

QCD studies and Higgs searches at the LHC

part three

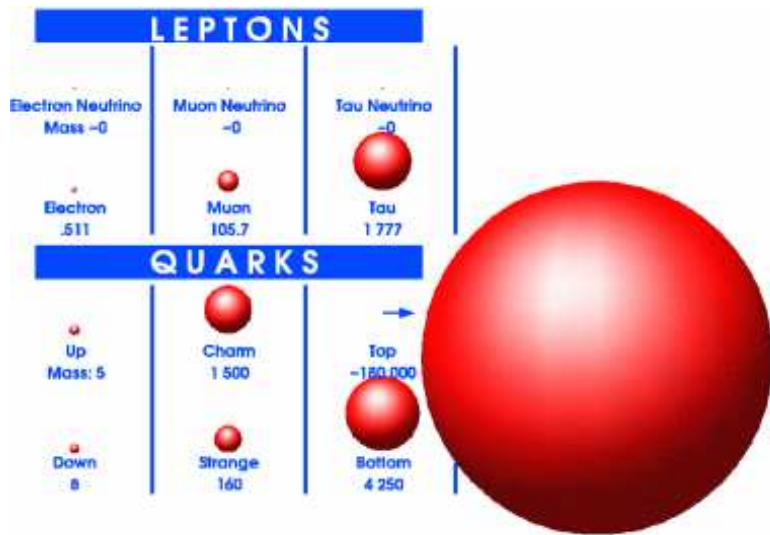
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DESY, Zeuthen

Plan

- Some new results on the heaviest elementary particle



Abundant production of top-quarks

TOP QUARK *t*

Discovered at Fermilab in 1995, the **TOP QUARK** is as short-lived as it is massive. Weighing in at a hefty 175 GeV, its lifetime, a mere 10^{-25} second, is the briefest of the six quarks. Top Quarks are an enigmatic particle whose personal life is sought after by thousands of physicists.

Acrylic felt with gravel fill for maximum mass.

\$9.75 PLUS SHIPPING

LIGHT ●●●●●●●●●●●●●●●● HEAVY

GLUON PHOTON NEUTRINO TACHYON ELECTRON UP QUARK DOWN QUARK TAU NEUTRINO MUON UP QUARK
NEUTRON DOWN QUARK TAU GLUON **TOP QUARK** NEUTRINO TACHYON ELECTRON UP QUARK DOWN
NEUTRINO MUON UP QUARK PROTON NEUTRON DOWN QUARK TAU GLUON PHOTON NEUTRINO TACHY
UP QUARK DOWN QUARK TAU NEUTRINO MUON UP QUARK PROTON NEUTRON DOWN QUARK TAU GLU
The **PARTICLE ZOO** DOWN QUARK TAU NEUTRINO MUON UP QUARK PROTON N
DOWN QUARK TAU NEUTRINO MUON UP QUARK PROTON NEUTRON DOWN QUARK TAU NEU

- Orders for top-quarks from www.particlezoo.com

Top-quark decays

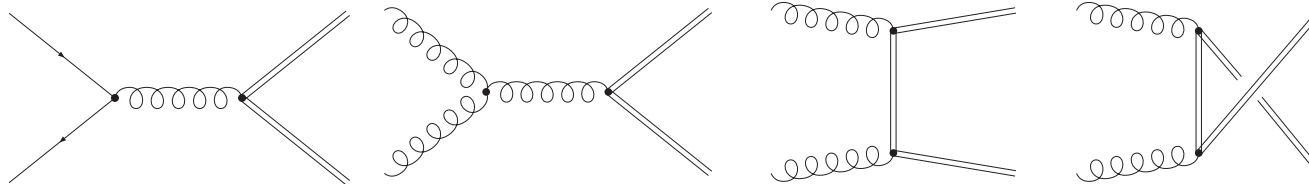


Top quark production

- Leading order Feynman diagrams

$$q + \bar{q} \longrightarrow Q + \bar{Q}$$

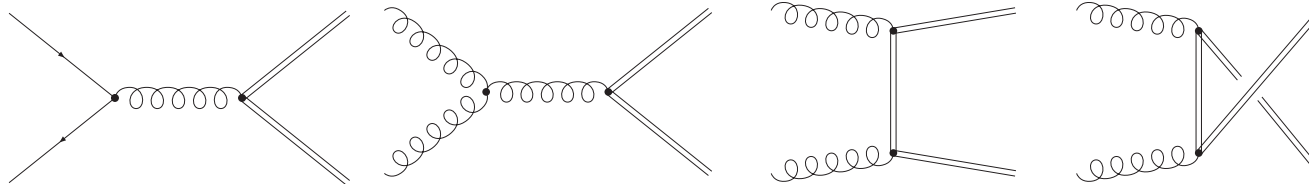
$$g + g \longrightarrow Q + \bar{Q}$$



- NLO in QCD Nason, Dawson, Ellis '88; Beenakker, Smith, van Neerven '89; Mangano, Nason, Ridolfi '92; Bernreuther, Brandenburg, Si, Uwer '04; Mitov, Czakon '08; ...
 - accurate to $\mathcal{O}(15\%)$ at LHC

Top quark production

- Leading order Feynman diagrams



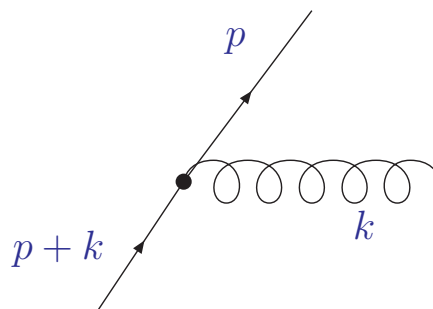
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 - accurate to $\mathcal{O}(15\%)$ at LHC
- First steps towards higher orders in QCD: explore limits
- Study of massive QCD amplitudes in high-energy limit $s \gg m^2$
 - exploit high-energy factorization in BFKL formalism
- Partonic threshold $s \simeq 4m^2$
 - Sudakov logarithms $\ln \beta$ (velocity of heavy quark $\beta = \sqrt{1 - 4m^2/s}$)

Sudakov logarithms

- Recall perturbative QCD:
 - calculation of observables as series in $\alpha_s \ll 1$
 - but: large logarithmic corrections, $\ln(\dots) \gg 1$
double logarithms (Sudakov)
- Soft/Collinear regions of phase space
 - double logarithms from singular regions in Feynman diagrams
 - propagator vanishes for: $E_g = 0$, soft $\theta_{qg} = 0$ collinear



$$\alpha_s \int d^4k \frac{1}{(p+k)^2} = \frac{1}{2p \cdot k} = \frac{1}{2E_q E_g (1 - \cos \theta_{qg})}$$

$$\longrightarrow \alpha_s \int dE_g d\sin \theta_{qg} \frac{1}{2E_q E_g (1 - \cos \theta_{qg})}$$

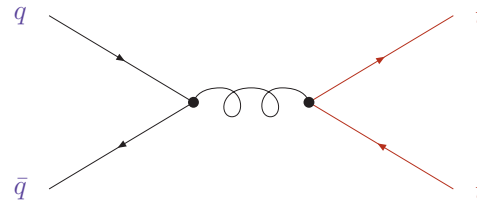
$$\longrightarrow \alpha_s \ln^2(\dots)$$

- Improved perturbation theory: resum logarithms to all orders
 - long history of resummation Kidonakis, Sterman '97; Bonciani, Catani, Mangano, Nason '98; Kidonakis, Laenen, S.M., Vogt '01; ...

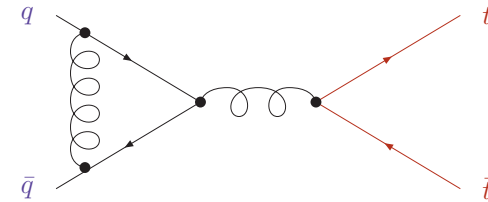
Sudakov logarithms in cross sections

- Intuitive aspects of higher order corrections

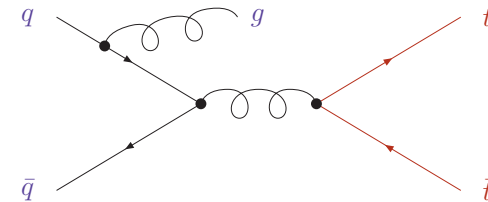
- lowest order, elastic



- first order correction
virtual < 0 (elastic)



- first order correction
Brems > 0 (inelastic)



- at threshold for $t\bar{t}$ -creation

- strong Sudakov-suppression inelastic tendency

$$\sigma \sim \exp\left[-\alpha_s \ln^2\left(1 - 4m_t^2/s\right)\right]$$

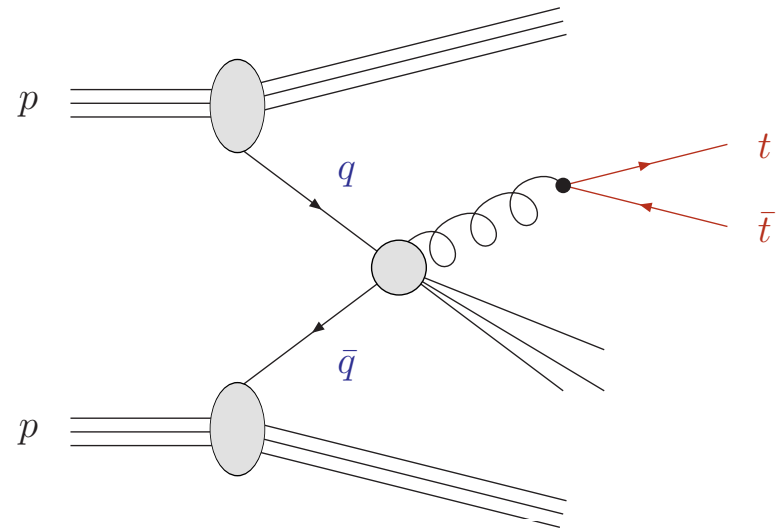
- universal factor for parton splittings (leading log accuracy)
modelling of MC parton showers

- Hadronic reaction $p\bar{p}$:

- recall master equation

$$\sigma_{pp \rightarrow t\bar{t}} = \sum_{ij} f_i \otimes f_j \otimes \hat{\sigma}_{ij \rightarrow t\bar{t}}$$

- initial partons: also Sudakov-supressed



- Parton cross section $\hat{\sigma}_{ij \rightarrow t\bar{t}}$

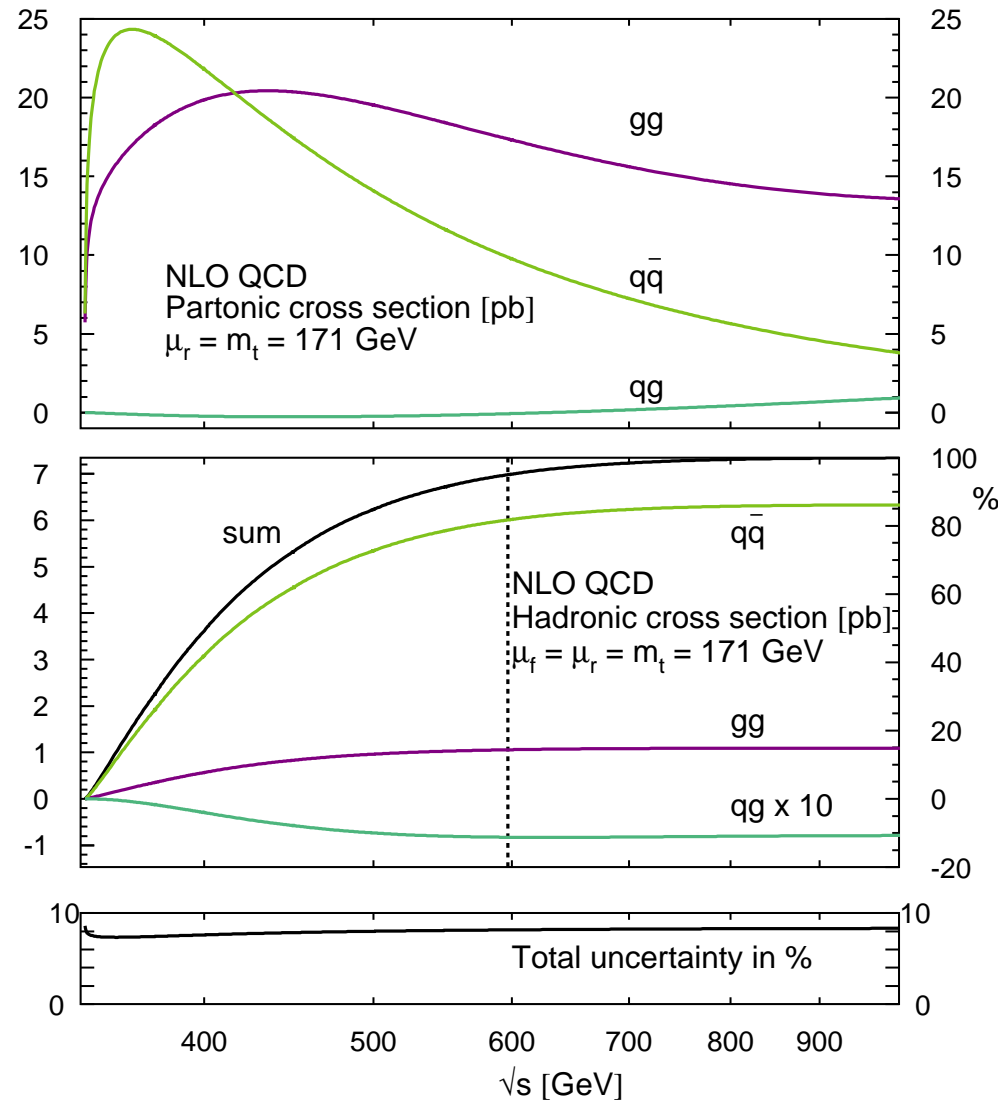
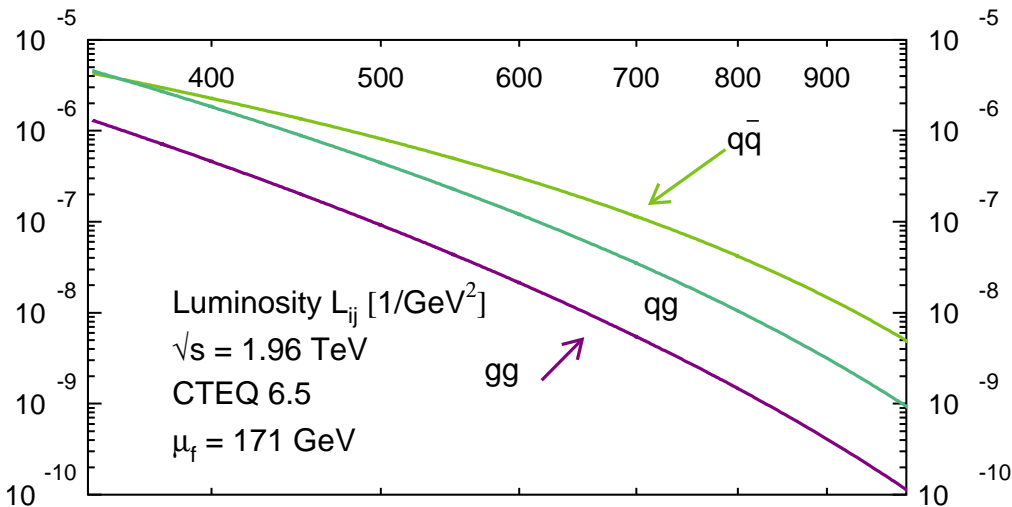
- Sudakov-enhancement after mass factorization

$$\hat{\sigma}_{ij \rightarrow t\bar{t}} = \frac{\sigma_{pp \rightarrow t\bar{t}}}{f_i \otimes f_j} = \frac{e^{-\alpha_s \ln^2(\dots)}}{(e^{-\alpha_s \ln^2(\dots)})^2} = e^{+\alpha_s \ln^2(\dots)}$$

- large double logarithms

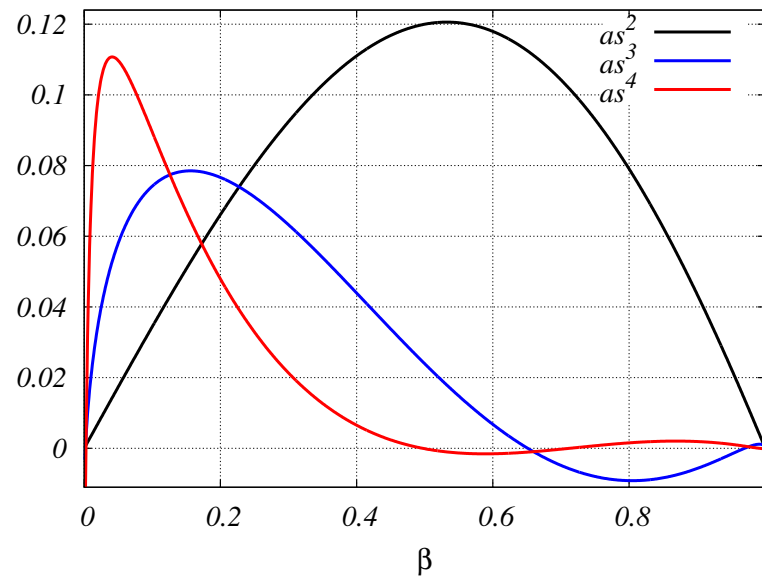
Total cross section at Tevatron

$$\sigma_{pp \rightarrow t\bar{t}} = \sum_{ij} f_i \otimes f_j \otimes \hat{\sigma}_{ij \rightarrow t\bar{t}}$$



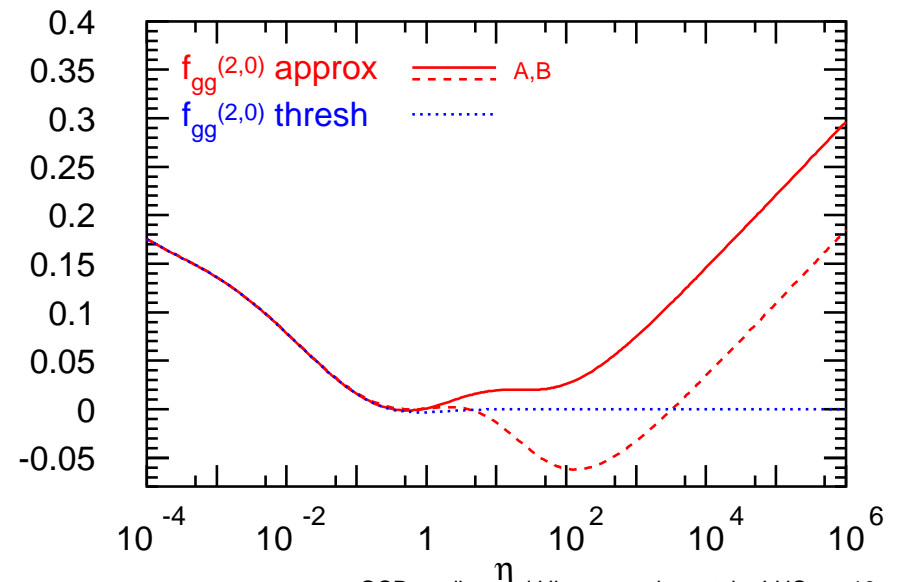
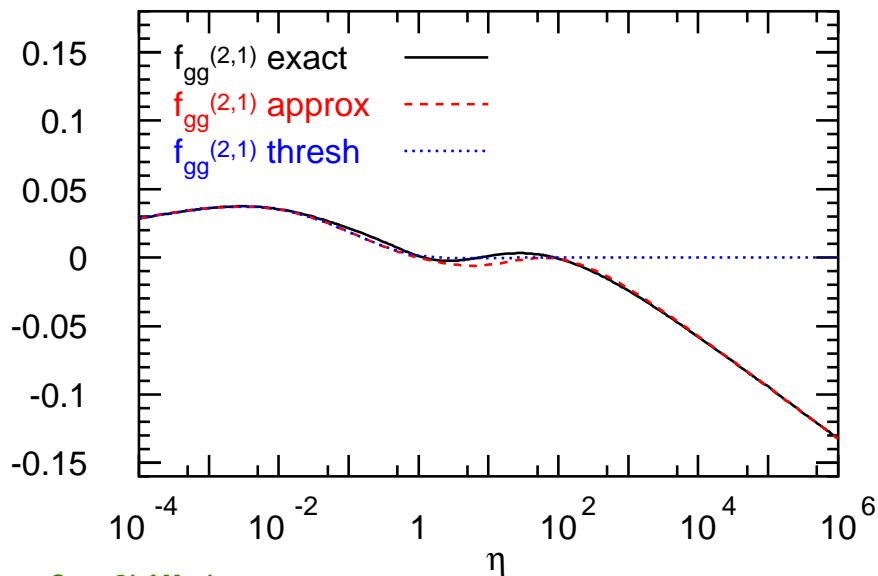
Top-pair hadro-production

- NNLO cross section for heavy-quark hadro-production
- Exact results for channel $q\bar{q} \rightarrow t\bar{t}$ Czakon, Mitov '12



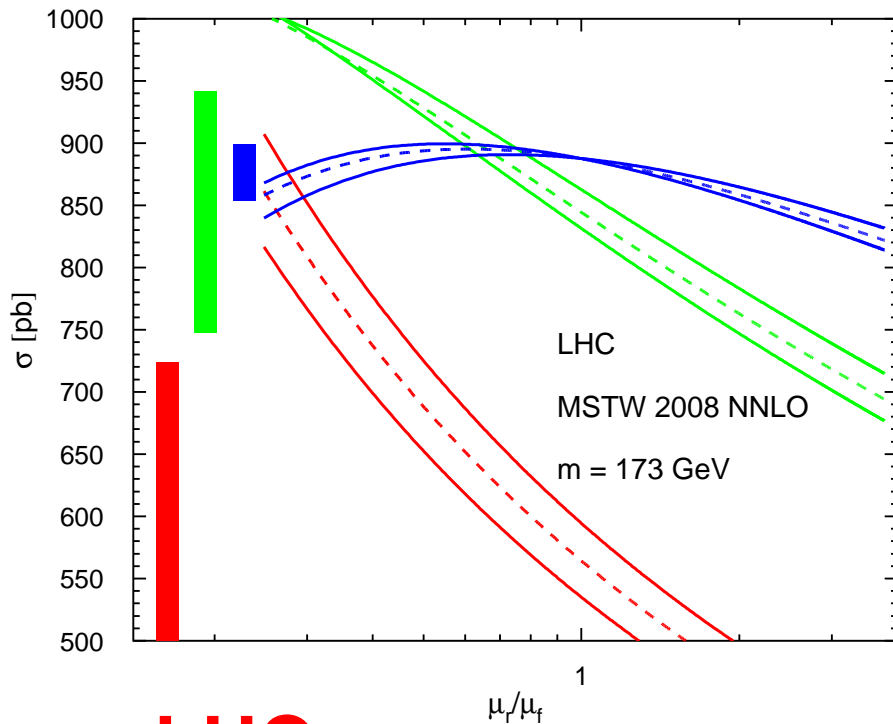
Top-pair hadro-production

- NNLO cross section for heavy-quark hadro-production
- Approximate results for channel $qg/gg \rightarrow t\bar{t}$
 - threshold at $s \simeq 4m_t^2$ with logarithms $\ln(\beta)$ in velocity of heavy quark $\beta = \sqrt{1 - 4m_t^2/s}$ at n^{th} -order
S.M, Uwer '08; Beneke, Czakon, Falgari, Mitov, Schwinn '09
 - high-energy limit for $\rho = 4m_t^2/s \rightarrow 1$
Catani, Ciafaloni, Hautmann '91; Ball, Ellis '01; S.M, Uwer, Vogt '12

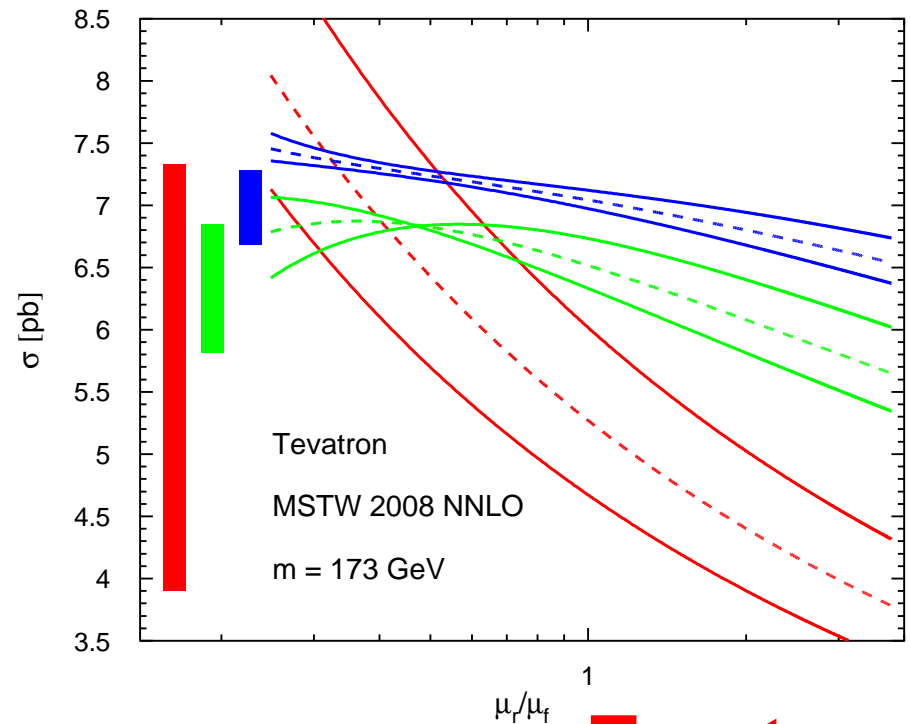


Scale dependence

- Theoretical uncertainty from variation of scales μ_R, μ_F
 - plot with PDF set MSTW 2008 (but largely independent on PDFs)
 - mass $m_t = 173 \text{ GeV}$
 - stable predictions in range $\mu_R, \mu_F \in [m_t/2, 2m_t]$
 - $-3\% \leq \Delta\sigma \leq +1\%$ at LHC
 - $-5\% \leq \Delta\sigma \leq +3\%$ at Tevatron



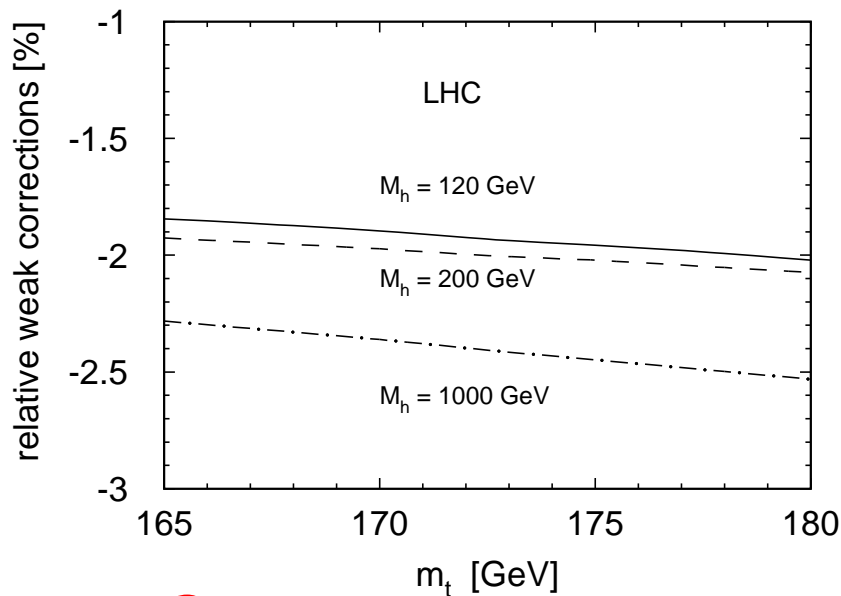
LHC



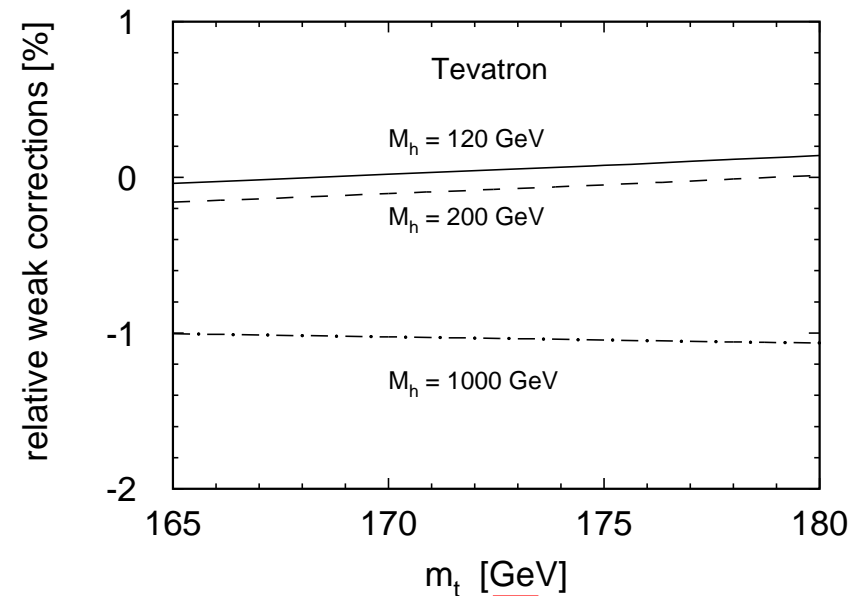
Tevatron

Electroweak corrections

- Electroweak corrections (ratio of σ_{EW}/σ_{LO})
Bernreuther, Fückler '05; Kühn, Uwer, Scharf '06
- Effect depends on Higgs mass
(choices $m_H = 120\text{GeV}$, $m_H = 200\text{GeV}$, $m_H = 1000\text{GeV}$)



LHC



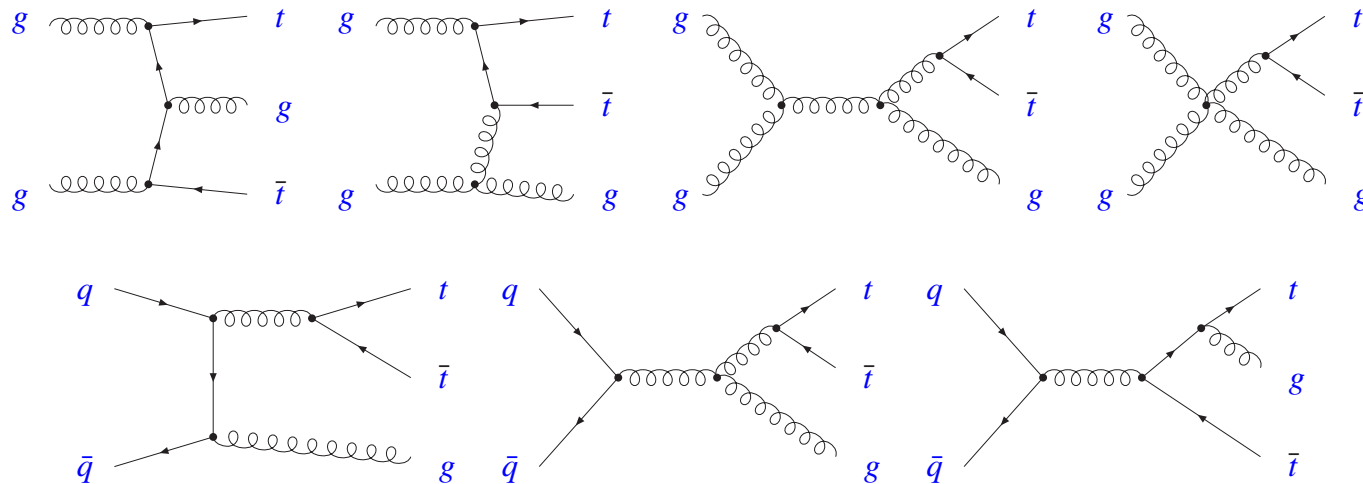
Tevatron

- Tevatron: vanishing contribution for light Higgs
- LHC: $\mathcal{O}(2\%)$ with respect to σ_{LO}
negative contribution to total cross section $\Delta\sigma_{EW} \simeq \mathcal{O}(10 - 15) \text{ pb}$

Top-quark pairs with one jet

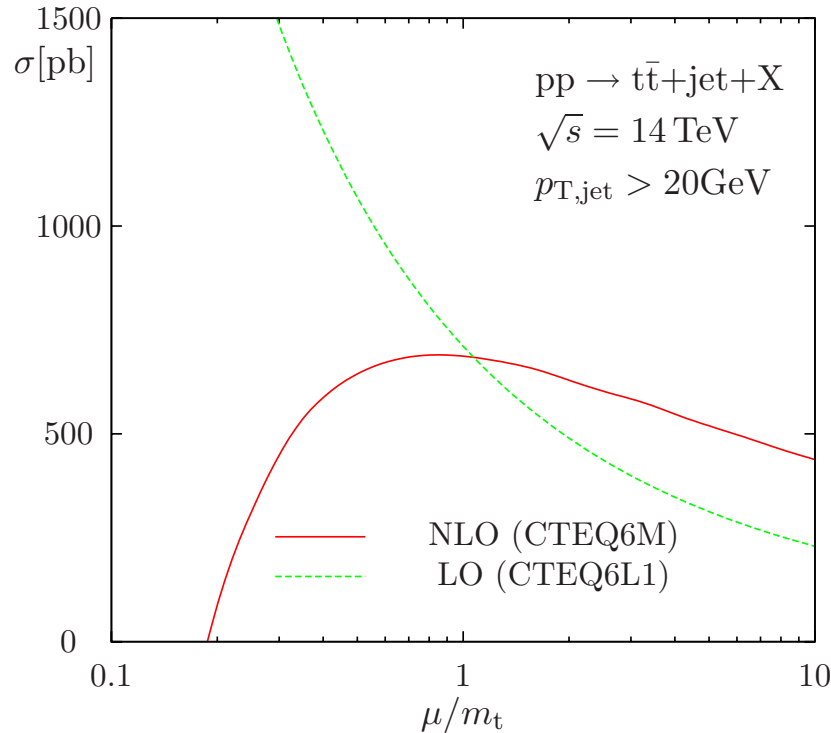
Production of $t\bar{t}$ +jet at fixed order

- LHC: large rates for production of $t\bar{t}$ -pairs with additional jets
- Scale dependence at LO large

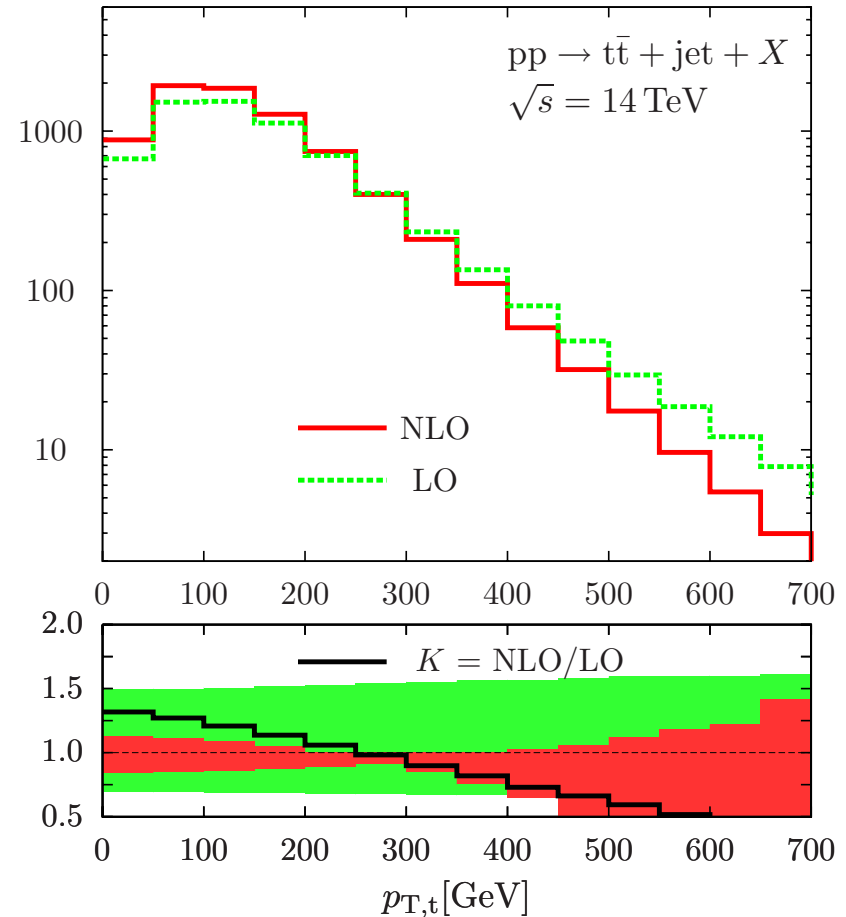


- Feynman diagrams (sample) for $t\bar{t}$ +jet production at LO

Production of $t\bar{t} + \text{jet}$ at NLO



$$\left(\frac{d\sigma}{dp_{T,t}} \right) \left[\frac{\text{fb}}{\text{GeV}} \right]$$



- NLO QCD corrections [Dittmaier, Uwer, Weinzierl '07-'08](#)
 - scale dependence greatly reduced at NLO
 - corrections for total rate at scale $\mu_r = \mu_f = m_t$ are almost zero
 - transverse-momentum distributions of top-quark $p_{T,t}$ along with K-factor and scale variation $m_t/2 \leq \mu \leq 2m_t$

Monte Carlo and parton showers at NLO

- Merging of fixed order NLO with parton shower Monte Carlo
Frixione, Webber '02, Nason '04
 - combining accuracy of exact hard matrix elements for large angle scattering at NLO with soft/collinear emission of parton shower
- POWHEG BOX as standard interface to parton shower programs
PYTHIA or HERWIG Alioli, Nason, Oleari, Re '10
- Production of $t\bar{t} + \text{jet}$ and parton showers
Kardos, Papadopoulos, Trocsanyi '11, Alioli, S.M., Uwer '11

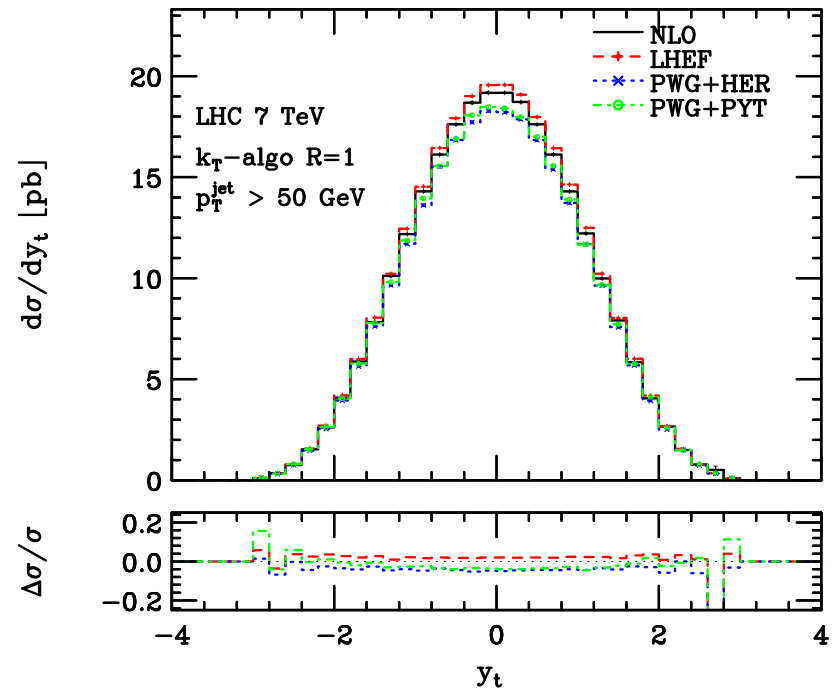
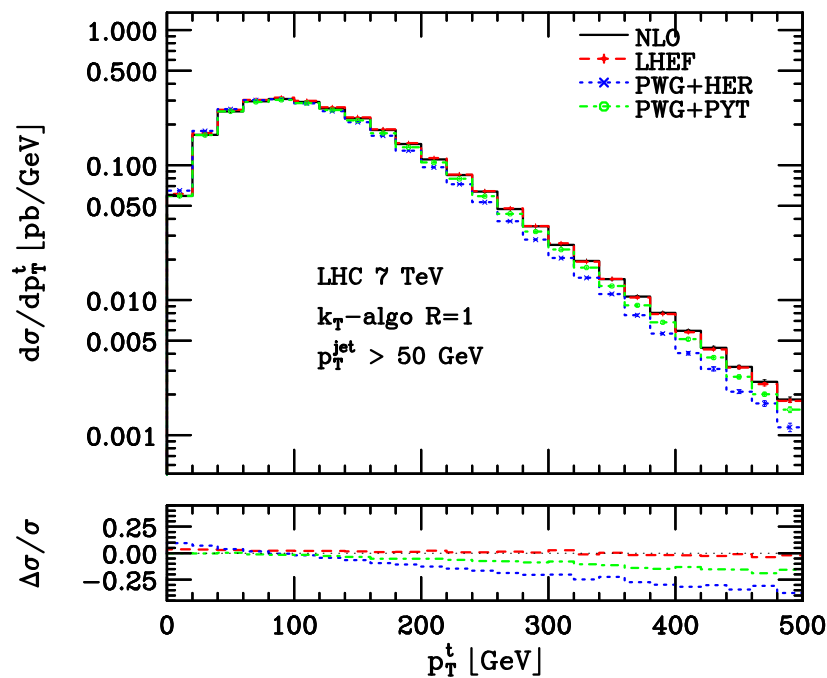
Implementation

- Event generation with cut on $p_t^{\text{gen}} \simeq 1 \text{ GeV}$
- Alternative option for soft and collinear divergences at Born level:
generation of weighted events with Born suppression factor
 $\bar{B}_{\text{supp}} = \bar{B} \times F(p_t)$ Alioli, Nason, Oleari, Re '10

$$F(p_t) = \left(\frac{p_t^2}{p_t^2 + (p_t^{\text{supp}})^2} \right)^n$$

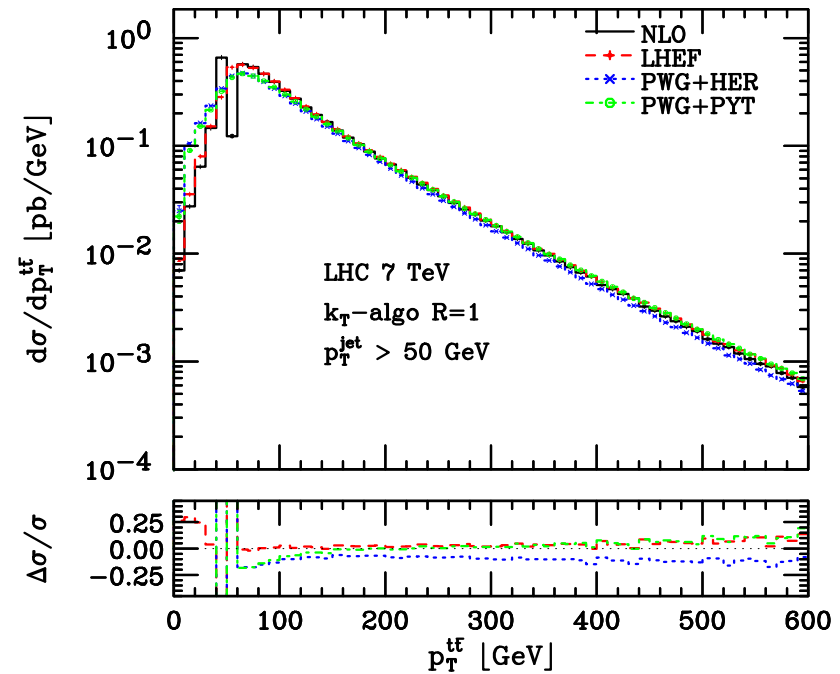
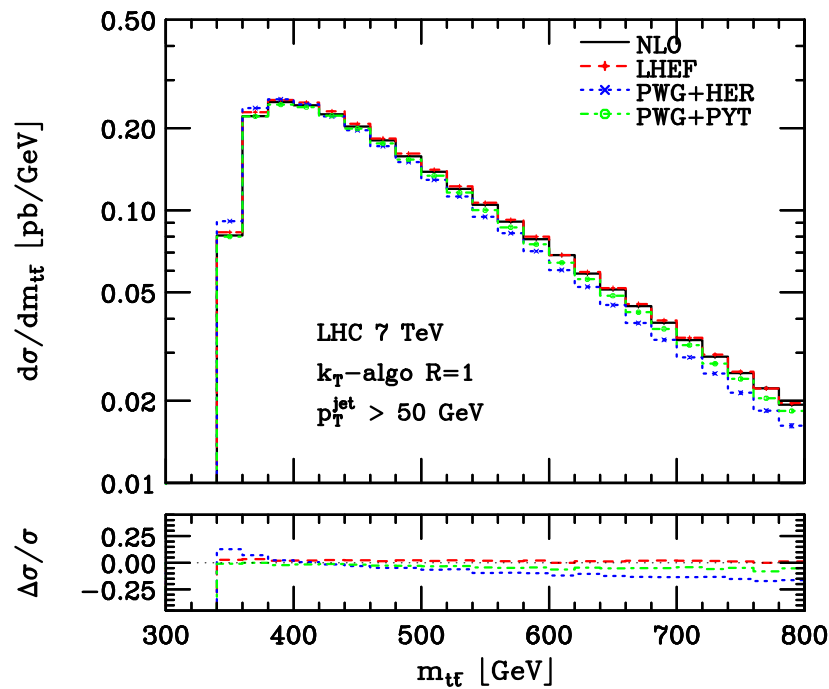
Production $t\bar{t}$ + jet and parton shower (I)

- Differential distributions in top-quark's transverse momentum p_T^t and rapidity y_t at LHC7
 - comparison of NLO, LHEF for POWHEG hardest emission without showering, and POWHEG with shower/hadronization with HERWIG or PYTHIA



Production $t\bar{t}$ + jet and parton shower (II)

- Differential distributions as function of $t\bar{t}$ -pair invariant mass $m_{t\bar{t}}$ and transverse momentum $p_T^{t\bar{t}}$ at LHC7



Heavy-quark masses

QCD Lagrangian

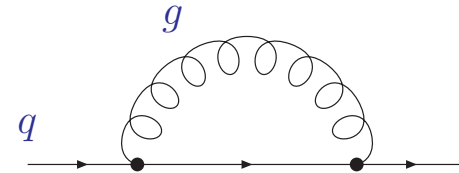
$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \sum_{\text{flavors}} \bar{q} (i\not{D} - m_q) q$$

- Covariant derivative $D_\mu = \partial_\mu + ig_s A_\mu$
- Formal parameters of the theory (no observables)
 - strong coupling $\alpha_s = g_s^2/(4\pi)$
 - quark masses m_q
- Quantum corrections (loop integrals) require UV renormalization; (scheme dependence):
 - $\alpha_s \rightarrow$ asymptotic freedom, running coupling (\overline{MS} scheme)
 - $m_q \rightarrow$ pole mass or running mass (\overline{MS} scheme)

Pole mass

- Based on (unphysical) concept of top-quark being a free parton

$$\not{p} - m_q - \Sigma(p, m_q) \Big|_{p^2 = m_q^2}$$



- heavy-quark self-energy $\Sigma(p, m_q)$ receives contributions from regions of all loop momenta – also from momenta of $\mathcal{O}(\Lambda_{QCD})$
- Definition of pole mass ambiguous up to corrections $\mathcal{O}(\Lambda_{QCD})$

Running quark masses

- \overline{MS} mass definition $m(\mu_R)$ realizes running mass (scale dependence)
- renormalization group equation (mass anomalous dimension γ)

$$\left(\mu_R^2 \frac{\partial}{\partial \mu_R^2} + \beta(\alpha_s) \frac{\partial}{\partial \alpha_s} \right) m(\mu_R) = \gamma(\alpha_s) m(\mu_R)$$

- short distance mass probes at scale of hard scattering

$$m_{\text{pole}} = m_{\text{short distance}} + \delta m$$

- conversion between pole mass and \overline{MS} mass definition in

$$\text{perturbation theory: } m = m(\mu_R) \left(1 + a_s(\mu_R) d^{(1)} + a_s(\mu_R)^2 d^{(2)} \right)$$

Scale dependence

- Renormalization group equation for scale dependence

- strong coupling α_s and mass m

$$\mu^2 \frac{d}{d\mu^2} \alpha_s(\mu) = \beta(\alpha_s) \qquad \mu^2 \frac{d}{d\mu^2} m(\mu) = \gamma(\alpha_s) m(\mu)$$

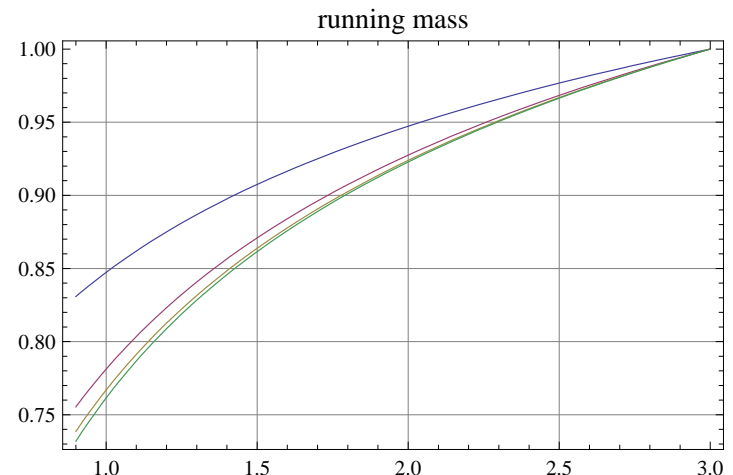
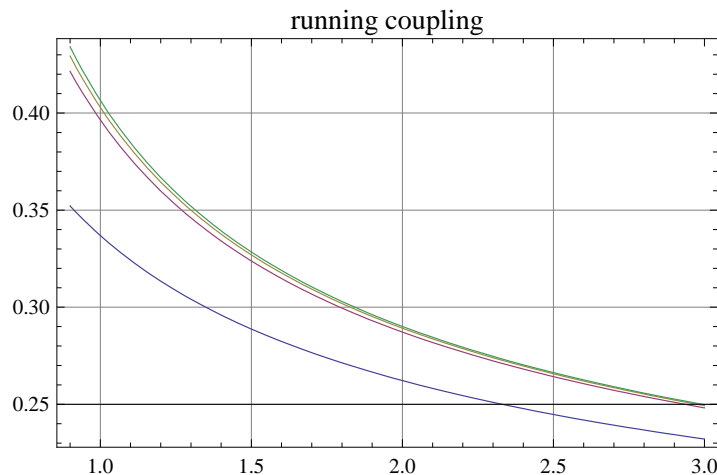
- Perturbative expansion known to four loops

- β -function van Ritbergen, Vermaseren, Larin '97 and mass anomalous dimension γ Chetyrkin '97; Larin, van Ritbergen, Vermaseren '97

- very good convergence of perturbative series even at low scales

- Plot at low scales $\mu = 1.0 \dots 3.0$ GeV

α_s (left) and mass ratio $m(3\text{GeV})/m(\mu)$ (right)



- Use of charm-quark mass $m_c(m_c)$ is well justified

Illustration for top-quark mass

ILC

- Pole mass measurements are strongly order-dependent

- e.g. threshold scan of cross section in e^+e^- collision
Beneke, Signer, Smirnov '99;
Hoang, Teubner '99;
Melnikov, Yelkhovsky '98;
Penin, Pivovarov '99;
Yakovlev '99
- LO (dotted), NLO (dashed), NNLO (solid)

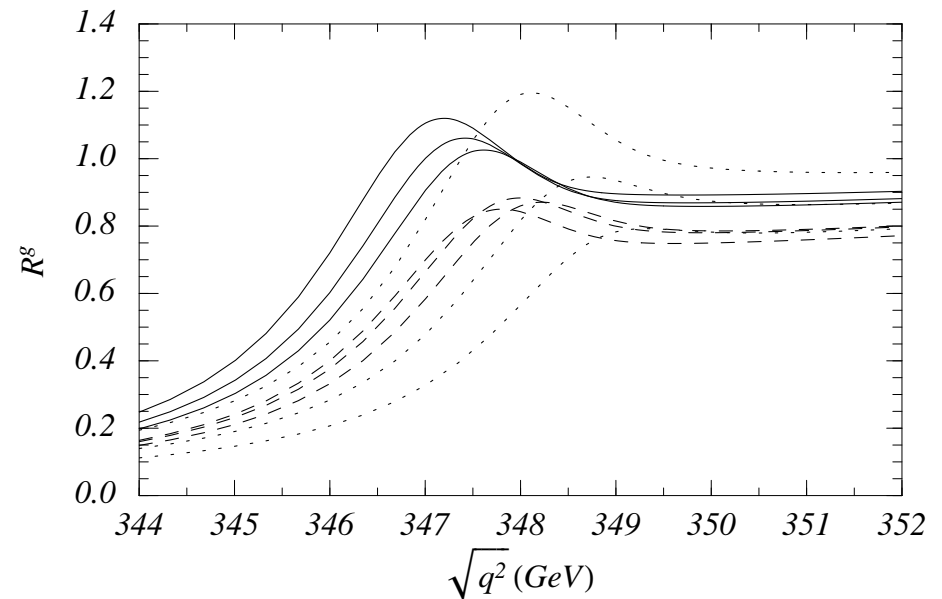
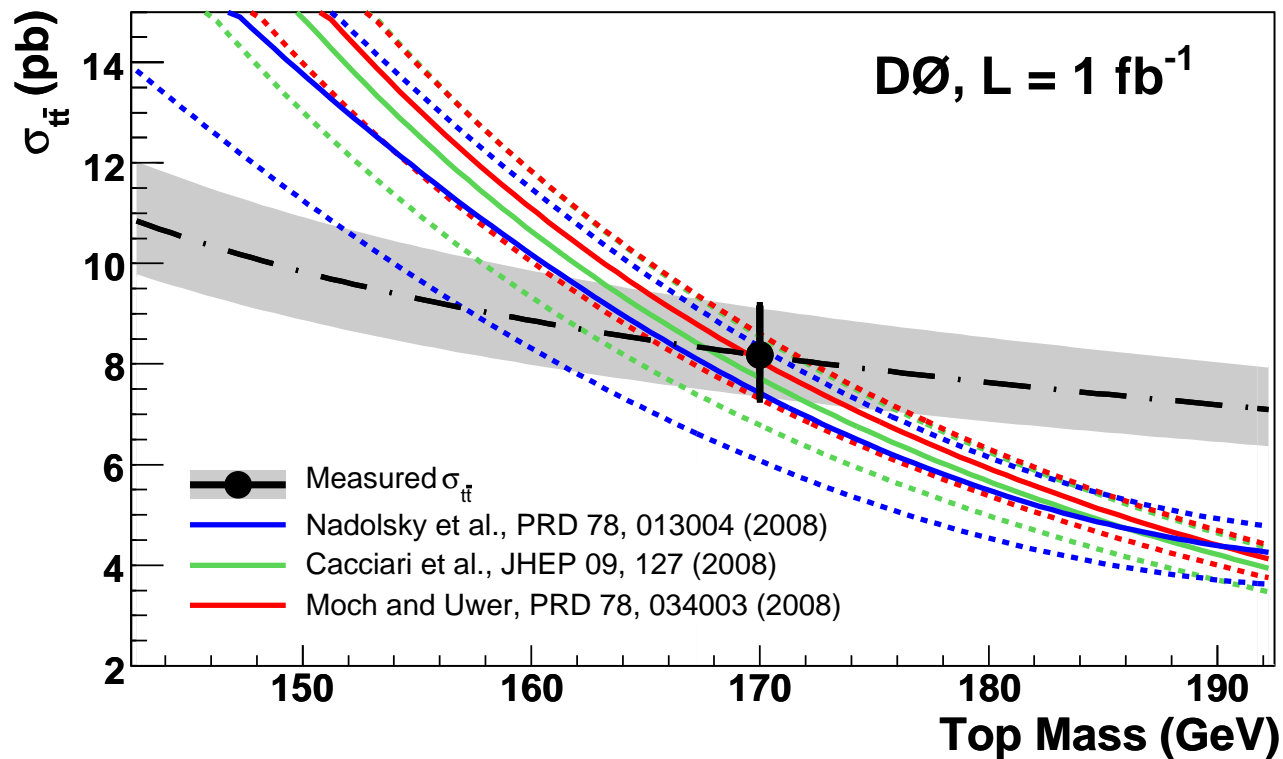


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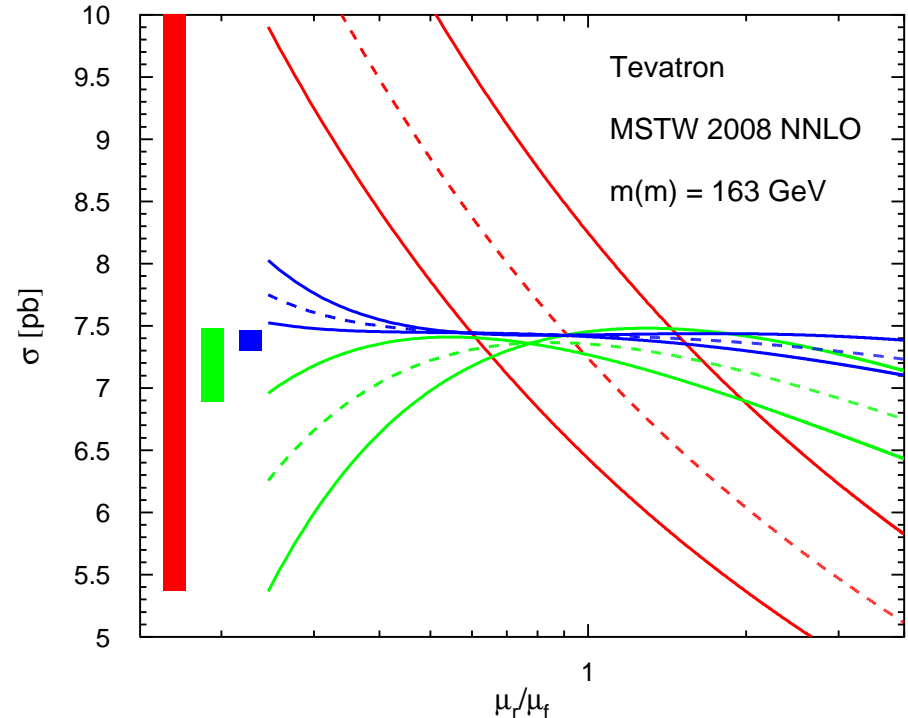
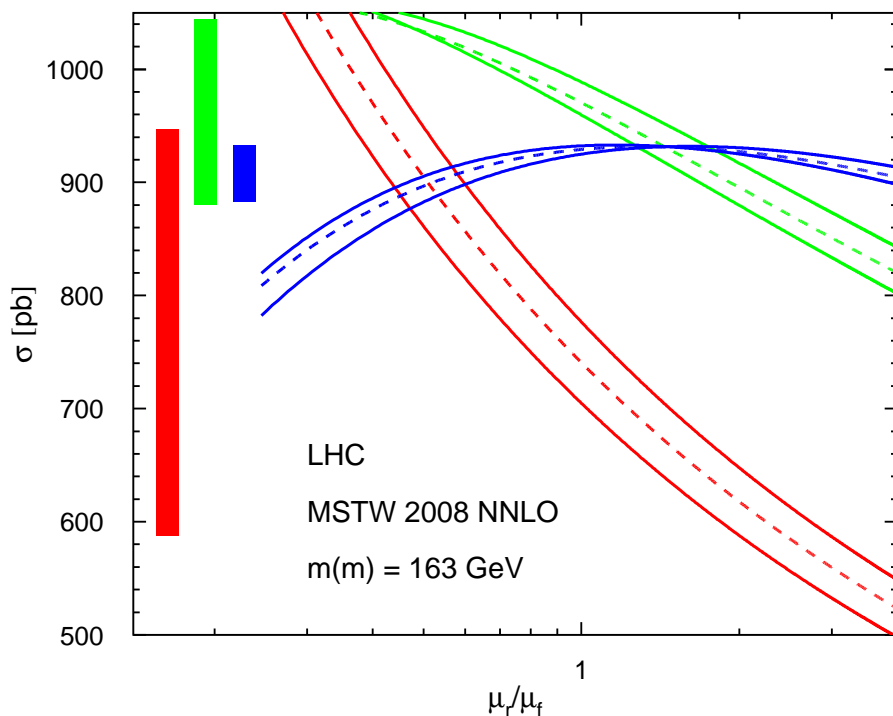
Tevatron

- Total cross section and different channels of Tevatron analyses (theory uncertainty band from scale variation)
- Determination of m_t from total cross section (slope $d\sigma/dm_t$)
 - e.g. DZero '09: NLO $m_t = 165.5^{+6.1}_{-5.9}$; NNLO $m_t = 169.1^{+5.9}_{-5.2}$; ...



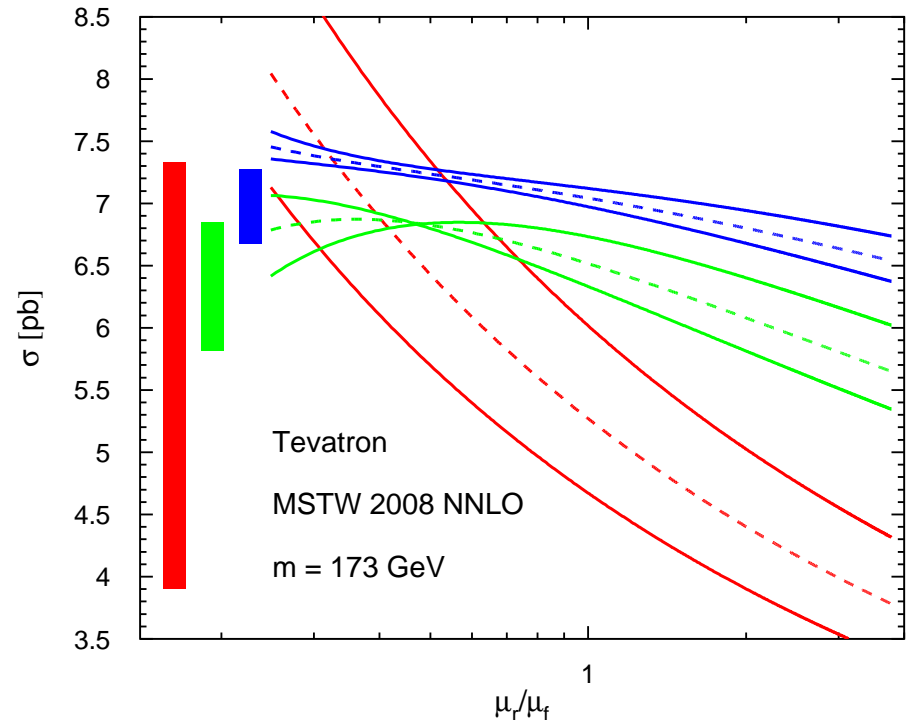
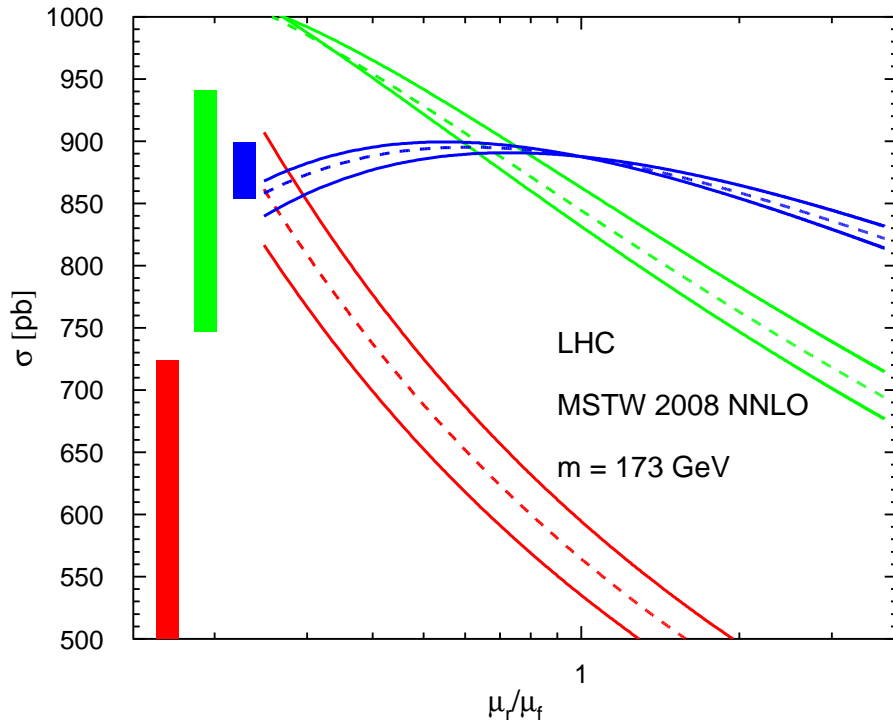
The running top-quark mass

- \overline{MS} mass definition $m(\mu_R)$ realizes running mass (scale dependence)
 - short distance mass probes at scale of hard scattering
 - conversion between pole mass and \overline{MS} mass definition in perturbation theory: $m_t = m(\mu_R) \left(1 + a_s(\mu_R)d^{(1)} + a_s(\mu_R)^2 d^{(2)} \right)$
- Scale dependence greatly reduced

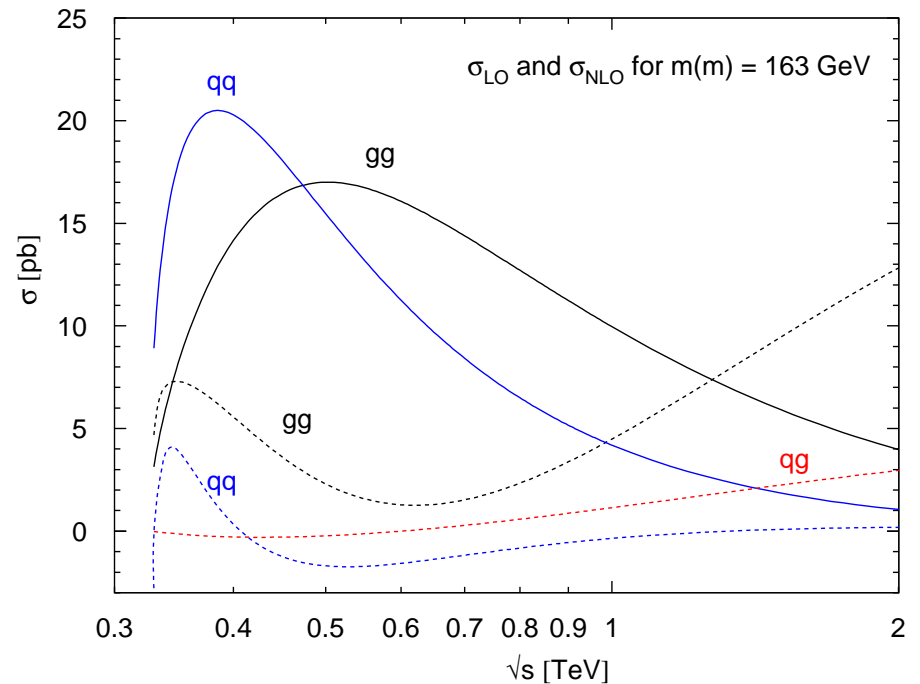
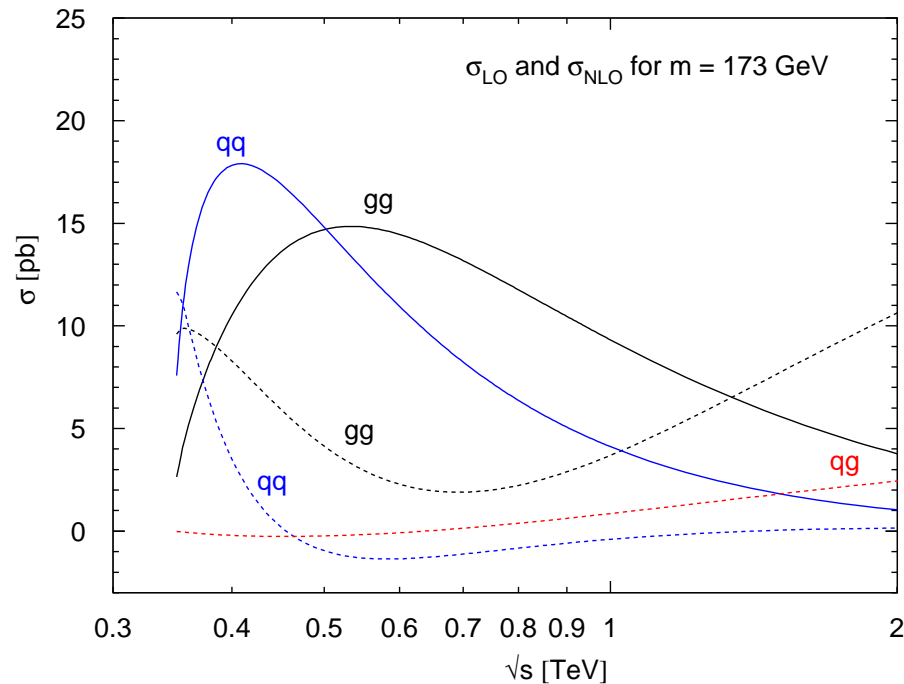


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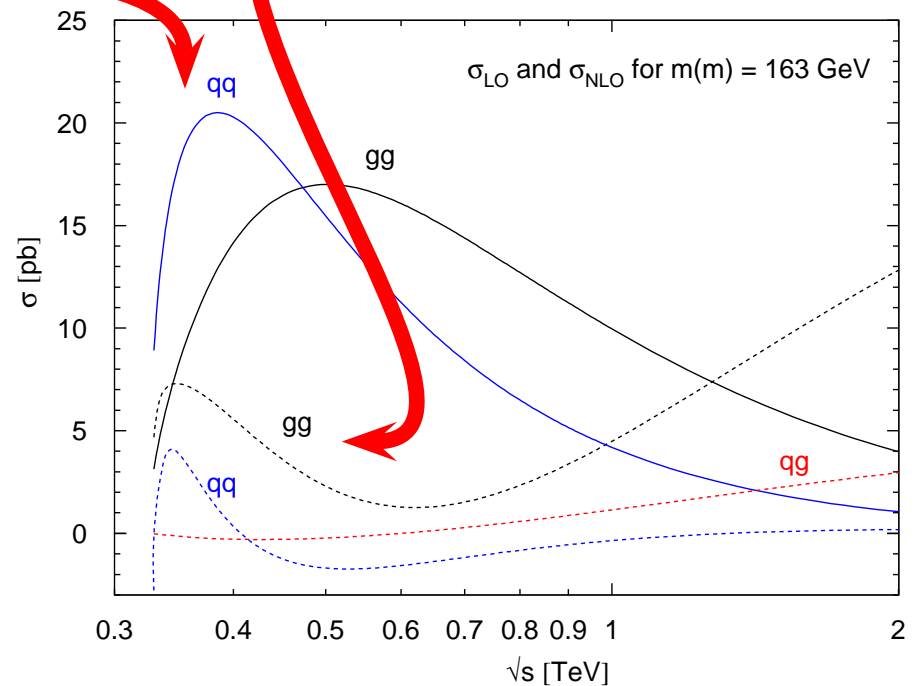
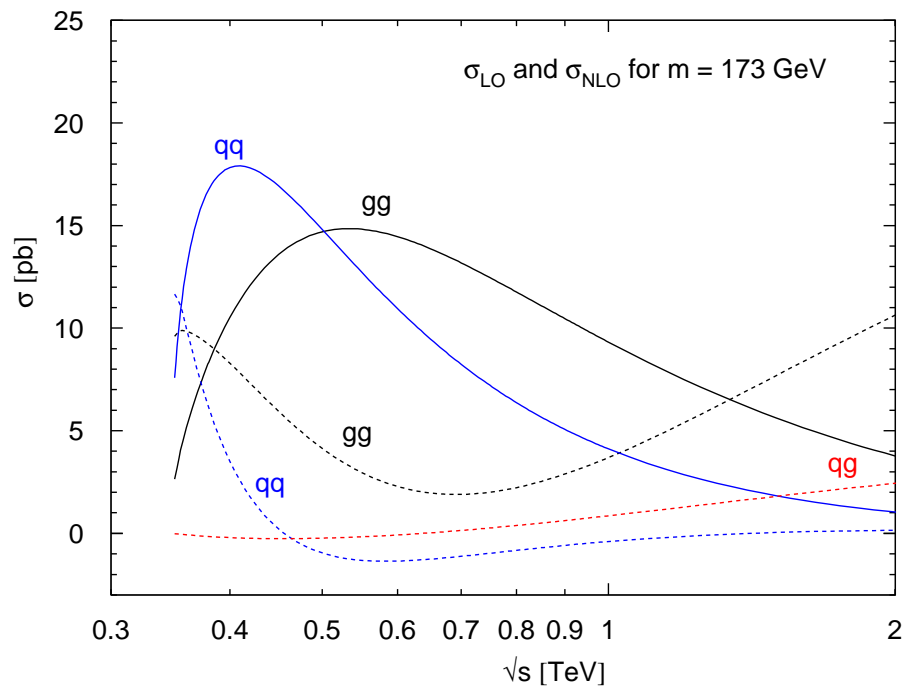
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 - conversion between pole mass and \overline{MS} mass definition in perturbation theory: $m_t = m(\mu_R) \left(1 + a_s(\mu_R)d^{(1)} + a_s(\mu_R)^2 d^{(2)} \right)$
- Pole mass scheme for comparison



- Perturbative stability of predictions with \overline{MS} mass definition
- Parton cross section for channels $q\bar{q}$, gg and qg
 - on-shell scheme for $m_t = 173$ GeV (left)
 - \overline{MS} scheme for $m(m) = 163$ GeV (right)



- Perturbative stability of predictions with \overline{MS} mass definition
- Parton cross section for channels $q\bar{q}$, gg and qg
 - on-shell scheme for $m_t = 173$ GeV (left)
 - \overline{MS} scheme for $m(m) = 163$ GeV (right)
- \overline{MS} scheme
 - more emphasis on LO contribution
 - less significance to threshold region at NLO

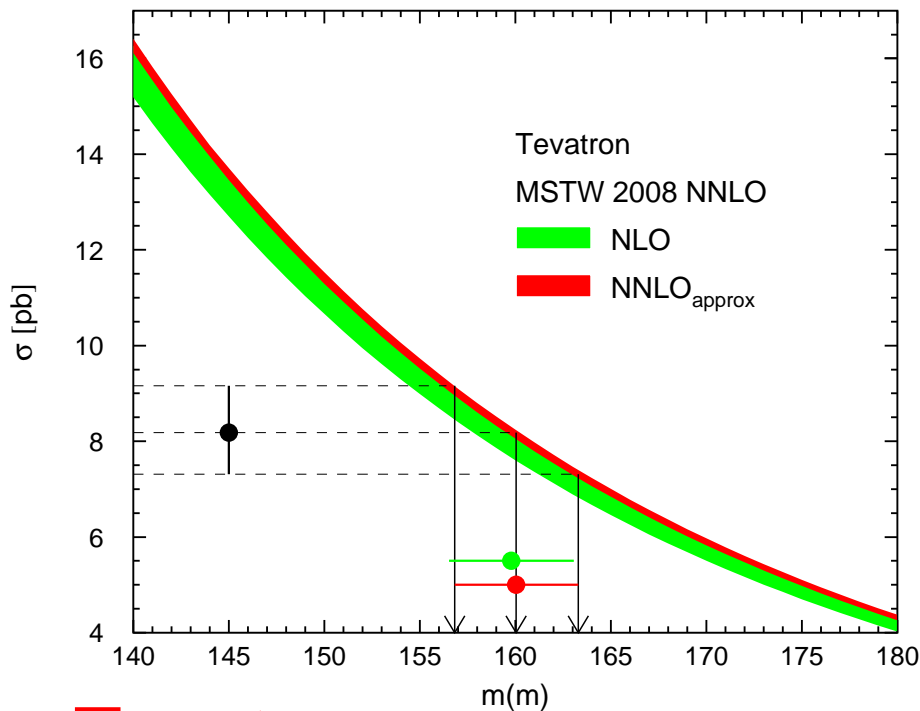


Top quark's \overline{MS} mass dependence

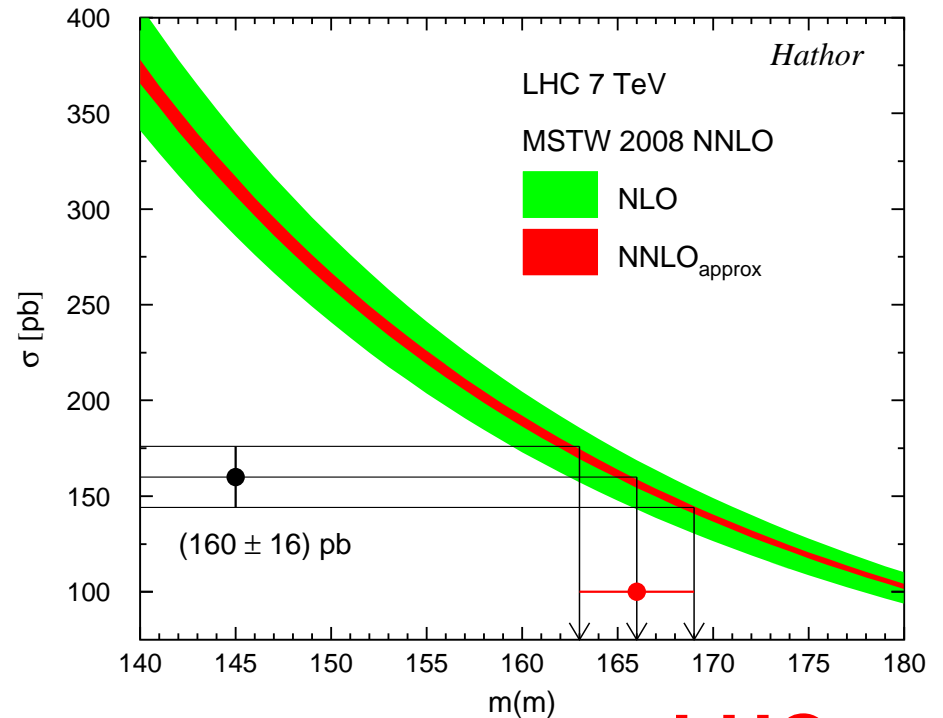
- Total top-quark cross section as function of \overline{m}

Langenfeld, S.M., Uwer '09

- theoretical uncertainty (band) due to variation of $\mu_R \in [\overline{m}/2, 2\overline{m}]$ for fixed set $\mu_F \in \overline{m}/2, \overline{m}, 2\overline{m}$



Tevatron



LHC

Top quark mass determination

- Determine top quark mass from Tevatron cross section data
 - $\sigma_{t\bar{t}} = 7.56^{+0.63}_{-0.56}$ pb D0 coll. arXiv:1105.5384
 - $\sigma_{t\bar{t}} = 7.50^{+0.48}_{-0.48}$ pb CDF coll. CDF-note-9913
- Fit of m_t for individual PDFs
(parton luminosity at Tevatron driven by $q\bar{q}$)

	ABM11	JR09	MSTW08	NN21
$m_t^{\overline{\text{MS}}}(m_t)$	$162.0^{+2.3}_{-2.3}^{+0.7}_{-0.6}$	$163.5^{+2.2}_{-2.2}^{+0.6}_{-0.2}$	$163.2^{+2.2}_{-2.2}^{+0.7}_{-0.8}$	$164.4^{+2.2}_{-2.2}^{+0.8}_{-0.2}$
m_t^{pole}	$171.7^{+2.4}_{-2.4}^{+0.7}_{-0.6}$	$173.3^{+2.3}_{-2.3}^{+0.7}_{-0.2}$	$173.4^{+2.3}_{-2.3}^{+0.8}_{-0.8}$	$174.9^{+2.3}_{-2.3}^{+0.8}_{-0.3}$
(m_t^{pole})	$(169.9^{+2.4}_{-2.4}^{+1.2}_{-1.6})$	$(171.4^{+2.3}_{-2.3}^{+1.2}_{-1.1})$	$(171.3^{+2.3}_{-2.3}^{+1.4}_{-1.8})$	$(172.7^{+2.3}_{-2.3}^{+1.4}_{-1.2})$

Top quark cross section at LHC

- Check predictions at LHC with $\sqrt{s} = 7 \text{ TeV}$
 - cross section computation with HATHOR (version 1.3) [Aliiev, Lacker, Langenfeld, S.M., Uwer, Wiedermann '10](#)
- Atlas at $\sqrt{s} = 7 \text{ TeV}$ $\sigma_{t\bar{t}} = 177_{-10}^{+11} \text{ pb}$
Atlas coll. ATLAS-CONF-2012-024
- CMS at $\sqrt{s} = 7 \text{ TeV}$ $\sigma_{t\bar{t}} = 165.8_{-13.3}^{+13.3} \text{ pb}$
CMS coll. CMS-PAS-TOP-11-024

	ABM11	JR09	MSTW08	NN21
$m_t^{\overline{\text{MS}}}(m_t)$	$159.0_{-2.0}^{+2.1} {}_{-1.4}^{+0.7}$	$165.3_{-2.2}^{+2.3} {}_{-1.2}^{+0.6}$	$166.0_{-2.2}^{+2.3} {}_{-1.5}^{+0.7}$	$166.7_{-2.2}^{+2.3} {}_{-1.3}^{+0.8}$
m_t^{pole}	$168.6_{-2.2}^{+2.3} {}_{-1.5}^{+0.7}$	$175.1_{-2.3}^{+2.4} {}_{-1.3}^{+0.6}$	$176.4_{-2.3}^{+2.4} {}_{-1.6}^{+0.8}$	$177.4_{-2.3}^{+2.4} {}_{-1.4}^{+0.8}$
(m_t^{pole})	$(166.1_{-2.1}^{+2.2} {}_{-2.3}^{+1.7})$	$(172.6_{-2.3}^{+2.4} {}_{-2.1}^{+1.6})$	$(173.5_{-2.3}^{+2.4} {}_{-2.5}^{+1.8})$	$(174.5_{-2.3}^{+2.4} {}_{-2.3}^{+2.0})$

New Observable

Mass measurement with $t\bar{t} + jet$ -samples

- Mass determination with new observable

Alioli, Fuster, Irlles, S.M., Uwer, Vos '12

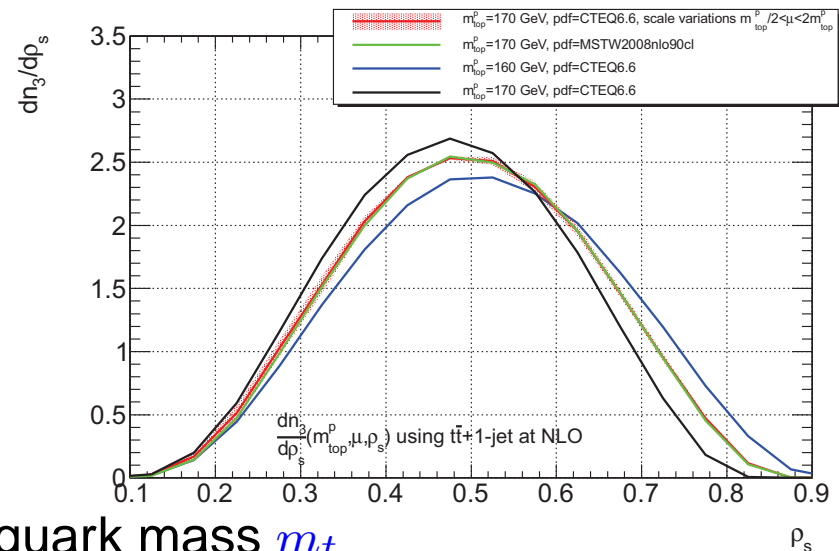
- define normalized-differential $t\bar{t} + jet$ cross section

$$\frac{dn_3}{d\rho_s}(m_{top}, \mu, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1jet}} \frac{d\sigma_{t\bar{t}+1jet}}{d\rho_s}(m_{top}, \mu, \rho_s)$$

- variable $\rho_s = \frac{2 \cdot m_0}{\sqrt{s_{t\bar{t}+1jet}}}$
with $m_0 = 170 \text{ GeV}$
and invariant mass
of multi-jet system $\sqrt{s_{t\bar{t}+1jet}}$

Upshot

- Independent determination of top-quark mass m_t
 - alternative to kinematic reconstruction and extraction from total cross section



Implications on electroweak vacuum

- Relation between Higgs mass m_H and top-quark mass m_t
 - condition of absolute stability of electroweak vacuum $\lambda(\mu) \geq 0$
 - extrapolation of Standard Model up to Planck scale M_P
 - $\lambda(M_P) \geq 0$ implies lower bound on Higgs mass m_H

$$m_H \geq 129.2 + 1.8 \times \left(\frac{m_t^{\text{pole}} - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \right) - 0.5 \times \left(\frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0 \text{ GeV}$$

- recent NNLO analyses Bezrukov, Kalmykov, Kniehl, Shaposhnikov '12; Degrandi, Di Vita, Elias-Miro, Espinosa, Giudice et al. '12
- uncertainty in results due to α_s and m_t (pole mass scheme)

Triviality Bound

- **Quantum corrections to the Higgs potential:** $V(\Phi) = \lambda[\Phi^\dagger\Phi - \frac{v^2}{2}]^2$
- **Corrections to coupling λ**

$$16\pi^2 \frac{d\lambda}{d\ln Q} = 24\lambda^2 - (3g'^2 + 9g^2 - 12y_t^2)\lambda + \frac{3}{8}g'^4 + \frac{3}{4}g'^2g^2 + \frac{9}{8}g^4 - 6y_t^4 + \text{higher order}$$

- **Large mass** \rightsquigarrow λ dominated renormalisation group equation (RGE):

$$16\pi^2 \frac{d\lambda}{d\ln Q} = 24\lambda^2 \quad \Longrightarrow \quad \lambda(Q) = \frac{M_H^2}{2v^2 - \frac{3}{2\pi^2}M_H^2 \ln(Q/v)}$$

λ increases with Q

- **Landau pole**

$$\Lambda \leq v e^{4\pi^2 v^2 / 3M_H^2}$$

New Physics must appear before this point to restore stability

\Longrightarrow For Λ fixed upper bound on M_H

- **Triviality** No quantum theory for $\Lambda \rightarrow \infty$: trivial theory $\lambda = 0$.

Vacuum Stability

- Corrections to coupling λ

$$16\pi^2 \frac{d\lambda}{d \ln Q} = 24\lambda^2 - (3g'^2 + 9g^2 - 12y_t^2)\lambda + \frac{3}{8}g'^4 + \frac{3}{4}g'^2g^2 + \frac{9}{8}g^4 - 6y_t^4 + \text{higher order}$$

- Small mass $\rightsquigarrow y_t$ dominated RGE:

$$16\pi^2 \frac{d\lambda}{d \ln Q} = -6y_t^4 \quad \implies \quad \lambda(Q) = \lambda_0 - \frac{\frac{3}{8\pi^2}y_0^4 \ln \frac{Q}{Q_0}}{1 - \frac{9}{16\pi^2}y_0^2 \ln \frac{Q}{Q_0}}$$

λ decreases with Q ; $\lambda < 0 \rightsquigarrow$ potential unbounded from below

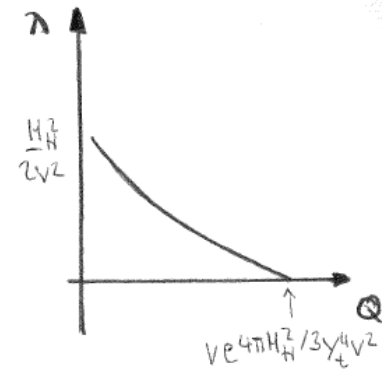
$$\lambda = 0 \text{ for } \lambda_0 \approx \frac{3}{8\pi^2} y_0^4 \ln \frac{Q}{Q_0}$$

- Vacuum stability

$$\Lambda \leq v e^{4\pi^2 M_H^2 / 3y_t^4 v^2}$$

New Physics must appear before this point to ensure vacuum stability

\implies For Λ fixed lower bound on M_H



Implications on electroweak vacuum

- Relation between Higgs mass m_H and top-quark mass m_t

$$m_H \geq 129.2 + 1.8 \times \left(\frac{m_t^{\text{pole}} - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \right) - 0.5 \times \left(\frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0 \text{ GeV}$$

- Uncertainty in Higgs bound due to m_t determined in \overline{MS} scheme

$$m_t^{\overline{MS}}(m_t) = 163.3 \pm 2.7 \text{ GeV}$$

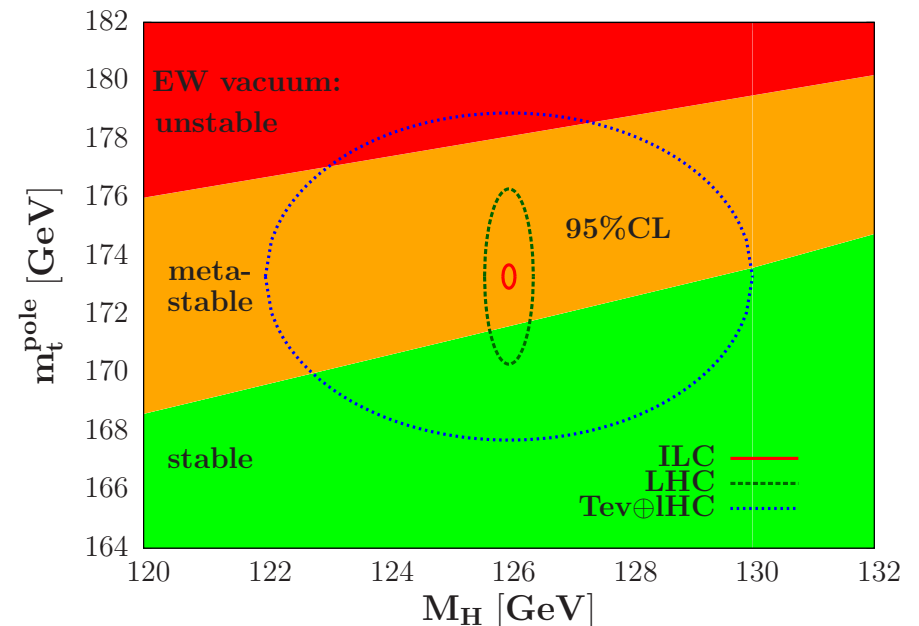
- Implications:

- m_t in pole mass scheme:

$$m_t^{\text{pole}} = 173.3 \pm 2.8 \text{ GeV}$$

- bound on

$$m_H \geq 129.4 \pm 5.6 \text{ GeV}$$



Implications on electroweak vacuum

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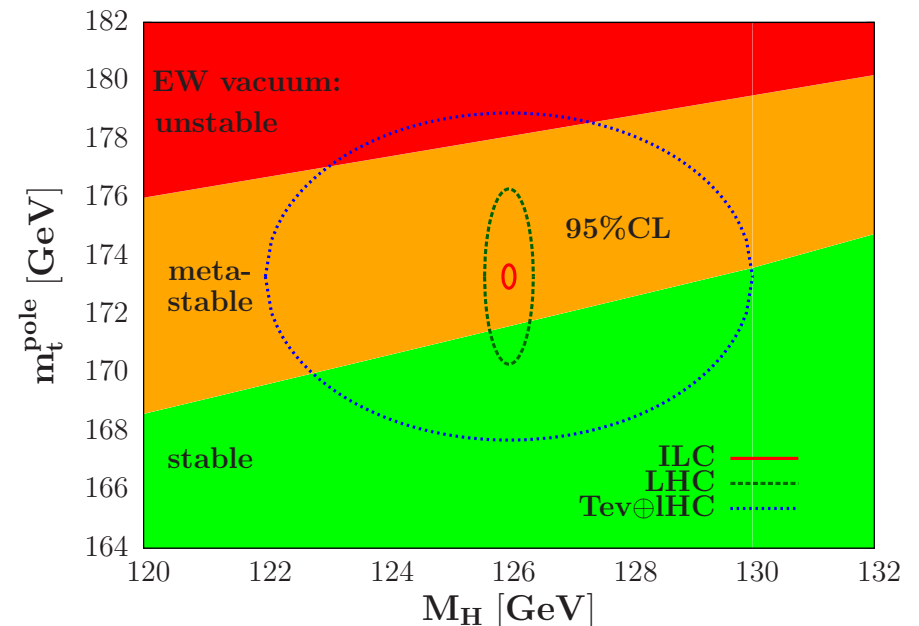
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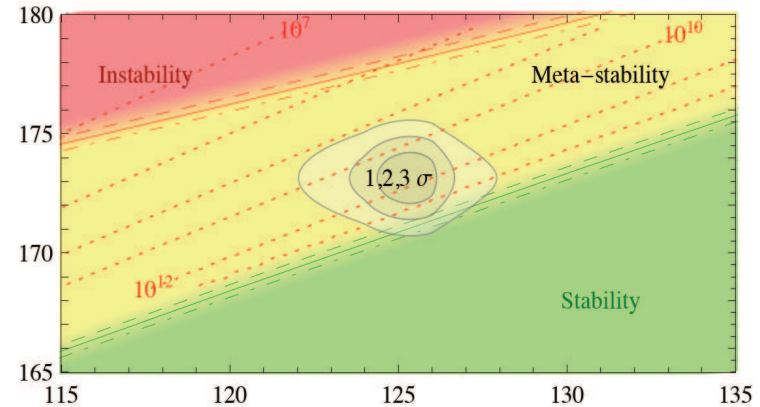
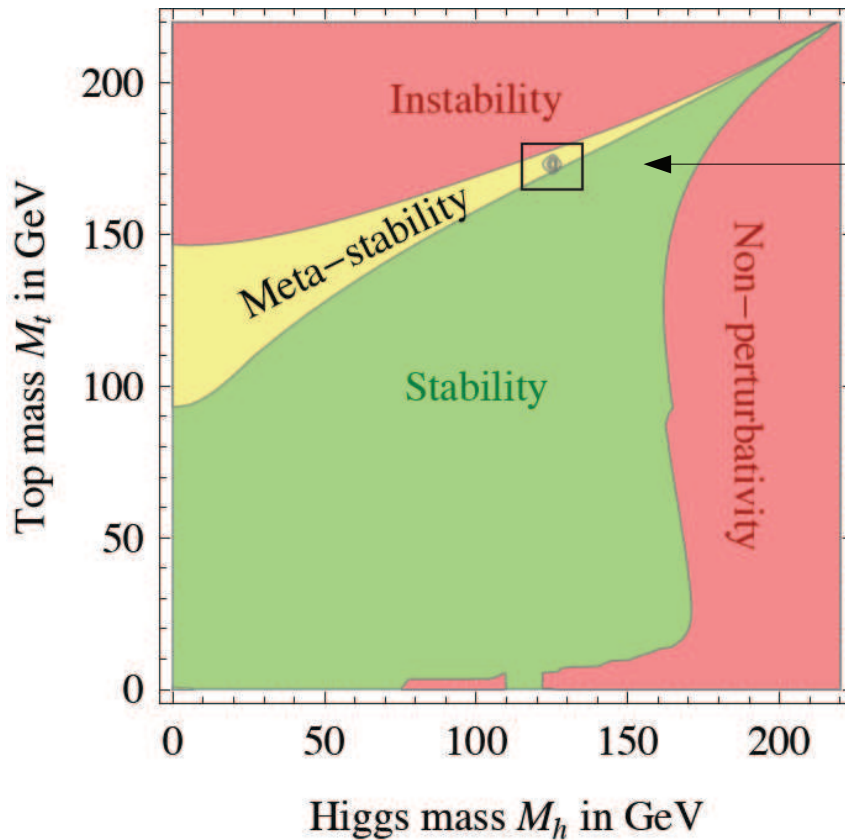
$$m_t^{\text{pole}} = 173.3 \pm 2.8 \text{ GeV}$$

- bound on

$$m_H \geq 129.4 \pm 5.6 \text{ GeV}$$



► Speculations on Planck-scale dynamics



Looking at the plane from a more distant perspective, it appears more clearly that “we live” in a quite “peculiar” region...

And moving m_t down by ~ 2 GeV, we reach the even more peculiar configuration where $\lambda(M_{pl})=0$

Froggatt, Nielsen, Takanishi, '01
 Arkani-Hamed *et al.*, '08
 Shaposhnikov, Wetterich, '10
 ...

G. Isidori (Higgs Hunting 2012)

Summary (part III)

- Top quark theory
 - improved understanding of theory and application of new concepts
 - resummation important for Tevatron and LHC phenomenology
- Cross sections
 - NNLO predictions for $t\bar{t}$
 - NLO corrections to $t\bar{t} + \text{jet}$
 - electroweak corrections
- \overline{MS} mass definition
 - greatly reduced scale dependence
 - much improved convergence of perturbation theory