of ALL the data with the SM predictions - precision tests of radiative corrections and the SM Higgs Mass Constraint



Though the values of $\sin \vartheta w$ extracted from different experiments are in good agreement, two most precise measurements from hadron and lepton asymmetries disagree by 3σ 21

The SM and Beyond

breaking

or of generations is arbitrary

The problems of the SM:

- Inconsistency at high energies due to Landau poles
- Large number of free parameters

- Inc origin of the n
 Flavour mixing and Where is the Dark matter?
 Formal unification • Formal unification of Long and electroweak interactions The way beyond the SM:

- The SAME fields with NEW interactions and NEW fields
 - NEW fields with NEW interactions

Compositeness, Technicolour, preons

GUT, SUSY, String, ED



We like elegant solutions



"Whatever happened to *elegant* solutions?"