

*LFV SUSY searches with  
Rp conservation*

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Dubna, CALC 2009*

# OUTLINE

- **Basic physics**
- **Input / bounds from FV processes**  
(emphasis on rare charged lepton decays/conversions)
- **Effects of Quantum Corrections**
- **Constraining non-universality from symmetries**
- **Cosmological data**
- **LFV collider signatures**

## Recent Reviews:

- *Flavour Physics of Leptons & Dipole Moments, M. Raidal et al., hep-ph/0801.1826*
- *Collider aspects of flavour physics at high Q, F. del Aguila et al., hep-ph/0801.1800*
- *RGEs:*  
*See i.e. Hisano & Nomura, hep-ph/9810479.*

## MSSM content & parameters

- SM particles & superpartners
- 2 Higgs fields with coupling  $\mu$ , ratio of v.e.v.s =  $\tan\beta$
- SUSY-breaking parameters:

Scalar masses  $m_0$       Gaugino masses  $m_{1/2}$

Trilinear soft terms  $A_\lambda$       Bilinear soft terms  $B_\mu$

- Assume universality? constrained MSSM = CMSSM

Single  $m_0$ , single  $m_{1/2}$ , single  $A_\lambda, B_\mu$

- CMSSM different from mSUGRA

where we have additional relations, as functions of  $m_{3/2}$

Strong bounds from flavour violating processes  
motivate Universality in soft scalar masses

$$BR(\mu \rightarrow e\gamma) \lesssim 1.2 \cdot 10^{-11}$$

$$BR(\mu^- \rightarrow e^- e^+ e^-) \lesssim 10^{-12}$$

$$BR(\tau \rightarrow e\gamma) \lesssim 1.1 \cdot 10^{-7}$$

$$BR(\tau \rightarrow \mu\gamma) \lesssim 6.8 \cdot 10^{-8}$$

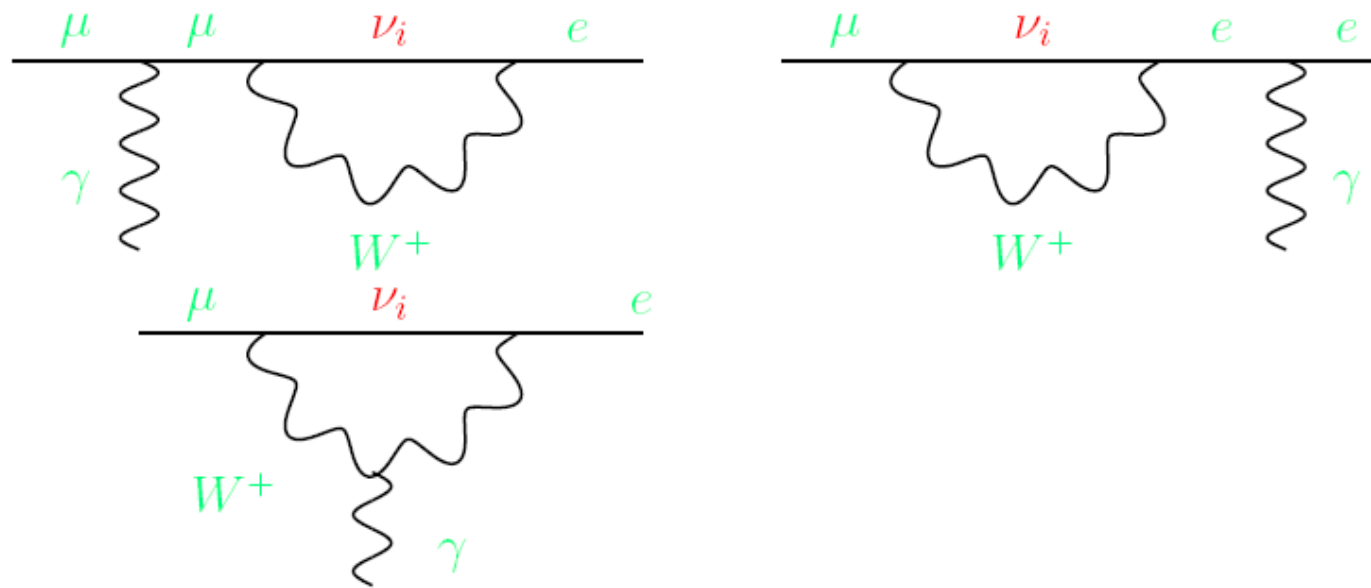
$$BR(\tau \rightarrow ll') \lesssim O(10^{-8}) \quad (l, l' = e, \mu)$$

*Very good expected future BR sensitivities:*

$$\mu \rightarrow e\gamma \quad 10^{-14}$$

$$\mu^- Ti \rightarrow e^- Ti \quad 10^{-18}$$

1.  $\mu \rightarrow e\gamma$  in the SM with  $m_{\nu_i} \neq 0$

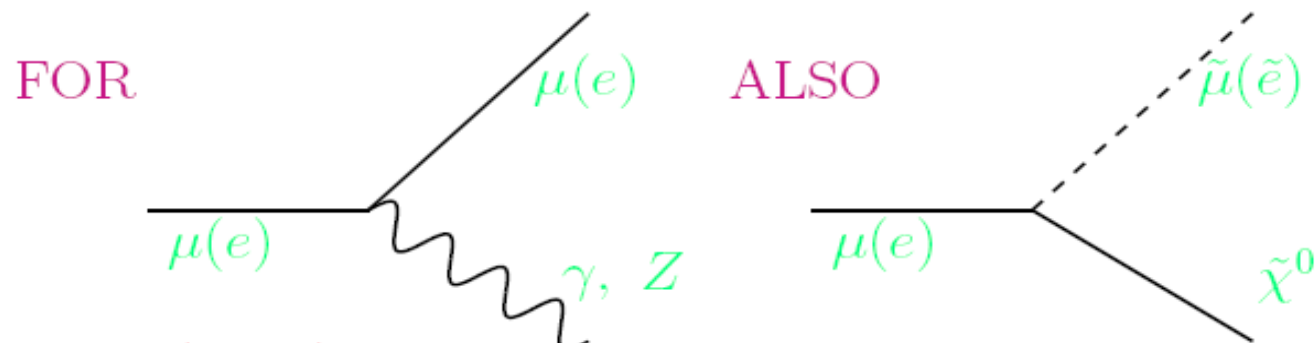


$$\nu_i = \nu_\mu \cos \theta + \nu_e \sin \theta, \quad \Gamma = \frac{1}{16} \frac{G_F^2 m_\mu^5 \alpha}{128 \pi^4} \left( \frac{m_2^2 - m_1^2}{m_W^2} \right) \sin^2 \theta \cos^2 \theta$$

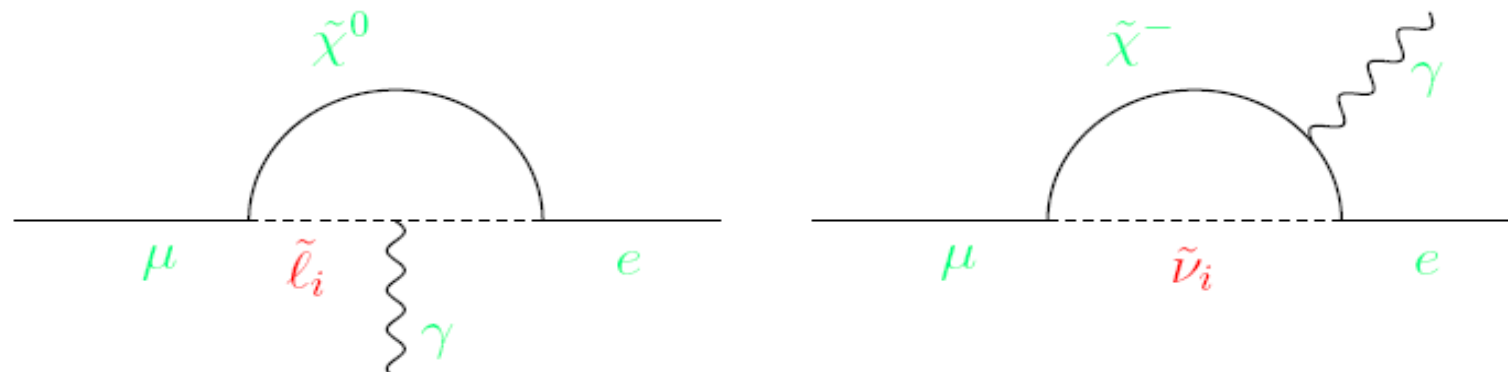
$BR \leq 10^{-50}$ , for  $\Delta m_{12}^2$  from neutrino data too small!

## LFV in minimal SUSY

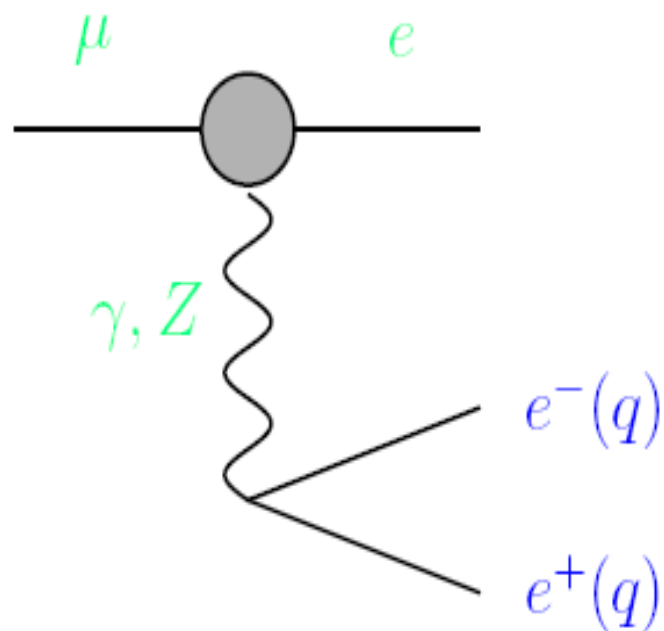
MSSM: For each SM vertex, also the one with  
2 particles  $\rightarrow$  superparticles



If  $\tilde{\mu}$ - $\tilde{e}$  ( $\tilde{\nu}_\mu$ - $\tilde{\nu}_e$ ) mixing, large rates for:



2.  $\mu \rightarrow 3e$  et  $\mu$ - $e$  conversion on nuclei



+ ... (suppressed box-diagr.)

$$BR \leq 10^{-53}$$

for  $\Delta m_{12}^2$  from neutrino data



Quite some space for deviations from universality  
in consistency with all bounds

✧ Universality violations possible at a high scale?  
*If yes, we need to predict their magnitude  
(possibly through flavour symmetries)*

✧ Even if we have universality at a high scale,  
it may be broken at low energies  
due to quantum corrections

*Let us now look at all these in more detail:*

## Generic SLEPTON mass matrices

In the unrotated basis  $\tilde{\ell}_i = (\tilde{e}_L, \tilde{\mu}_L, \tilde{\tau}_L, \tilde{e}_R^*, \tilde{\mu}_R^*, \tilde{\tau}_R^*)$ , the slepton mass matrix reads as:

$$\mathcal{L}_M = -\frac{1}{2}\tilde{\ell}^\dagger M_{\tilde{\ell}}^2 \tilde{\ell}, \quad M_{\tilde{\ell}}^2 = \begin{pmatrix} M_{LL}^2 & M_{LR}^2 \\ M_{RL}^2 & M_{RR}^2 \end{pmatrix},$$

where

$$\begin{aligned} M_{LL}^2 &= \frac{1}{2}m_\ell^\dagger m_\ell + M_L^2 - \frac{1}{2}(2m_W^2 - m_Z^2) \cos 2\beta I \\ M_{RR}^2 &= \frac{1}{2}m_\ell^\dagger m_\ell + M_R^2 - (m_Z^2 - m_W^2) \cos 2\beta I \\ M_{LR}^2 &= (A^e - \mu \tan \beta) m_\ell \\ M_{RL}^2 &= (M_{LR}^2)^\dagger \end{aligned}$$

$$A_{ij}^e = A_0 \cdot \delta_{ij}, \quad M_L^2 = M_R^2 = m_0^2 I$$

$$\delta_{XX}^{ij} = (M_{XX}^2)^{ij} / (M_{XX}^2)^{ii} \quad (X = L, R)$$

## Universal soft terms at GUT(mSUGRA models)

In a basis such that  $m_f$  is diagonal:

$$M_{\tilde{\ell}}^2 = \left( \begin{array}{ccc|ccc} m_{\tilde{e}_L}^2 & 0 & 0 & \bar{A}_{\tilde{e}} \cdot m_e & 0 & 0 \\ 0 & m_{\tilde{\mu}_L}^2 & 0 & 0 & \bar{A}_{\tilde{\mu}} \cdot m_{\mu} & 0 \\ 0 & 0 & m_{\tilde{\tau}_L}^2 & 0 & 0 & \bar{A}_{\tilde{\tau}} \cdot m_{\tau} \\ \hline \bar{A}_{\tilde{e}} \cdot m_e & 0 & 0 & m_{\tilde{e}_R}^2 & 0 & 0 \\ 0 & \bar{A}_{\tilde{\mu}} \cdot m_{\mu} & 0 & 0 & m_{\tilde{\mu}_R}^2 & 0 \\ 0 & 0 & \bar{A}_{\tilde{\tau}} \cdot m_{\tau} & 0 & 0 & m_{\tilde{\tau}_R}^2 \end{array} \right)$$

The 1st and 2nd generation sleptons are almost degenerate:

$$m_{\tilde{\tau}_L} < m_{\tilde{e}_L} = m_{\tilde{\mu}_L} \quad ; \quad m_{\tilde{\tau}_R} < m_{\tilde{e}_R} = m_{\tilde{\mu}_R}$$

$$m_{\tilde{\tau}_R} < m_{\tilde{\tau}_L}$$

## Simplest Scheme: 2-3 Lepton Flavour Violation

*(motivated by large Atmospheric Neutrino Mixing)*

If large 2-3 mixing, in a basis such that  $m_l$  is diagonal:

$$M_{\tilde{\ell}}^2 = \left( \begin{array}{ccc|ccc} m_{\tilde{e}_L}^2 & 0 & 0 & \bar{A}_{\tilde{e}} \cdot m_e & 0 & 0 \\ 0 & m_{\tilde{\mu}_L}^2 & M_{LL}^2 & 0 & \bar{A}_{\tilde{\mu}} \cdot m_{\mu} & 0 \\ 0 & M_{LL}^2 & m_{\tilde{\tau}_L}^2 & 0 & 0 & \bar{A}_{\tilde{\tau}} \cdot m_{\tau} \\ \hline \bar{A}_{\tilde{e}} \cdot m_e & 0 & 0 & m_{\tilde{e}_R}^2 & 0 & 0 \\ 0 & \bar{A}_{\tilde{\mu}} \cdot m_{\mu} & 0 & 0 & m_{\tilde{\mu}_R}^2 & M_{RR}^2 \\ 0 & 0 & \bar{A}_{\tilde{\tau}} \cdot m_{\tau} & 0 & M_{RR}^2 & m_{\tilde{\tau}_R}^2 \end{array} \right)$$

Flavor mixing entries are defined as

$$\delta_{XX}^{ij} = (M_{XX}^2)^{ij} / (M_{XX}^2)^{ii} \quad (X = L, R).$$

*LFV through RGE effects*

## Including See-Saw neutrinos

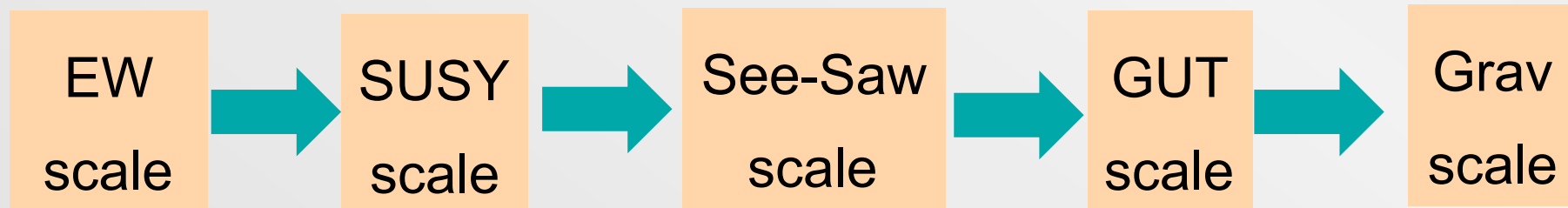
Leptonic Sector of Superpotential (*up to See-Saw scale*):

$$W = N_i^c (\lambda_\nu)_{ij} L_j H_2 - E_i^c (\lambda_e)_{ij} L_j H_1 + \frac{1}{2} N_i^c \mathcal{M}_{ij} N_j^c + \mu H_2 H_1$$

Superpotential of Effective Low Energy Theory:

$$W_{eff} = L_i H_2 \left( \lambda_\nu^T (\mathcal{M}^D)^{-1} \lambda_\nu \right)_{ij} L_j H_2 - E_i^c (\lambda_e)_{ij} L_j H_1$$

RGE evolution: *Various Steps*



Even if:

$$M_{\text{GUT}} : m_{\tilde{\ell}, \tilde{\nu}} \propto \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \text{RGEs} \longrightarrow \begin{pmatrix} 1 & \star & \star \\ \star & 1 & \star \\ \star & \star & 1 \end{pmatrix}$$

- RGEs for the charged-lepton mass matrix

$$t \frac{d}{dt} (m_{\tilde{\ell}}^2)_i^j = \frac{1}{16\pi^2} \left\{ (m_{\tilde{\ell}}^2 \lambda_{\ell}^{\dagger} \lambda_{\ell})_i^j + (m_{\tilde{\ell}}^2 \lambda_{\nu}^{\dagger} \lambda_{\nu})_i^j + \dots \right\}$$

The corrections in the basis where  $(\lambda_{\ell}^{\dagger} \lambda_{\ell})_i^j$  is diagonal, are:

$$\delta m_{\tilde{\ell}} \propto \frac{1}{16\pi} \ln \frac{M_{\text{GUT}}}{M_N} \lambda_{\nu}^{\dagger} \lambda_{\nu} m_{\text{SUSY}}^2$$

(And similar corrections for  $\delta m_{\tilde{\nu}}$ )

For big  $\mu$ - $e$  lepton mixing, big rates for  $\mu \rightarrow e\gamma$

*Provided the neutrino Yukawas are sufficiently large (larger  $M_N$  in See-Saw)*

Corrections from Massive Neutrinos to Yukawa Couplings  
(from MGUT to MN)

$$16\pi^2\mu\frac{d}{d\mu}f_{e_{ij}} = \left\{ -\frac{9}{5}g_1^2 - 3g_2^2 + 3\text{Tr}(f_d f_d^\dagger) + \text{Tr}(f_e f_e^\dagger) \right\} f_{e_{ij}} \\ + 3(f_e f_e^\dagger f_e)_{ij} + (f_e f_\nu^\dagger f_\nu)_{ij},$$

$$16\pi^2\mu\frac{d}{d\mu}f_{\nu_{ij}} = \left\{ -\frac{3}{5}g_1^2 - 3g_2^2 + 3\text{Tr}(f_u f_u^\dagger) + \text{Tr}(f_\nu f_\nu^\dagger) \right\} f_{\nu_{ij}} \\ + 3(f_\nu f_\nu^\dagger f_\nu)_{ij} + (f_\nu f_e^\dagger f_e)_{ij}.$$

(very simple at 1-loop, small  $\tan\beta$ )

$$16\pi^2\frac{d}{dt}\lambda_\tau = (\lambda_N^2 - G_E)\lambda_\tau$$

$$16\pi^2\frac{d}{dt}\lambda_N = (4\lambda_N^2 + 3\lambda_t^2 - G_N)\lambda_N$$



## Slepton contributions from runs if $M_{\text{grav}} \sim M_{\text{GUT}}$

*RGEs from  $M_{\text{grav}} \sim M_{\text{GUT}} \rightarrow M_N$ :*

$$(m_{\bar{L}}^2)_{ij} \simeq -\frac{1}{8\pi^2} (3m_0^2 + a_0^2) V_{Dki}^* V_{Dkj} f_{\nu_k}^2 \log \frac{M_{\text{grav}}}{M_{\nu_k}}$$

$$(m_{\bar{e}}^2)_{ij} \simeq 0,$$

$$A_e^{ij} \simeq -\frac{3}{8\pi^2} a_0 f_{e_i} V_{Dki}^* V_{Dkj} f_{\nu_k}^2 \log \frac{M_{\text{grav}}}{M_{\nu_k}},$$

*Contribute only to LL slepton mixing*

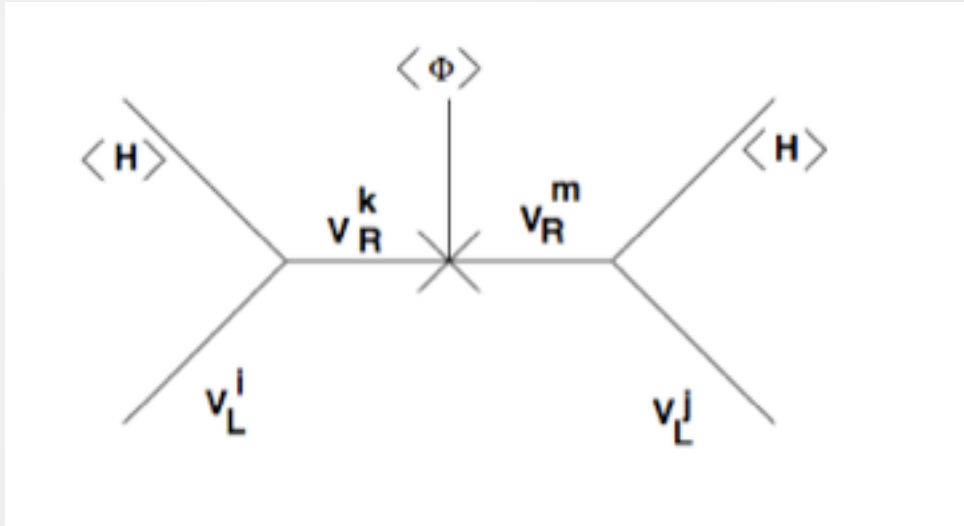
## Slepton contributions from runs if $M_{\text{grav}} > M_{\text{GUT}}$

*Renormalisation effects from  $M_{\text{GUT}} \rightarrow M_G (= M_P?)$*

$$(m_L^2)_{ij} \simeq -\frac{2}{(4\pi)^2} U_{ik} f_{\nu_k}^2 U_{jk}^* (3m_0^2 + A_0^2) \log \frac{M_G}{M_{N_k}},$$
$$(m_E^2)_{ij} \simeq -\frac{6}{(4\pi)^2} e^{-i\varphi_{d_i}} V_{ki}^* f_{u_k}^2 V_{kj} e^{i\varphi_{d_j}} (3m_0^2 + A_0^2) \log \frac{M_G}{M_{\text{GUT}}},$$

*Contribute also to RR slepton mixing*

Keep also in mind renormalisation of effective neutrino operator



$$16\pi^2 \frac{d}{dt} \sin^2 2\theta_{23} = -2 \sin^2 2\theta_{23} (1 - \sin^2 2\theta_{23}) (Y_\tau^2) \frac{m_{eff}^{33} + m_{eff}^{22}}{m_{eff}^{33} - m_{eff}^{22}}$$

$$\frac{m_{eff}^{ij}}{m_{eff,0}^{ij}} = \exp \left\{ \frac{1}{8\pi^2} \int_{t_0}^t \left( -c_i g_i^2 + 3\lambda_t^2 + \frac{1}{2}(\lambda_i^2 + \lambda_j^2) \right) \right\} \quad I_{\lambda_i} = \exp \left[ \frac{1}{8\pi^2} \int_{t_0}^t \lambda_i^2 dt \right]$$

$$= I_g \cdot I_t \cdot \sqrt{I_{\lambda_i}} \cdot \sqrt{I_{\lambda_j}}$$

## SU(5) - small $\tan \beta$

(large top, small bottom and tau Yukawa)

Observables	Numerical Values
$m_{\nu_1}/m_{\nu_3}$	0.16(0.09)
$m_{\nu_2}/m_{\nu_3}$	0.20(0.37)
$M_1/M_3$	0.06(0.16)
$M_2/M_3$	0.12(0.42)
$\theta_{23}$	0.91(1.13)
$\theta_{12}$	0.56(0.10)
$\theta_{13}$	0.21(0.07)
$\delta$	0.43(-0.45)
$J_{CP}$	0.0088(0.00066)
$\epsilon_1$	0.00046(0.0039)
$\epsilon_2$	0.0007(0.00014)
$\epsilon_3$	0.0003(0.000001)
$BR(\mu \rightarrow e\gamma)$	$8.5 \times 10^{-12}(6.1 \times 10^{-14})$
$BR(\tau \rightarrow e\gamma)$	$5.95 \times 10^{-13}(1.74 \times 10^{-14})$
$BR(\tau \rightarrow \mu\gamma)$	$5.1 \times 10^{-12}(2.6 \times 10^{-12})$

[Ellis, Gomez, SL]

*LFV through non-Universality at high energies*

## SU(5) unification

$$5^* : \begin{pmatrix} d_1^c \\ d_2^c \\ d_3^c \\ e^- \\ -\nu_e \end{pmatrix}_L, \begin{pmatrix} s_1^c \\ s_2^c \\ s_3^c \\ \mu^- \\ -\nu_\mu \end{pmatrix}_L, \begin{pmatrix} b_1^c \\ b_2^c \\ b_3^c \\ \tau^- \\ -\nu_\tau \end{pmatrix}_L$$

*SU(5) to SU(3) X SU(2) X U(1) decomposition:*

$5^* : (3^*, 1, 1/3) + (1, 2^*, -1/2)$

## SU(5) unification

$$10 : \left( \begin{array}{ccc|cc} 0 & u_3^c & -u_2^c & -u^1 & -d^1 \\ -u_3^c & 0 & u_1^c & -u^2 & -d^2 \\ u_2^c & -u_1^c & 0 & -u^3 & -d^3 \\ \hline u^1 & u^2 & u^3 & 0 & -e^+ \\ d^1 & d^2 & d^3 & e^+ & 0 \end{array} \right)_L, \left( \begin{array}{cc} \mu^+ & c^i \\ s^i & c_i^c \end{array} \right)_L, \left( \begin{array}{cc} \tau^+ & t^i \\ b^i & t_i^c \end{array} \right)_L$$

*SU(5) to SU(3) X SU(2) X U(1) decomposition:*

$$\underline{10 : (3^*, 1, -2/3) + (3, 2, 1/6) + (1, 1, 1)}$$

## $SU(5)$

- (i) Assume the family symmetry is combined with  $SU(5)$
- (ii) Use the GUT structure ONLY to constrain  $U(1)$  charges

Under this group we have the following relations:

$$Q_{(q,u^c,e^c)_i} = Q_i^{10}$$

$$Q_{(l,d^c)_i} = Q_i^{\bar{5}}$$

$$Q_{(\nu_R)_i} = Q_i^{\nu_R}$$

- $M_{up}$  symmetric
- $M_{\ell\pm} = M_{down}^T$
- L lepton mixing  $\approx$  R down-quark one



Can we obtain acceptable patterns of masses/mixings? i.e.

$$\frac{M_u}{m_t} = \begin{pmatrix} \bar{\epsilon}^6 & \bar{\epsilon}^5 & \bar{\epsilon}^3 \\ \bar{\epsilon}^5 & \bar{\epsilon}^4 & \bar{\epsilon}^2 \\ \bar{\epsilon}^3 & \bar{\epsilon}^2 & 1 \end{pmatrix}, \frac{M_{down}}{m_b} = \begin{pmatrix} \bar{\epsilon}^4 & \bar{\epsilon}^3 & \bar{\epsilon}^3 \\ \bar{\epsilon}^3 & \bar{\epsilon}^2 & \bar{\epsilon}^2 \\ \bar{\epsilon} & 1 & 1 \end{pmatrix}$$

$$\frac{M_\ell}{m_\tau} = \begin{pmatrix} \bar{\epsilon}^4 & \bar{\epsilon}^3 & \bar{\epsilon} \\ \bar{\epsilon}^3 & \bar{\epsilon}^2 & 1 \\ \bar{\epsilon}^3 & \bar{\epsilon}^2 & 1 \end{pmatrix}, m_{eff} \propto \begin{pmatrix} \bar{\epsilon}^2 & \bar{\epsilon} & \bar{\epsilon} \\ \bar{\epsilon} & 1 & 1 \\ \bar{\epsilon} & 1 & 1 \end{pmatrix}$$

## Flavour symmetries determine soft SUSY terms

$$\mathcal{L}_{m^2} = m_0^2(\phi_1^*\phi_1 + \phi_2^*\phi_2 + \phi_3^*\phi_3 + \left(\frac{\langle\theta\rangle}{M_{\text{fl}}}\right)^{q_2-q_1} \phi_1^*\phi_2 + \left(\frac{\langle\theta\rangle}{M_{\text{fl}}}\right)^{q_3-q_1} \phi_1^*\phi_3 + \left(\frac{\langle\theta\rangle}{M_{\text{fl}}}\right)^{q_3-q_2} \phi_2^*\phi_3 + \text{h.c.}).$$

L-R symmetric

$$\begin{pmatrix} 1 & \tilde{\epsilon}^{|a+2b|} & \tilde{\epsilon}^{|a+b|} \\ \tilde{\epsilon}^{|a+2b|} & 1 & \tilde{\epsilon}^{|b|} \\ \tilde{\epsilon}^{|a+b|} & \tilde{\epsilon}^{|b|} & 1 \end{pmatrix}$$

SU(5)

$$\mathbf{E}_L \sim \begin{pmatrix} 1 & \lambda^2 & \lambda^2 \\ \lambda^2 & 1 & 1 \\ \lambda^2 & 1 & 1 \end{pmatrix}$$

$$\mathbf{E}_R \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

$$Q_{(q,u^c,e^c)_i} = Q_i^{10}$$

$$Q_{(l,d^c)_i} = Q_i^{\bar{5}}$$

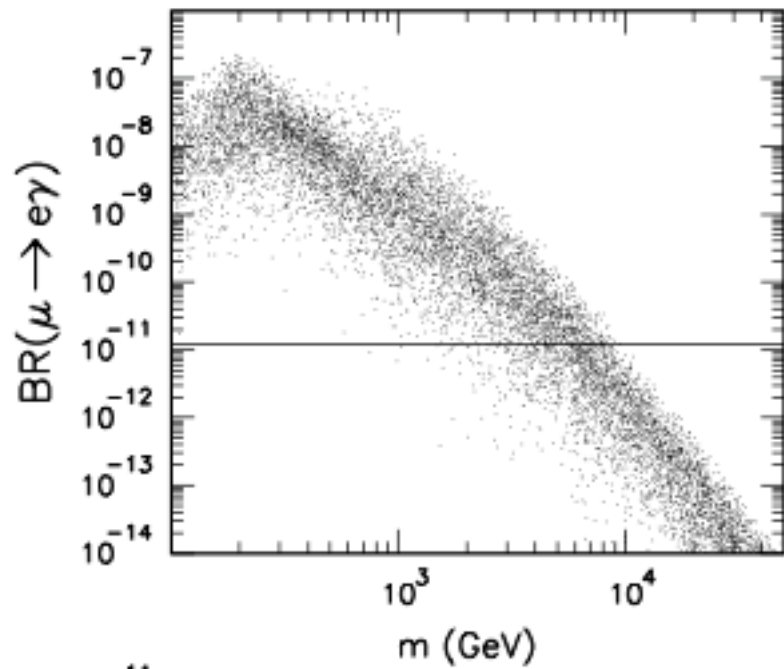
$$Q_{(\nu_R)_i} = Q_i^{\nu R}$$

$$\frac{M_\ell}{m_\tau} = \begin{pmatrix} \bar{\epsilon}^4 & \bar{\epsilon}^3 & \bar{\epsilon} \\ \bar{\epsilon}^3 & \bar{\epsilon}^2 & 1 \\ \bar{\epsilon}^3 & \bar{\epsilon}^2 & 1 \end{pmatrix}$$

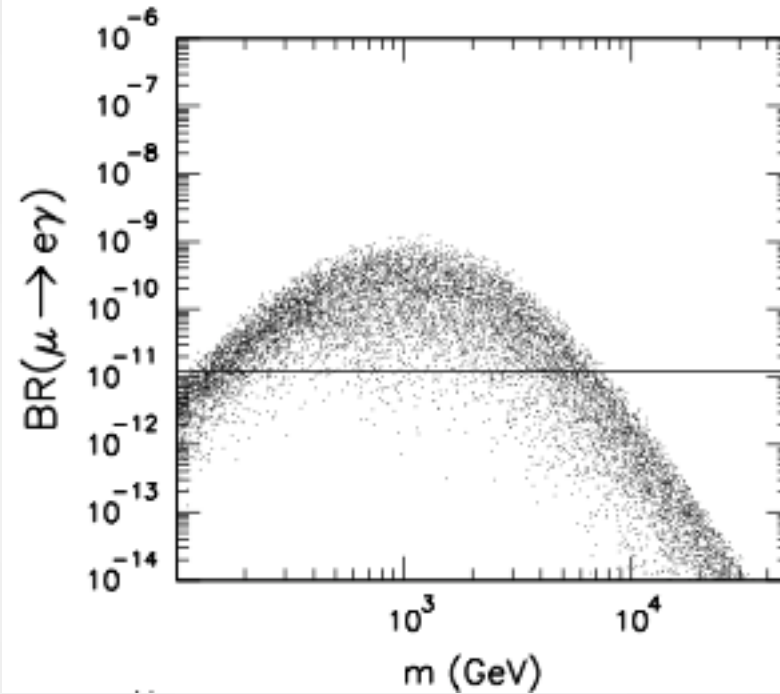
L: (1,0,0)

R: (3,2,0)

[Chankowski, Kowalska, Lavignac, Pokorski]



$M_{1/2}=400, \quad m \sim m_0$



$M_{1/2}=1000$

*Very large sparticle masses required*

## Viable models with non-Abelian flavour symmetries

*i.e. SU(3) family symmetry* [\[Antusch, King, Malinsky\]](#)

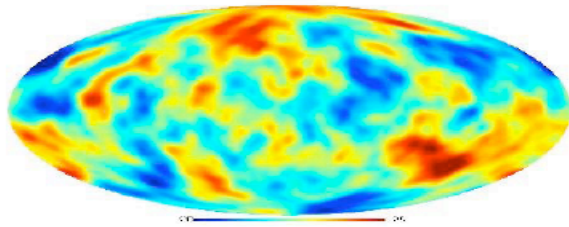
$$\hat{m}_{\nu^c}^2 \approx m_0^2 \left[ b_0^{\nu^c} \mathbb{1} + \begin{pmatrix} \varepsilon^2 \bar{\varepsilon}^2 b_1^{\nu^c} & \varepsilon^2 \bar{\varepsilon}^2 b_1^{\nu^c} e^{i\phi_1} & \varepsilon^2 \bar{\varepsilon}^2 b_1^{\nu^c} e^{i\phi_2} \\ \cdot & \varepsilon^2 b_2^{\nu^c} & \varepsilon^2 b_2^{\nu^c} e^{i\phi_3} \\ \cdot & \cdot & \varepsilon_3^2 b_3^{\nu^c} \end{pmatrix} + \dots \right]$$
$$\hat{m}_{e^c}^2 \approx m_0^2 \left[ b_0^{e^c} \mathbb{1} + \begin{pmatrix} \bar{\varepsilon}^4 b_1^{e^c} & \bar{\varepsilon}^4 b_1^{e^c} e^{i\phi_1} & \bar{\varepsilon}^4 b_1^{e^c} e^{i\phi_2} \\ \cdot & \varepsilon^2 b_2^{e^c} & \varepsilon^2 b_2^{e^c} e^{i\phi_3} \\ \cdot & \cdot & \bar{\varepsilon}_3^2 b_3^{e^c} \end{pmatrix} + \dots \right].$$

*Viable predictions for smaller SUSY masses*

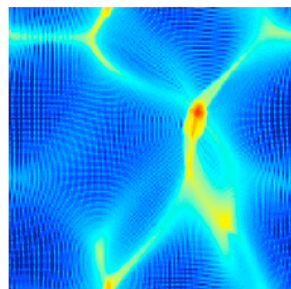
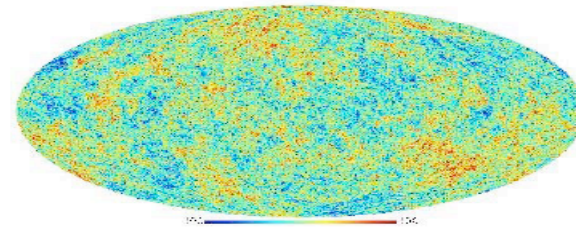
*Including Dark Matter Considerations  
in SUSY with massive neutrinos*

# COSMOLOGICAL OBSERVATIONS

COBE  
(7 degree resolution)



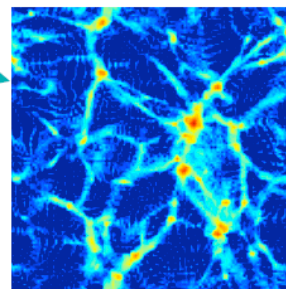
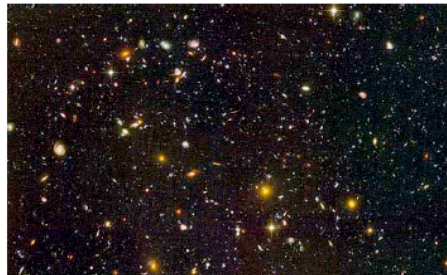
WMAP  
(0.25 degree resolution)



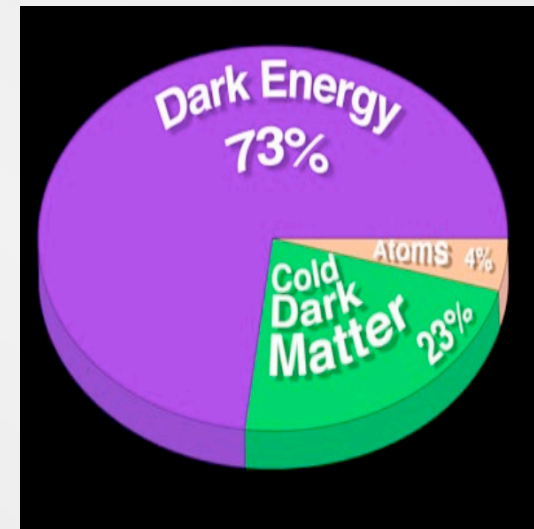
HDM wipes out structure on small scales

Simulations of DM density maps

Hubble Deep Field



CDM creates too many sub-structures?



## Dark Matter– What can it be?

Has to be Weakly Interacting

*(if strong or EM would couple to matter and be detectable)*

- Baryonic? (i.e. Neutron Stars, Black Holes)

- Neutrinos? *(simplest schemes excluded by WMAP)*

- Axions?

- Lightest SUSY particle (LSP)?

○ Neutralino?

○ S-neutrino *(excluded by LEP direct searches)*

○ Gravitino? *(would be really hard to detect)*

***The parametric space favoured by Cosmology  
also constrains the allowed channels in Colliders  
(for instance SUSY cascade chains)***



# WMAP on CMSSM (*stable neutralino LSP*)

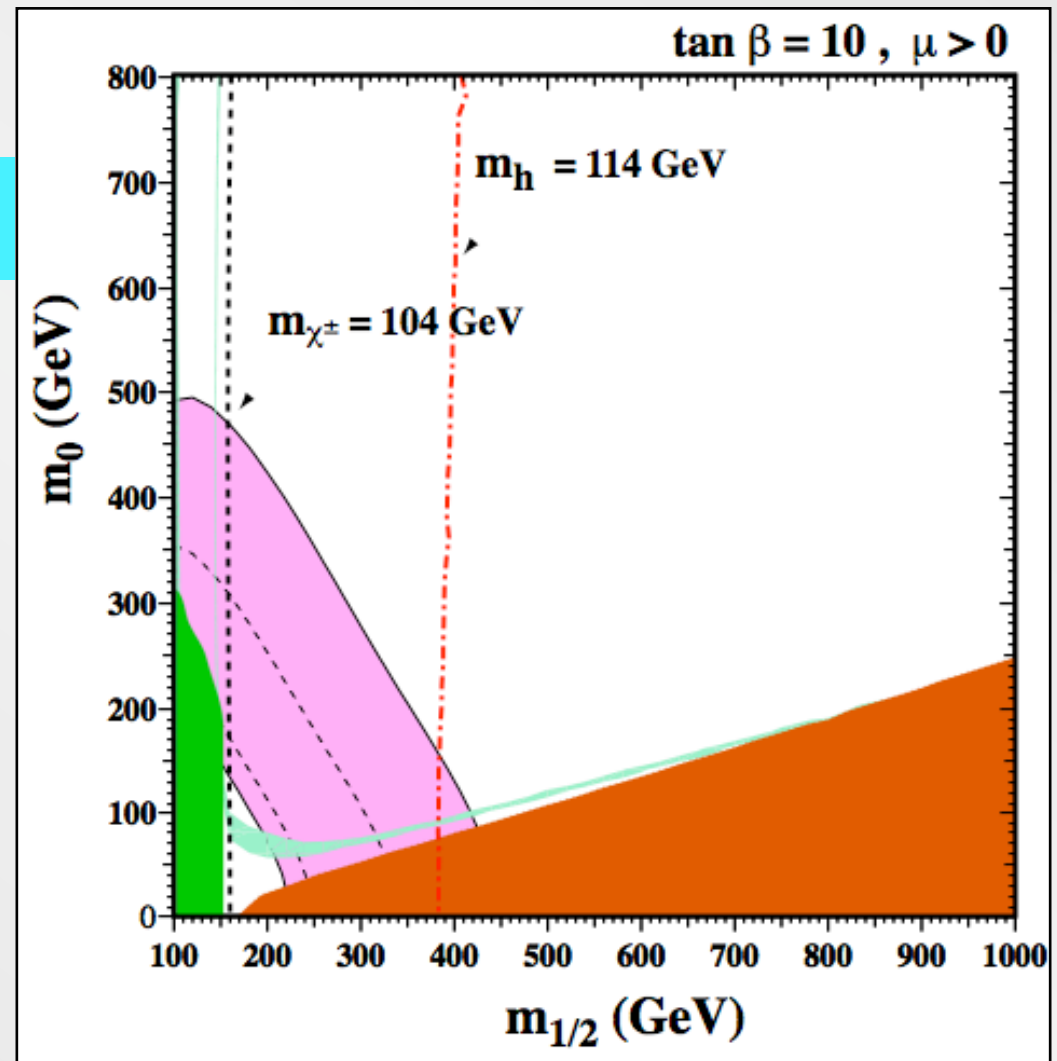
[Ellis, Olive, Santoso, Spanos]

WMAP bound on relic density

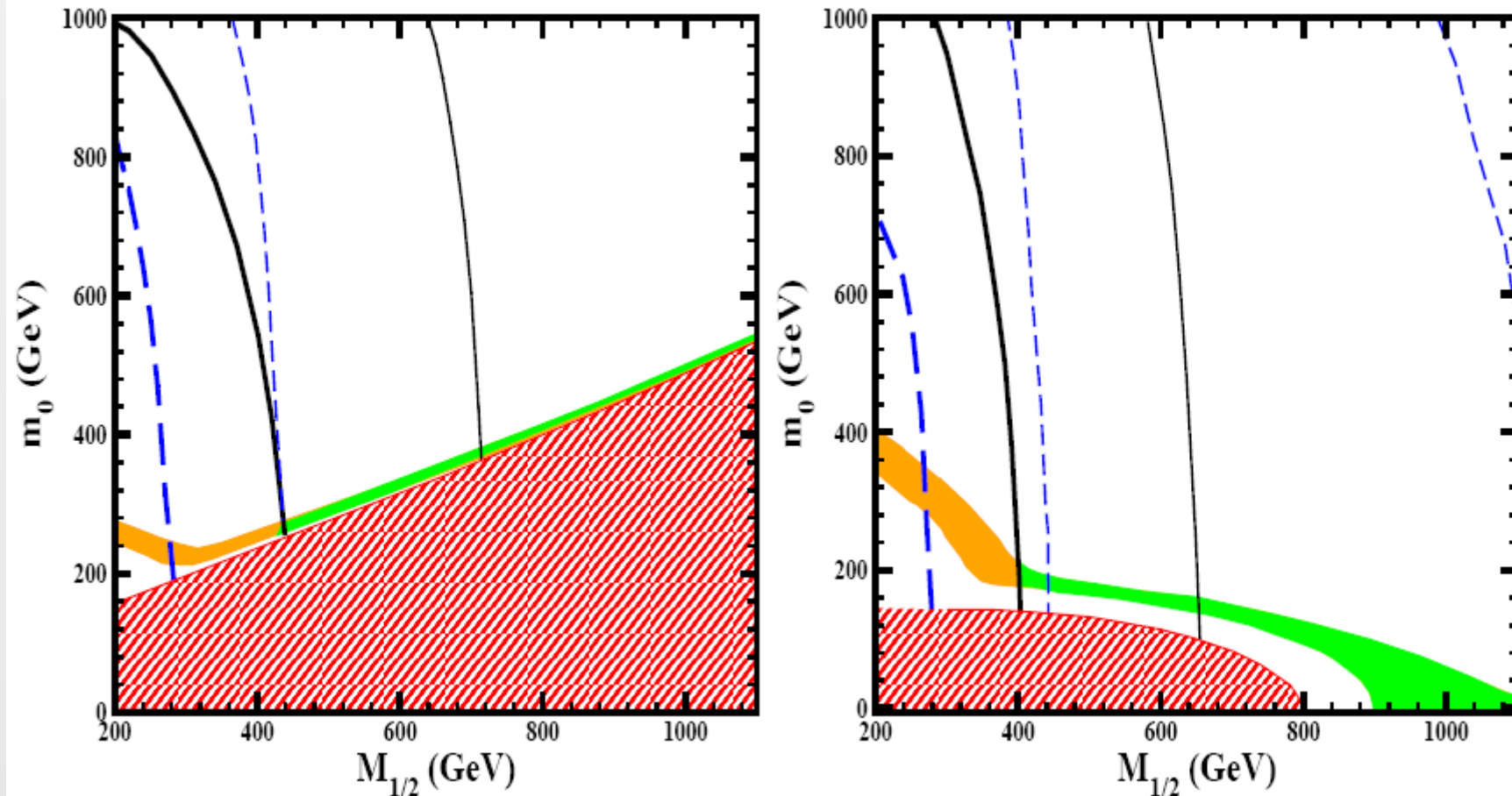
Excluded since stau LSP

Excluded by  $b \rightarrow s$  gamma

Favoured by  $g - 2$  (?)



*If massive neutrinos with large Yukawa couplings and/or additional GUT corrections, picture significantly modified!*

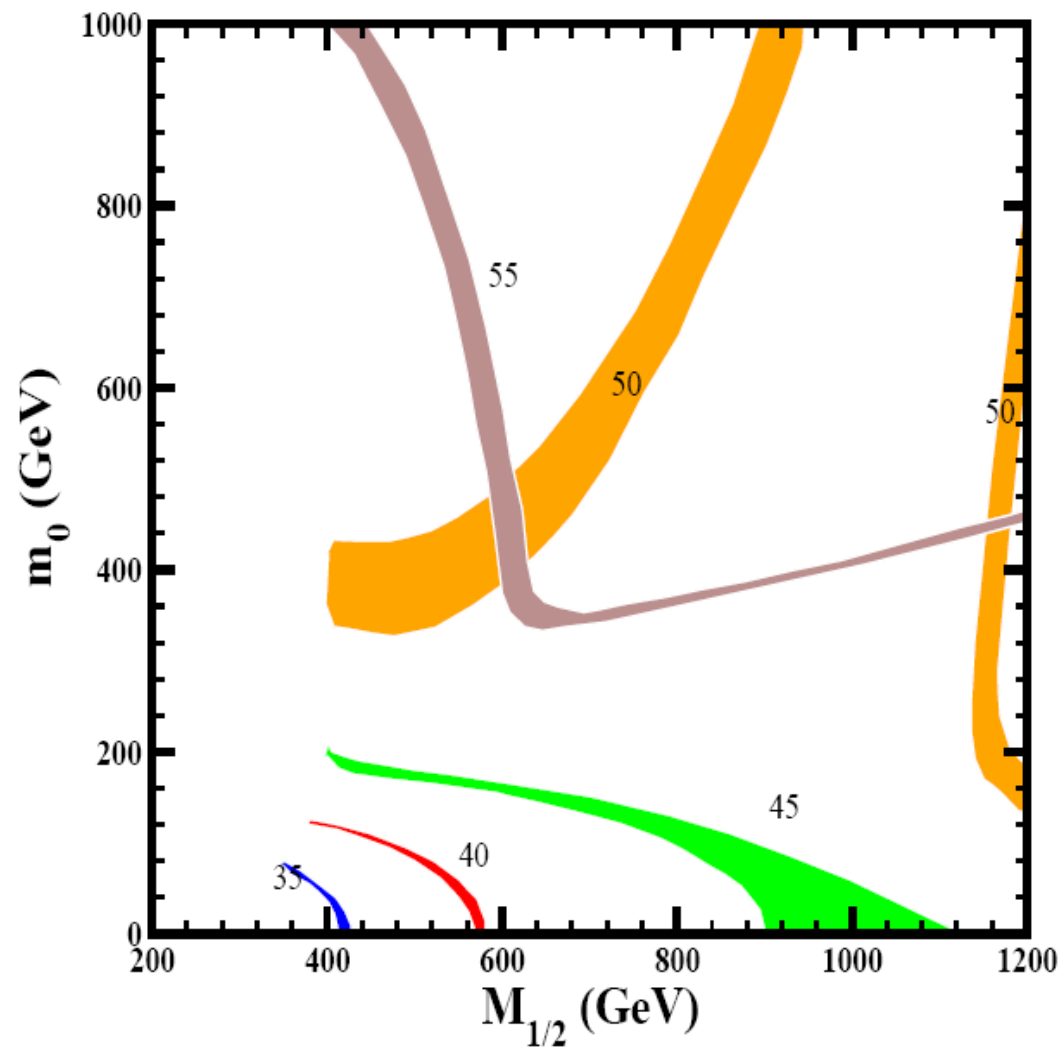


Effect of quantum corrections to Yukawas & (s-)particle masses

[Gomez, SL, Naranjo, Rodriguez-Quintero]

*Allowed region (linked to sparticle spectra)*

*very sensitive to  $\tan\beta$*



## *LFV in Colliders*

## Bounds from Rare processes very strong

Can the LHC or the ILC see LFV?

In which channels?

For which area of the SUSY parameter space?

**IT TURNS OUT THAT:**

✧ In general, the LHC and the ILC good for probes for a **heavy sparticle spectrum**

✧ Also for areas where **cancellations** take place **in the loop diagrams** for rare decays

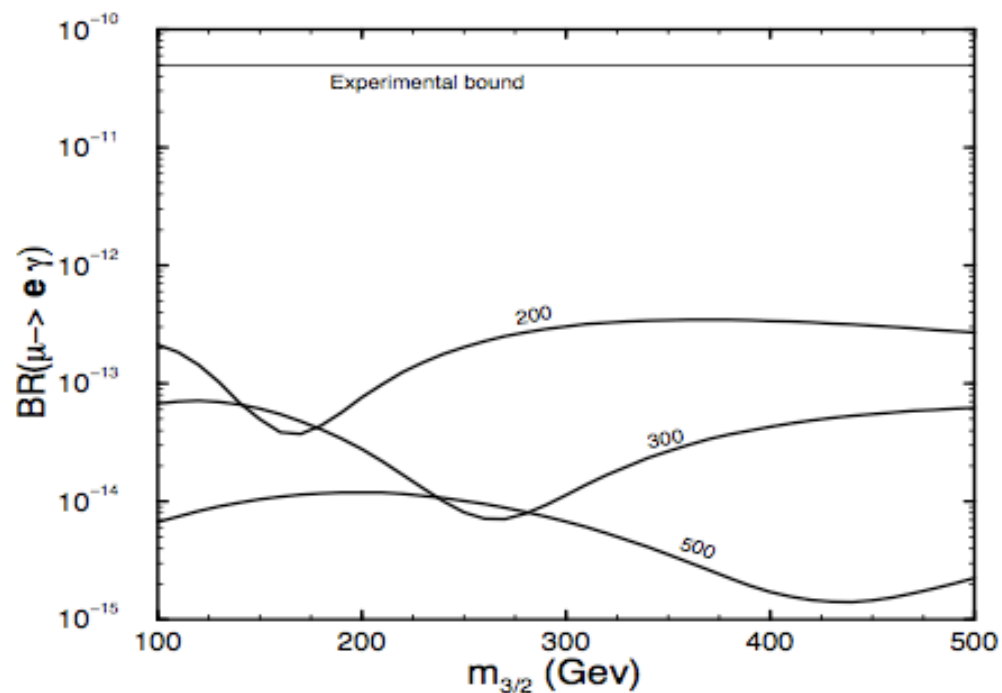
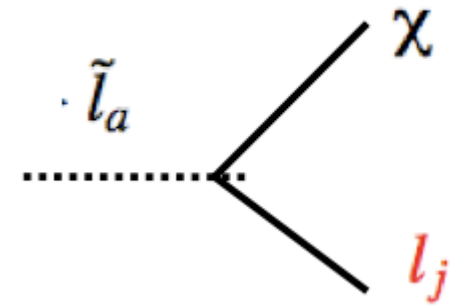
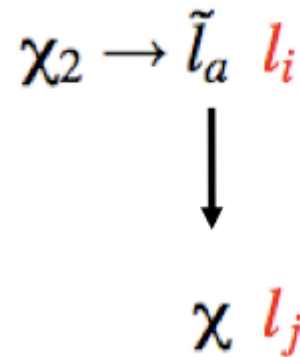
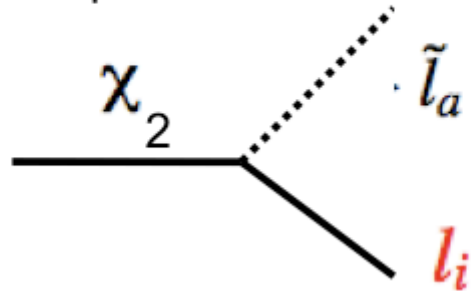


Figure 3:  $BR(\mu \rightarrow e \gamma)$  for a range of values of  $m_{1/2}$  (labeled above). Universal soft masses at the GUT scale are considered ( $\Delta = 0$ ). The curves are obtained using  $\tan \beta = 7$  and  $A_0 = -1.5m_{3/2}$  as input parameters.

## Example of FC versus LFV

[Hisano, Kitano, Nojiri]

Lepton pairs in neutralino decays:



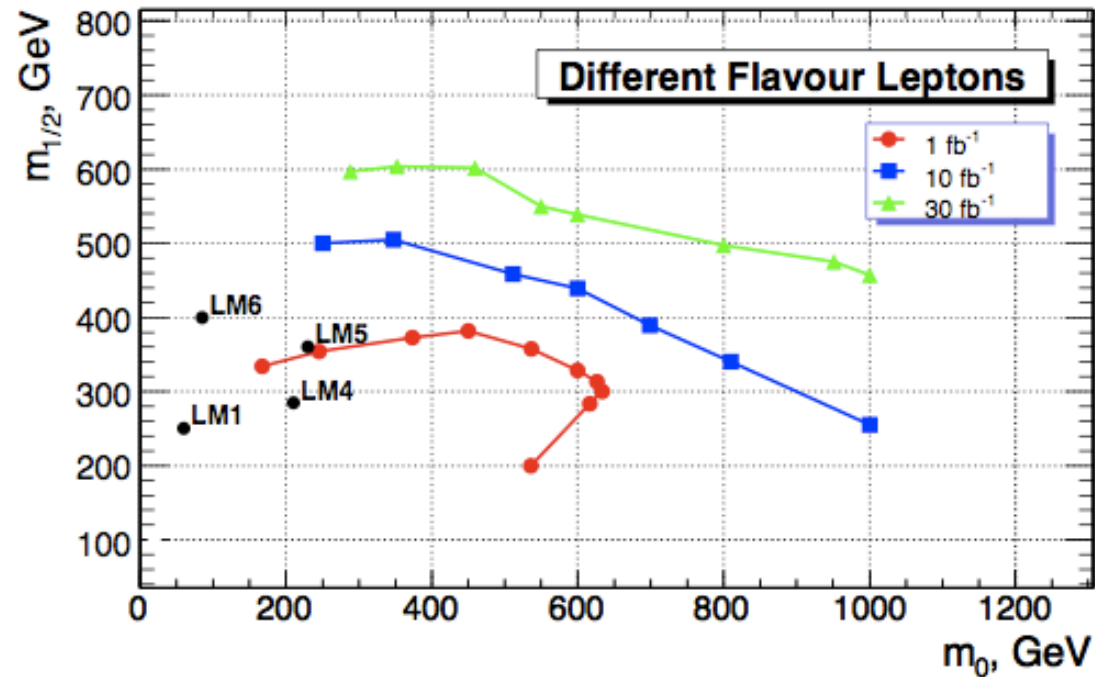
LFV: Decays involving leptons of different flavour

**How large LFV?**

Depends on sfermion mixing (back to MODEL BUILDING)

## LFV in $\mu$ -e channel

[Andreev, Bityukov, Krasnikov, Toropin]

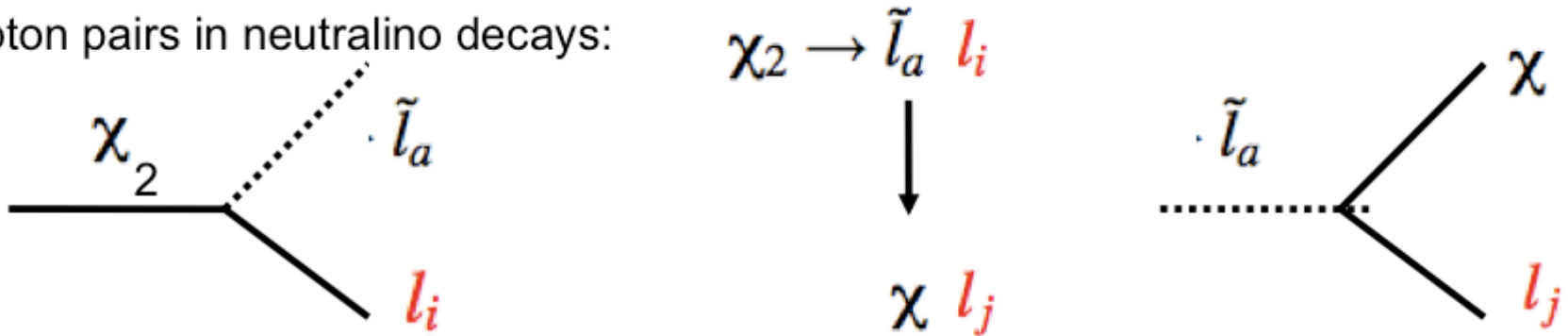


**Fig. 3.10:** Discovery plot ( $\tan\beta = 10$ ,  $\text{sign}(\mu) = +$ ,  $A = 0$ ) for the luminosities  $\mathcal{L} = 1, 10, 30 \text{ fb}^{-1}$  for the  $e^\pm\mu^\mp + \cancel{E}_T$  signature.



## LFV in the $\tau - \mu$ channel

Lepton pairs in neutralino decays:



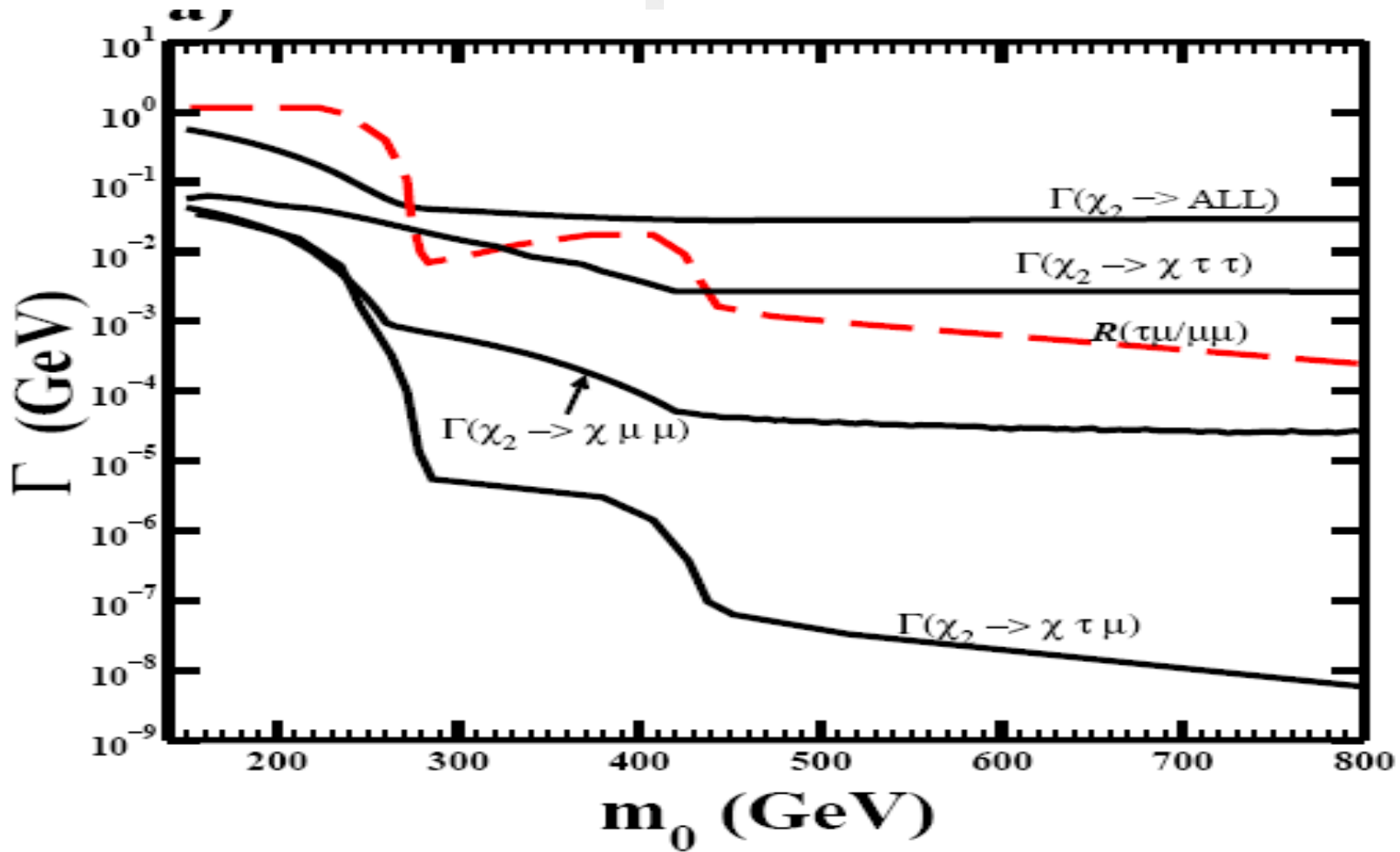
LFV:

$$\chi_2 \rightarrow \chi + \tau^\pm \mu^\mp$$

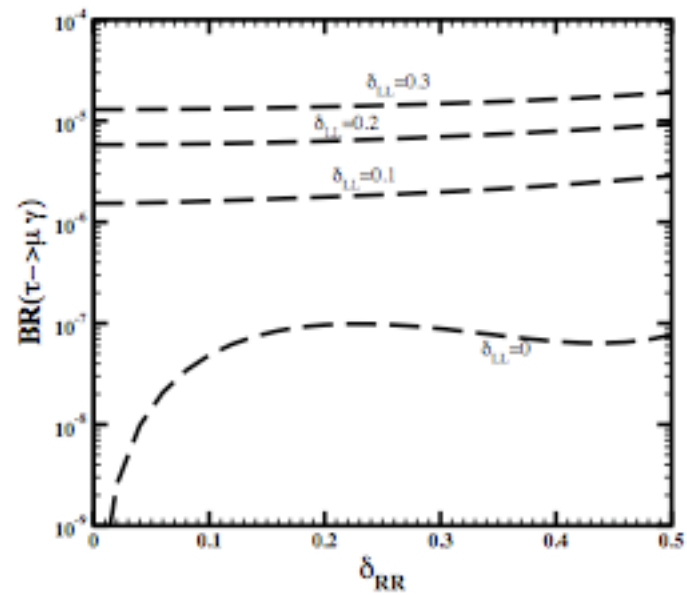
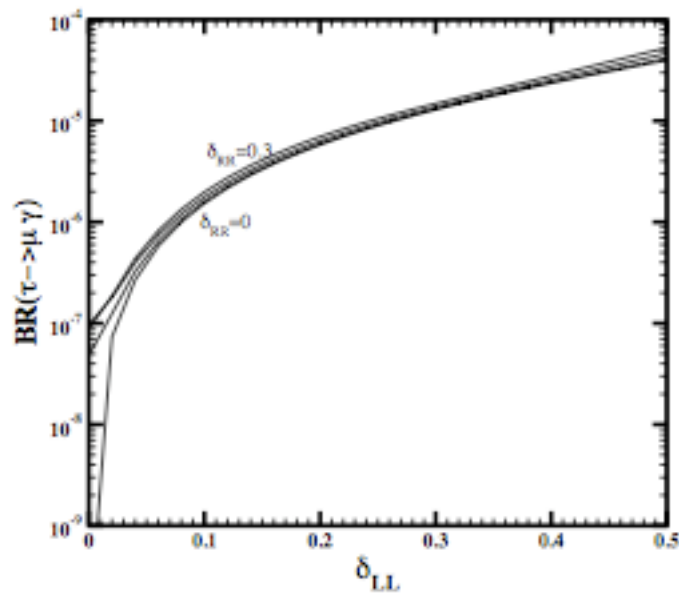
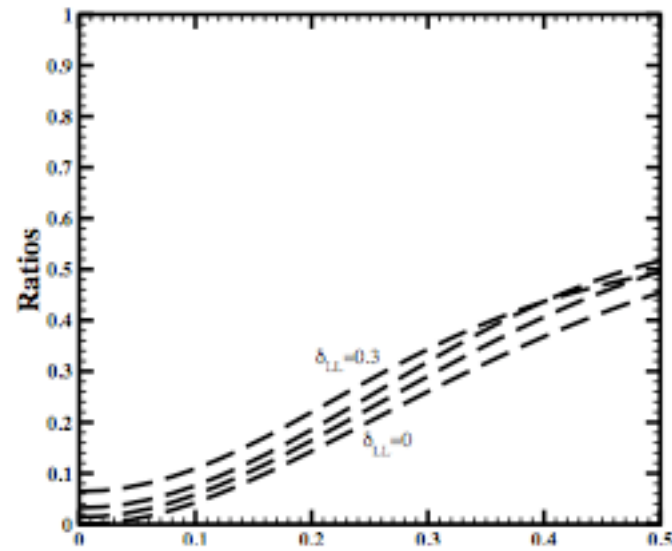
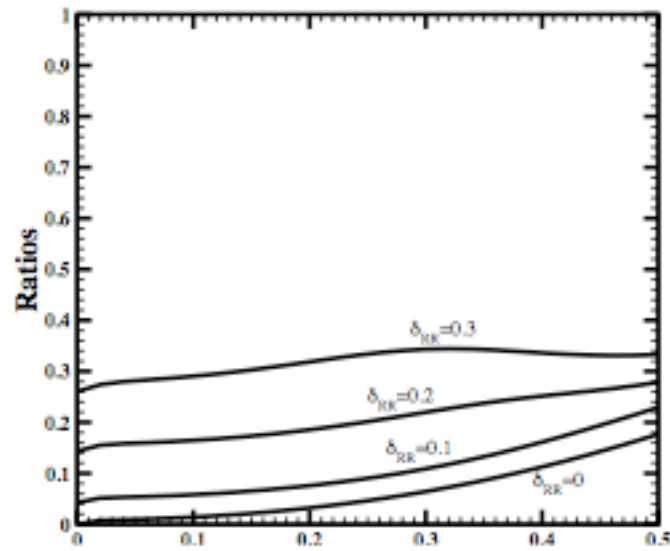
[Hinchliffe, Paige]

## LFV at the LHC

$$\tilde{\chi}_2^0 \rightarrow \tilde{l}_i^+ l_j^- \rightarrow \tilde{\chi}_1^0 l_i^+ l_j^- \quad \tilde{\chi}_2^0 \rightarrow \chi_1^0 Z(h) \rightarrow \tilde{\chi}_1^0 l_i^+ l_i^-$$

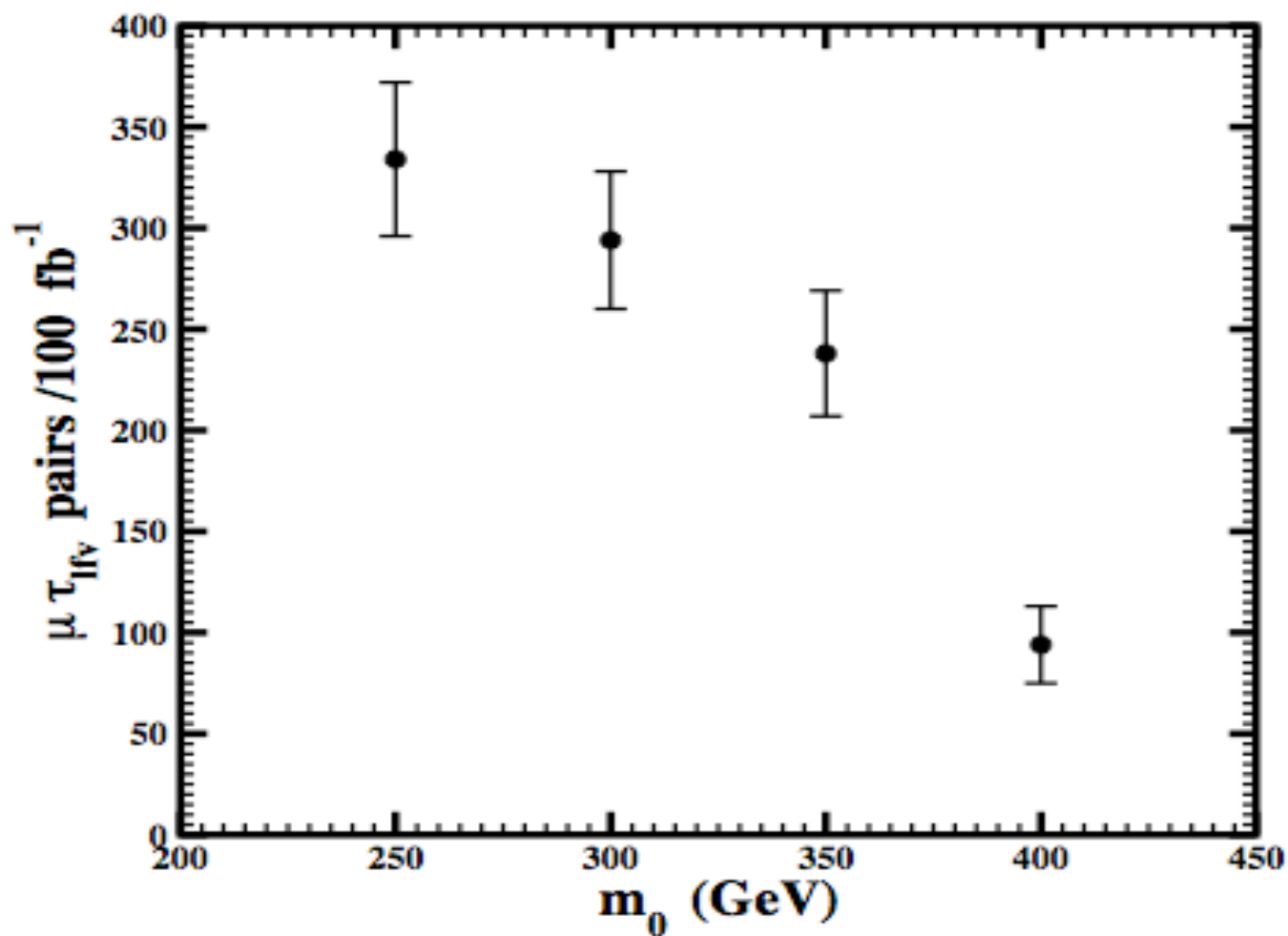


[Ellis, Carvahlo, Gomez, SL, Romao]



[Carquin, Ellis, Gomez, SL, Rodriguez-Quintero]

## Results for Varying $m_0$ at Fixed $M_{1/2}$



## LFV at a LC

$$e^+e^- \rightarrow \tilde{\ell}_i^- \tilde{\ell}_j^+ \rightarrow \tau^\pm \mu^\mp \tilde{\chi}_1^0 \tilde{\chi}_1^0$$

$$e^+e^- \rightarrow \tilde{\nu}_i \tilde{\nu}_j^c \rightarrow \tau^\pm \mu^\mp \tilde{\chi}_1^+ \tilde{\chi}_1^-$$

$$e^+e^- \rightarrow \tilde{\chi}_2^\pm \tilde{\chi}_1^\mp \rightarrow \tau^\pm \mu^\mp \tilde{\chi}_1^+ \tilde{\chi}_1^-$$

$$e^+e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0 \rightarrow \tau^\pm \mu^\mp \tilde{\chi}_1^0 \tilde{\chi}_1^0$$

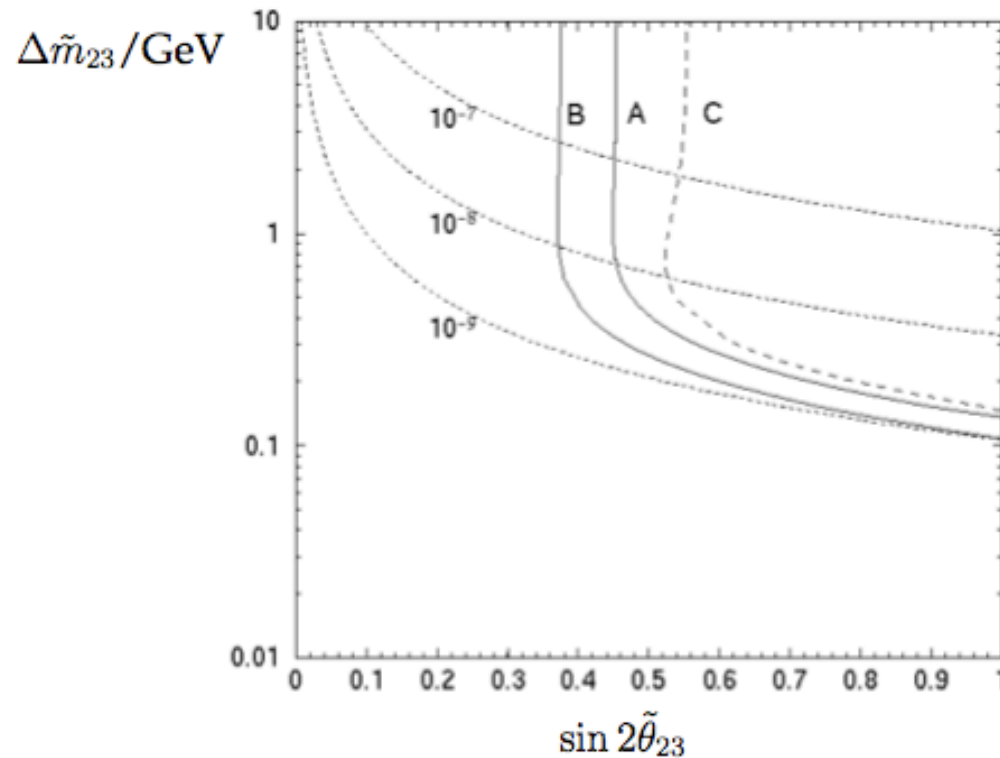


Figure 1: Various  $3\sigma$  significance contours in the  $\Delta \tilde{m}_{23} - \sin 2\tilde{\theta}_{23}$  plane, for the SUSY point mentioned in the text. The contours A and B show the integrated signals (8-9) at  $\sqrt{s} = 500$  GeV and for  $500 \text{ fb}^{-1}$  and  $1000 \text{ fb}^{-1}$ , respectively. The contour C shows the  $\tilde{\nu}\tilde{\nu}^c$  contribution separately for  $500 \text{ fb}^{-1}$  [6]. The dotted lines indicate contours for  $Br(\tau \rightarrow \mu\gamma) = 10^{-7}, 10^{-8}$  and  $10^{-9}$  [11].

[Deppish, Kalinowski, Pas, Redelbach, Ruckl]

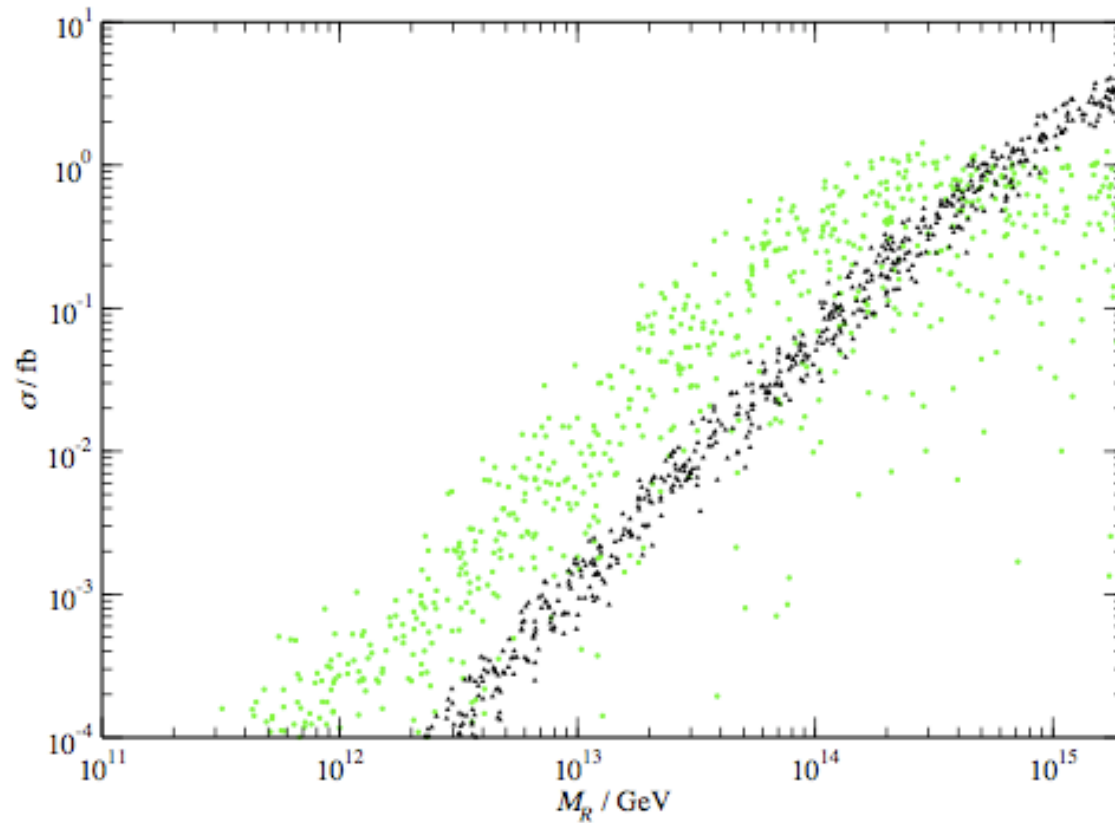


Figure 2: Cross-sections at  $\sqrt{s} = 500$  GeV for  $e^+e^- \rightarrow \mu^+e^- + 2\tilde{\chi}_1^0$  (circles) and  $e^+e^- \rightarrow \tau^+\mu^- + 2\tilde{\chi}_1^0$  (triangles) in scenario B.

Scenario	$m_{1/2}/\text{GeV}$	$m_0/\text{GeV}$	$\tan \beta$	$\tilde{m}_6/\text{GeV}$	$\tilde{\Gamma}_6/\text{GeV}$	$m_{\tilde{\chi}_1^0}/\text{GeV}$
B	250	100	10	208	0.32	98

## CONCLUSIONS

- ✓ Neutrino data point towards SM extensions with LFV
- ✓ LFV strongly bounded by various experimental processes, but there is significant space for LFV physics searches
- ✓ Predictions differ sufficiently enough to give input for Model Building Aspects and sources of LFV
  - Non-universalities versus RGE effects**
  - Minimal versus non-Minimal GUT schemes**
  - R-conserving versus R-violating SUSY**

*A very exciting ERA to come!*