## **R-parity Violation**

*M. Lola Dubna, CALC 2009* 

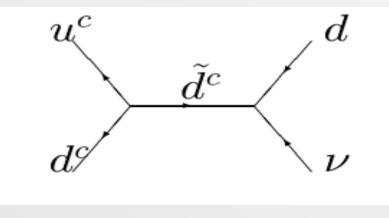
#### WHY R-violating SUSY?

In addition to couplings generating fermion masses,

$$h_{ij}L_iH_1\bar{E}_j$$
  $h'_{ij}Q_iH_1\bar{D}_j$   $h''_{ij}Q_iH_2\bar{U}_j$ 

also 
$$\lambda_{ijk}L_iL_j\bar{E}_k$$
  $\lambda'_{ijk}L_iQ_j\bar{D}_k$   $\lambda''_{ijk}\bar{U}_i\bar{D}_j\bar{D}_k$ 

- The first 2 violate lepton number, the 3<sup>rd</sup> baryon number
- If simultaneously present, unacceptable *p* decay



#### **Structure of R-violating couplings**

•  $L_i L_j \bar{E}_k$ 

[Superfield notation, SU(2) Doublet, Doublet, Singlet] This term gives:  $L_i^- N_j \bar{E}_k$  or  $N_i L_j^- \bar{E}_k$ In component fields: Fermion-Fermion-Scalar Combinations The term  $L_i^- N_j \bar{E}_k$  yields  $\tilde{\ell}_i \nu_j \bar{e}_k$ ,  $\ell_i \tilde{\nu}_j \bar{e}_k$ ,  $\ell_i \nu_j \bar{e}_k$ 

- $L_i Q_j \overline{D}_k$ [Superfield notation, SU(2) Doublet, Doublet, Singlet] Same as  $LL\overline{E}$  with  $L \to Q$ ,  $\overline{E} \to \overline{D}$  $L_i Q_j$ -term gives:  $\ell_i u_j$ -term or  $\nu_i d_j$ -term u-type quarks couple to charged leptons, d-type to neutrinos
  - $\bar{U}_i \bar{D}_j \bar{D}_k$ : [Singlet-Singlet] Simple combination of L-handed anti-quarks (R-handed quarks)

**R-parity:** SM particles: +1, SUSY: -1 Yukawas giving masses to fermions allowed:  $\bar{f}fh_{1,2}$ All other terms forbidden: i.e.  $\tilde{f}_i f_j \bar{f}_k$  Rp versus Rp-violation:

X If R-parity imposed, (SM: +1, SUSY: -1)

forbids all terms with  $\Delta L \neq 0$  and  $\Delta B \neq 0$ 

**LSP: stable**, dark matter candidate Colliders: Missing energy

Can also allow subsets of operators:

Only  $\Delta B \neq 0$  or  $\Delta L \neq 0$ 

( *p*-decay needs both types of terms )

**LSP: unstable** – lose (?) a dark matter candidate Colliders: Multi-lepton/jet events

#### i.e: Flavour-independent Discrete Symmetry ZN (Ibanez, Ross)

SM fields have  $Z_N$  charges:  $(a_Q, a_u, a_d, a_\ell, a_e)$ Higgs charges : such that fermion mass terms are allowed  $a_Q + a_d = a_\ell + a_e$ 

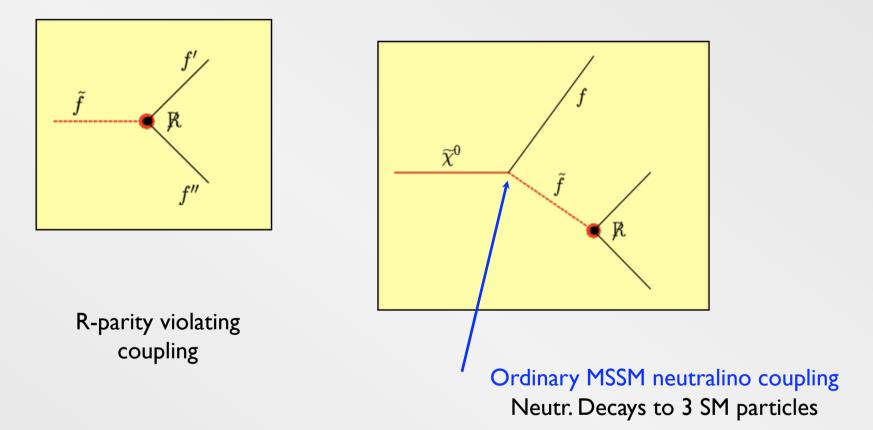
• Then, a symmetry is:  $\underbrace{R\text{-parity}}_{2a_{\ell}+a_{e}} (-) \qquad \underbrace{\text{Bar.par.}}_{2a_{\ell}+a_{e}} (LL\bar{E}, LQ\bar{D}) \qquad \underbrace{\text{Lep.par.}}_{2a_{\ell}+a_{e}} (\bar{U}\bar{D}\bar{D}) \\
 2a_{\ell}+a_{e} \neq 0 \qquad 2a_{\ell}+a_{e} = 0 \qquad 2a_{\ell}+a_{e} \neq 0 \\
 2a_{d}+a_{u} \neq 0 \qquad 2a_{d}+a_{u} \neq 0 \qquad 2a_{d}+a_{u} = 0 \\
 Note: \text{ If } 2a_{\ell}+a_{e} = 0 \text{ then } a_{\ell}+a_{Q}+a_{d} = 0$ 

Can go even further with flavour symmetries:

Experimental bounds (see later) indicate:
 large hierarchies between \$\mathcal{R}\_p\$ operators
 Similar hierarchies observed in fermion masses
 How are the two problems related?

♦ Generation of R-violating terms →
 as for fermion masses through effective terms
 LLĒ (
 LLĒ (
 n, LQD (
 n, ŪDD (
 n)
 As before n depends on charges of L, Ē, Q, Ū, D
 [Ben-Hamo,Binetruy,Bhattacharyya, Dudas, Ellis, Nir,Lavignac,Lola,Ramond,Ross,Savoy,...]

#### R-violating signals: couplings & LSP decays



For a Review, see Barbier et al., hep-ph/0406039 and Refs therein See also Allanach, Dedes & Dreiner, hep-ph/9906209

#### Some of the earliest refs on R-violation

- F. Zwirner, Phys. Lett. B132 (1983) 103
- L. Hall and M. Suzuki, Nucl. Phys. B231 (1984) 419
- J. Ellis et al, Phys. Lett. B150 (1985) 142
- G. Ross and J. Valle, Phys. Lett. B151 (1985) 375
- S. Dawson, Nucl. Phys. B261 (1985) 297
- R. Barbieri and A. Masiero, Nucl. Phys. B267 (1986) 679
- S. Dimopoulos and L.J. Hall, Phys. Lett. B207 (1987) 210
- V. Barger, G.F. Giudice, and T. Han, Phys. Rev. D40 (1989) 2987

#### • Possible Signals

- Pair sparticle productions and R-violating decays
- Single superparticle productions
- Virtual processes
- -Single sparticle productions possible for large Rp
- Otherwise MSSM productions, and Rp decays
  - ♦ (neutral/charged) LSP decay to SM particles for any  $\lambda, \lambda', \lambda'' \ge 10^{-6}$ , decay inside apparatus  $\Rightarrow$

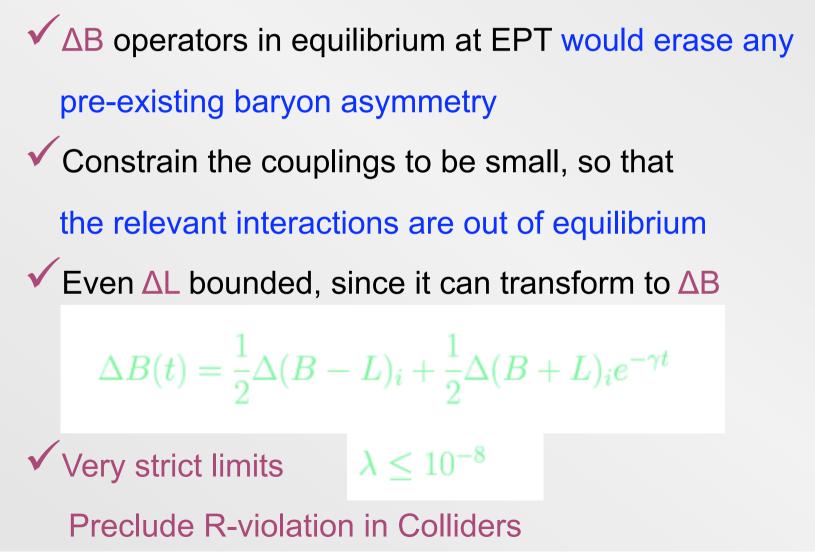
 $\blacklozenge$  Missing energy  $\rightarrow$  multi-lepton/jet signals

otherwise: Standard missing energy signature

 $[h_{top} \approx O(1), h_{up} \approx O(10^{-5})]$ 

### **Cosmology & R-parity violation**

#### Initially thought that:



These constraints can be avoided, in either of the following:

✓ ∆B generated at/below EPT

✓ Rp is spontaneously broken at low Temperature

✓ △L couplings are <u>family-dependent</u>

(then can avoid bounds in given flavour channels)

 $\checkmark$  Early leptogenesis  $\Delta Li - \Delta Lj$  may occur in specific channels

and then may transform to  $\Delta B$ 

#### <u>More dangerous: Flavour-dependent Constraints</u> <u>from modifications of SM processes)</u>

ijk	$\lambda_{ijk}$	Sources	ijk	$\lambda_{ijk}''$	Sources
121	0.05	CC univ.	112	$10^{-6}$	Double nucleon dec.
122	0.05	CC univ.	113	$10^{-4}$	$n-\bar{n}$ osc.
123	0.05	CC univ.	123	1.25	Perturb. unitar.
131	0.06	$\Gamma(\tau \to e \nu \bar{\nu}) / \Gamma(\tau \to \mu \nu \bar{\nu})$	212	1.25	Perturb. unitar.
132	0.06	$\Gamma(\tau \to e \nu \bar{\nu}) / \Gamma(\tau \to \mu \nu \bar{\nu})$	213	1.25	Perturb. unitar.
133	0.003	$\nu_e$ - mass	223	1.25	Perturb. unitar.
231	0.06	$\Gamma(\tau \to e \nu \bar{\nu}) / \Gamma(\tau \to \mu \nu \bar{\nu})$	312	0.50	$R_l$ (LEP1)
232	0.06	$\Gamma(\tau \to e \nu \bar{\nu}) / \Gamma(\tau \to \mu \nu \bar{\nu})$	313	0.50	$R_l$ (LEP1)
233	0.06	$\Gamma(\tau \to e \nu \bar{\nu}) / \Gamma(\tau \to \mu \nu \bar{\nu})$	323	0.50	$R_l$ (LEP1)

Upper limits on  $\lambda$ - and  $\lambda''$ -couplings for  $\tilde{m} = 100$  GeV.

ijk	$\lambda'_{ijk}$	Sources	ijk	$\lambda'_{ijk}$	Sources	ijk	$\lambda'_{ijk}$	Sources
111	0.00035	$(\beta\beta)_{0\nu}$	211	0.09	$R_{\pi}$ ( $\pi$ -dec.)	311	0.10	$\tau^-  ightarrow \pi^- \nu_{\tau}$
112	0.02	CC univ.	212	0.09	$R_{\pi}$ ( $\pi$ -dec.)	312	0.10	$\tau^-  ightarrow \pi^- \nu_{\tau}$
113	0.02	CC univ.	213	0.09	$R_{\pi}$ ( $\pi$ -dec.)	313	0.10	$\tau^-  ightarrow \pi^- \nu_{\tau}$
121	0.035	APV	221	0.18	D-dec.	321	0.20	$D^0 \!\!-\!\! ar{D}^0$
122	0.02	$\nu_e$ -mass	222	0.18	D-dec.	322	0.20	$D^0\!\!-\!\!ar{D}^0$
123	0.20	$D^0 \!\!-\!\! \bar{D}^0$	223	0.18	D-dec.	323	0.20	$D^0\!\!-\!\!ar{D}^0$
131	0.035	APV	231	0.22	$\nu_{\mu}$ DIS.	331	0.48	$R_{\tau}(\text{LEP})$
132	0.34	$R_e$ (LEP)	232	0.36	$R_{\mu}$ (LEP)	332	0.48	$R_{\tau}(\text{LEP})$
133	0.0007	$\nu_e$ -mass	233	0.36	$R_{\mu}$ (LEP)	333	0.48	$R_{\tau}(\text{LEP})$

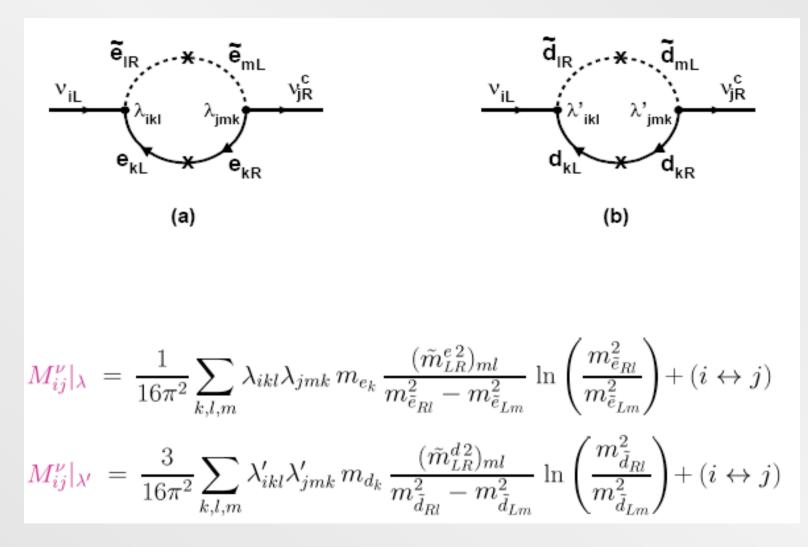
Upper limits on  $\lambda'$ -couplings for  $\tilde{m} = 100$  GeV.

Combinations	Limits	Sources	Combinations	Limits	Sources
$\lambda'_{11k}\lambda''_{11k}$	$10^{-22}$	Proton dec.	$\lambda'_{ijk}\lambda''_{lmn}$	$10^{-10}$	Proton dec.
$\lambda_{1j1}\lambda_{1j2}$	$7.10^{-7}$	$\mu \to 3 e$	$\lambda_{231}\lambda_{131}$	$7.10^{-7}$	$\mu \to 3 e$
Im $\lambda'_{i12}\lambda'^*_{i21}$	$8.10^{-12}$	$\epsilon_K$	$\lambda'_{i12}\lambda'_{i21}$	$1.10^{-9}$	$\Delta m_K$
$\lambda'_{i13}\lambda'_{i31}$	$8.10^{-8}$	$\Delta m_B$	$\lambda'_{1k1}\lambda'_{2k2}$	$8.10^{-7}$	$K_L \rightarrow \mu e$
$\lambda'_{1k1}\lambda'_{2k1}$	$5.10^{-8}$	$\mu {\rm Ti} \to e {\rm Ti}$	$\lambda'_{11j}\lambda'_{21j}$	$5.10^{-8}$	$\mu {\rm Ti} \to e {\rm Ti}$

Upper limits on some important product couplings for  $\tilde{m} = 100$  GeV.

**Neutrinos in R-violating SUSY** 

1-loop neutrino mass contributions:

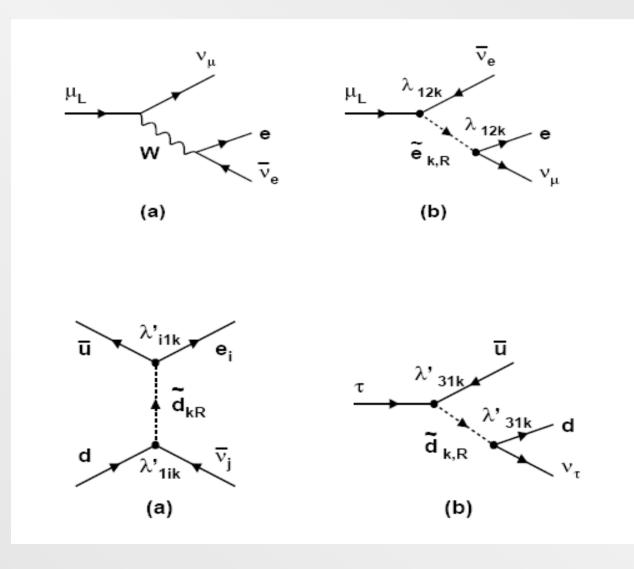


# Constraints on R-violating couplings from massive neutrinos

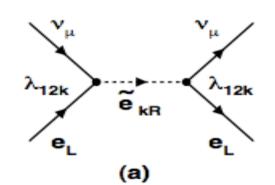
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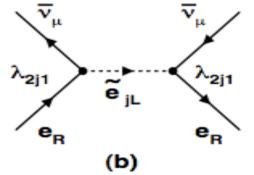
$$\lambda_{133} \leq 9.4 \times 10^{-4} \left(\frac{\langle m_{\nu} \rangle}{0.35 \ eV}\right)^{\frac{1}{2}} \left(\frac{\tilde{m}}{100 \ GeV}\right)^{\frac{1}{2}}$$
$$\lambda_{133}' \leq 2.1 \times 10^{-4} \left(\frac{\langle m_{\nu} \rangle}{0.35 \ eV}\right)^{\frac{1}{2}} \left(\frac{4.5 \ GeV}{m_b}\right) \left(\frac{\tilde{m}}{100 \ GeV}\right)^{\frac{1}{2}}$$

#### Charged Current Universality



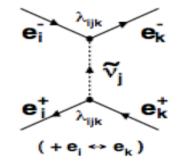
#### **Neutral Current Interactions**

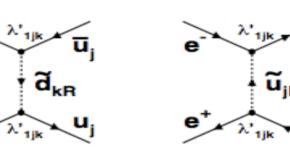


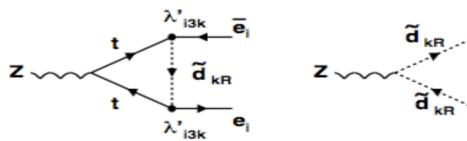


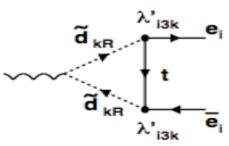
d<sub>k</sub>

d,

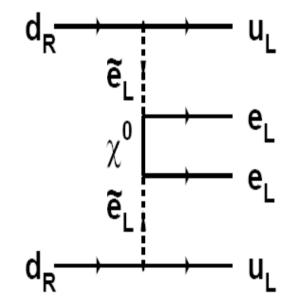


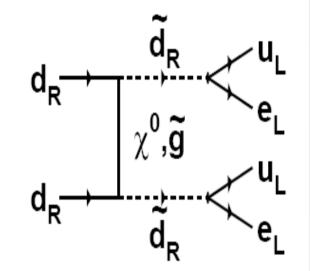




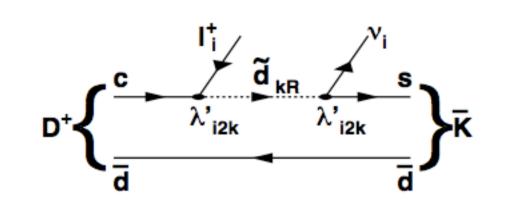


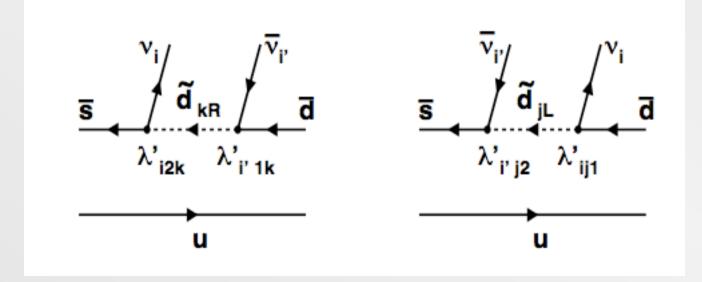
#### Neutrinoless Double Beta Decay



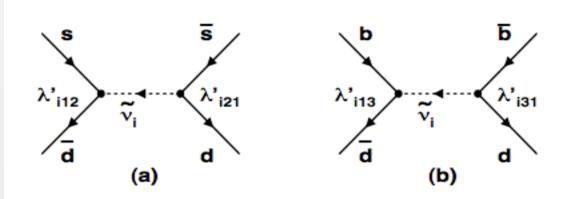


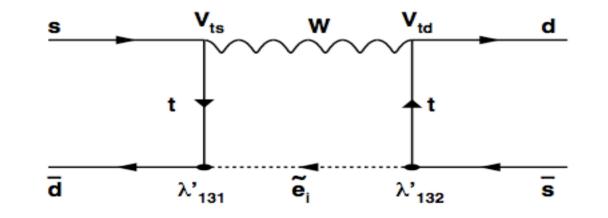
Rare Semi-leptonic decays



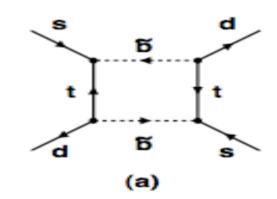


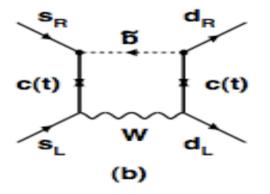
#### Hadron Flavour Changing Processes

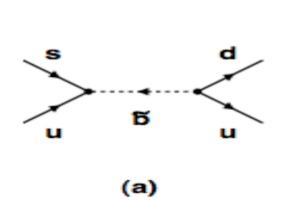


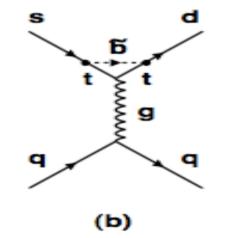


#### Kaon System

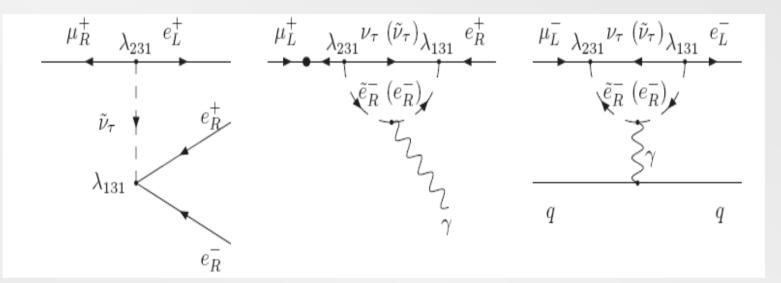








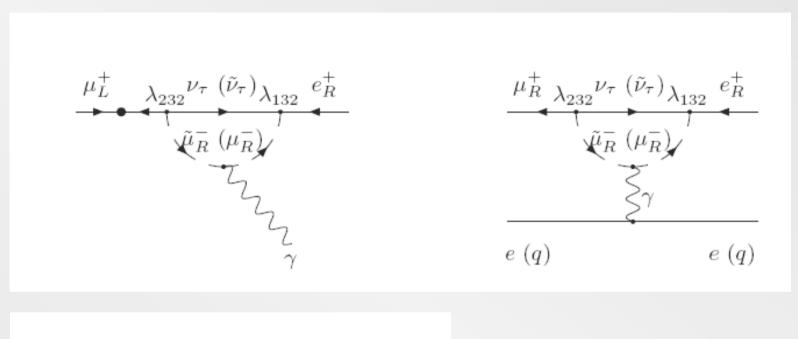
<u>*R-violation:*</u> Correlated Rates depending on coupling combinations (A. de Gouvea, S.L, K. Tobe)



$$\frac{\operatorname{Br}(\mu^+ \to e^+ \gamma)}{\operatorname{Br}(\mu^+ \to e^+ e^- e^+)} = \frac{4 \times 10^{-4} \left(1 - \frac{m_{\tilde{\nu}_{\tau}}^2}{2m_{\tilde{e}_R}^2}\right)^2}{\beta} = 1 \times 10^{-4}$$
$$\frac{\operatorname{R}(\mu^- \to e^- \text{ in Ti (Al)})}{\operatorname{Br}(\mu^+ \to e^+ e^- e^+)} = 2(1) \times 10^{-3}$$

To be compared with **160** and **0.92** in MSSM (where <u>always 1-loop</u>: on shell photon penguin dominates)

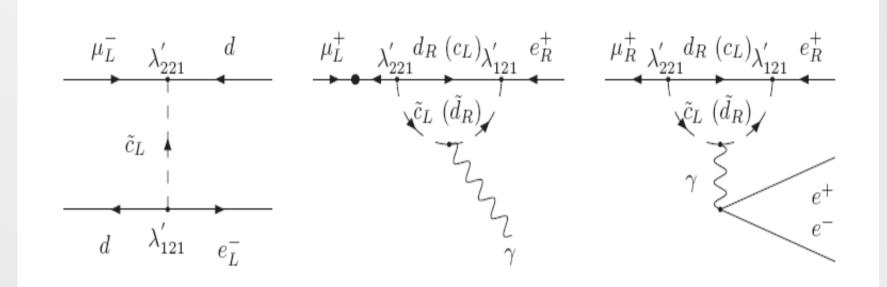
#### For all processes at loop level:



$$\frac{\operatorname{Br}(\mu^+ \to e^+ \gamma)}{\operatorname{Br}(\mu^+ \to e^+ e^- e^+)} = 1.2$$

$$\frac{\mathbf{R}(\mu^- \to e^- \text{ in Ti (Al)})}{\mathbf{Br}(\mu^+ \to e^+ e^- e^+)} = 18$$

For:



$$\begin{array}{rcl} \frac{{\rm Br}(\mu^+ \to e^+ \gamma)}{{\rm Br}(\mu^+ \to e^+ e^- e^+)} &=& 1.1, \\ \\ \frac{{\rm R}(\mu^- \to e^- \mbox{ in Ti} \mbox{ (Al)})}{{\rm Br}(\mu^+ \to e^+ e^- e^+)} &=& 2 \ (1) \times 10^5 \end{array}$$

	$Br(\mu \rightarrow e\gamma)$	$R(\mu \rightarrow e \text{ in } Ti)$
	$\frac{\mathrm{Br}(\mu \to 3e)}{\mathrm{Br}(\mu \to 3e)}$	$\frac{\operatorname{IC}(\mu \to 3e)}{\operatorname{Br}(\mu \to 3e)}$
Case $(1)$		
$\lambda_{131}\lambda_{231}$	$1 \times 10^{-4}$	$2 \times 10^{-3}$
$\lambda_{121}\lambda_{122}$	$8 \times 10^{-4}$	$7 \times 10^{-3}$
$\lambda_{131}\lambda_{132}$	$8  imes 10^{-4}$	$5  imes 10^{-3}$
Case $(2)$		
$\lambda_{132}\lambda_{232}$	1.2	18
$\lambda_{133}\lambda_{233}$	3.7	18
$\lambda_{231}\lambda_{232}$	3.6	18
$\lambda'_{122}\lambda'_{222}$	1.4	18
$\lambda'_{123}\lambda'_{223}$	2.2	18
Case $(3)$		
$\lambda'_{111}\lambda'_{211}$	0.4	$3 imes 10^2$
$\lambda'_{112}\lambda'_{212}$	0.5	$8  imes 10^4$
$\lambda'_{113}\lambda'_{213}$	0.7	$1 imes 10^5$
$\lambda'_{121}\lambda'_{221}$	1.1	$2  imes 10^5$
MSSM with $\nu_R$	$1.6 imes10^2$	0.92

Distinct differences in LFV predictions between

(i) MSSM & R-violation

(ii) different combinations of (dominant) R-violating couplings

#### **Collider search Strategies....**

For  $\Delta L$ , look for:

Modifications to SM Processes or Exotic Events

(like  $\Delta Li$ , novel final state topologies,

isolated leptons in jet backgrounds without missing Energy)

More detailed analysis (sophisticated jet clustering algorithms) required for detecting  $\Delta B$  operators *(Butterworth,Ellis, Raklev, Salam)* 

 $\frac{...keeping in mind the constraints}{Fermion mixing \Rightarrow mixing of different operators}$  $\Rightarrow Correlations of experimental bounds$ that depend on flavour charges

An example:  $L_1Q_2\overline{D}_1$  cannot be very large

- If  $V_{CKM}(1,2)$  arises from down sector: bounds from  $K \to \pi \nu \bar{\nu}$
- If  $V_{CMK}(1,2)$  arises from up sector: bounds from neutrinoless double beta decay

...and even more constraints in given models

Strong constraints on products of couplings ie:

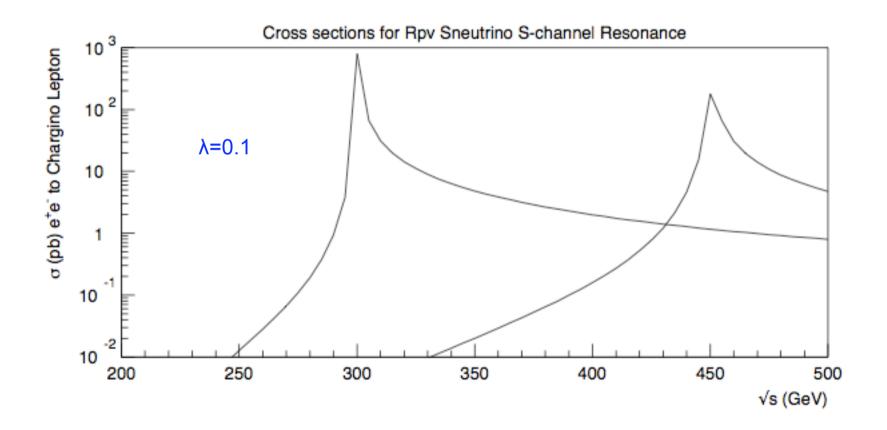
 $\lambda'_{i13}\lambda'_{i31} \leq 3.2 \cdot 10^{-7}$  $\lambda'_{i12}\lambda'_{i21} \leq 4 \cdot 10^{-9}$ 

(+) Symmetric quark matrices  $\Rightarrow$ 

 $\lambda_{i13}' \le 6 \cdot 10^{-4}$  $\lambda_{i12}' \le 6 \cdot 10^{-5}$ 

(also for couplings with  $j \leftrightarrow k$ )

$$\begin{split} \underline{Single \ sleptons \ at \ e+e-\ Colliders\ }(Dreiner,SL) \\ e^+e^- &\to (\tilde{\nu})^* \to f\bar{f}' \quad \text{and} \quad e^+e^- \to (\tilde{\nu})^* \to \begin{cases} \ell_i^{\pm} \tilde{\chi}^{\mp} \\ \nu_i \tilde{\chi}^0 \\ \nu_i \tilde{\chi}^0 \\ \end{bmatrix} \\ &\to \quad \frac{8\pi}{m_{\tilde{\nu}}^2} B(\tilde{\nu} \to f\bar{f}) B(\tilde{\nu} \to \nu \tilde{\chi}^0) \text{, as } s \to m_{\tilde{\nu}}^2 \end{split}$$



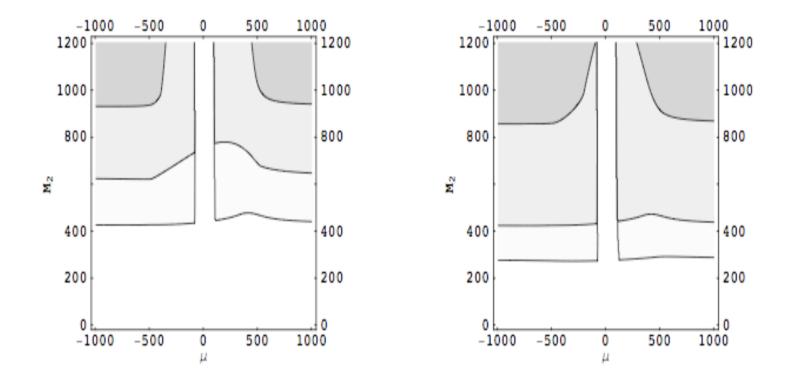
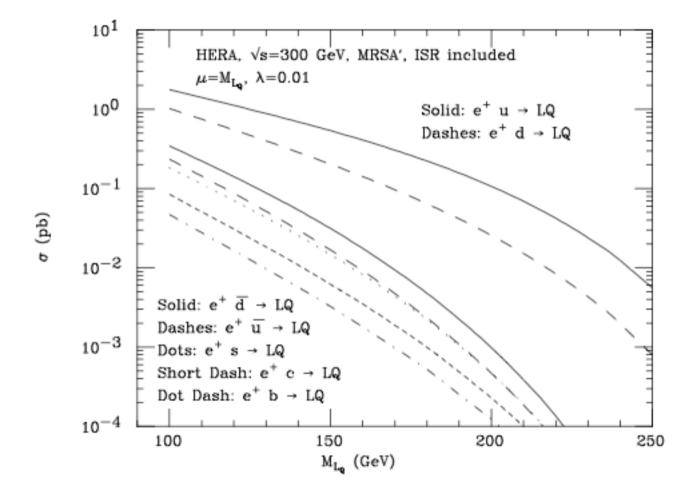


Figure 2:  $\mathcal{B}$  for  $\tilde{\nu}$  decay to fermions for parameters most relevant for LC. We present contours for  $\mathcal{B} \geq 0.9, 0.3, 0.1$ , from the darker to the lighter areas respectively. We choose  $\tan\beta = 2.0, m_{\tilde{\nu}} = 500 \text{ GeV}$  and  $\lambda = 0.1$  (left) and 0.2 (right). The LEP 2 bound on charginos has been implemented.

#### Single Leptoquark / squark productions at HERA (Altarelli, Ellis, Guidice, SL, Mangano)

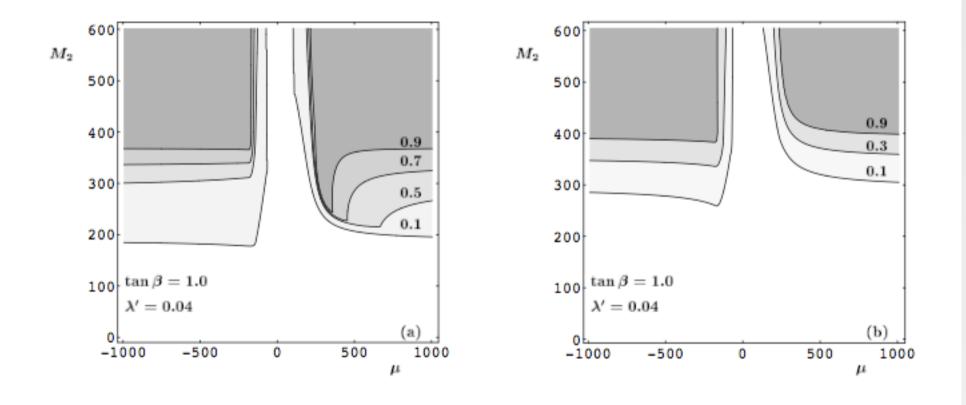


#### Cancellation effects in LH - squark decays (Altarelli, Ellis, Guidice, SL, Mangano)

$$\Gamma( ilde{c}_L
ightarrow e^+d)=rac{1}{16\pi}(\lambda_{121}')^2m_{ ilde{c}_L}$$

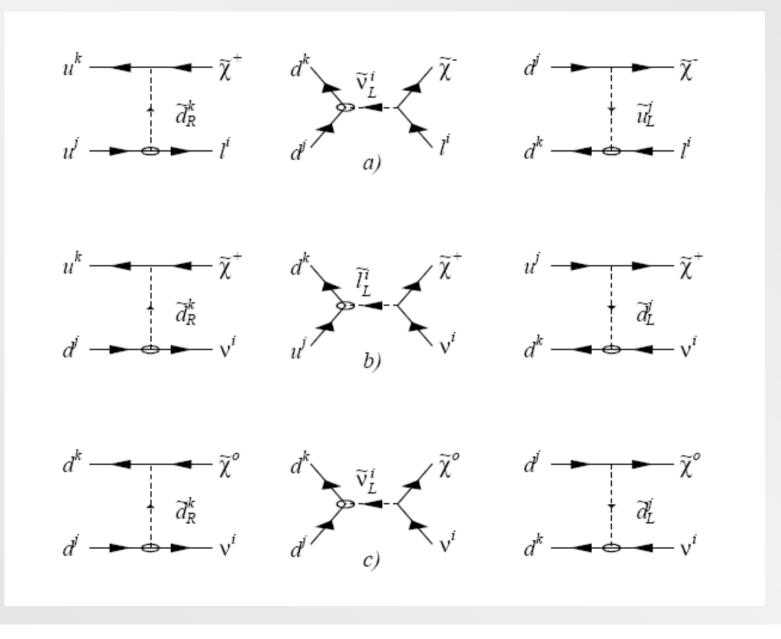
$$egin{aligned} &\Gamma( ilde{c}_L o c \chi^0_i) = rac{g^2}{32\pi} (A_i^2 + B_i^2) \ m_{ ilde{c}_L} \left( 1 - rac{m_{\chi^0_i}^2}{m_{ ilde{c}_L}^2} 
ight)^2 \ &A_i = rac{m_c N_{i4}}{M_W \sin eta}, \ B_i = N_{i2} + rac{1}{3} an heta_W N_{i1} \ . \end{aligned}$$

#### i.e. LH-squark (left) versus sneutrino decays (right)

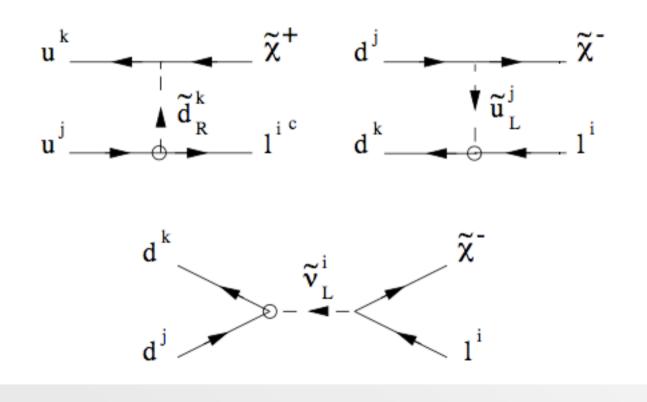


<u>Due to cancellations, larger area where</u> <u>Rp-violating decay of squarks to fermions dominates</u>

#### i.e.Single Superparticle Productions at Hadron Colliders



#### <u>Single Charginos at Tevatron</u> (Chemtob, Moreau, Deliot, Royon, Perez)



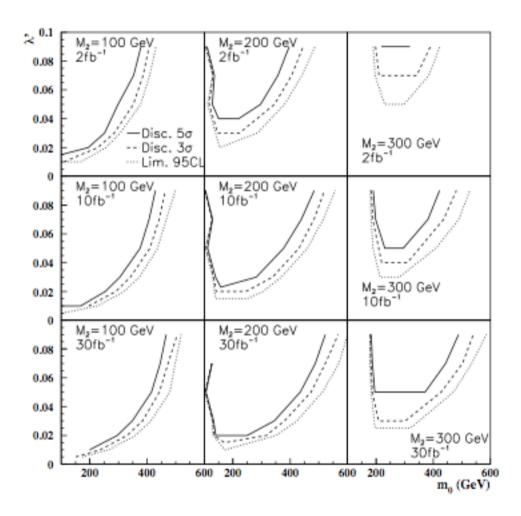
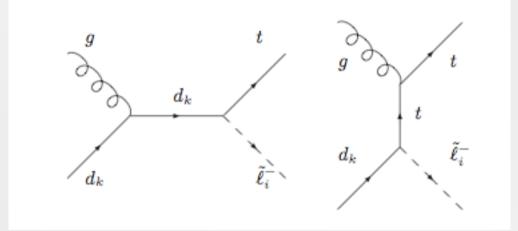
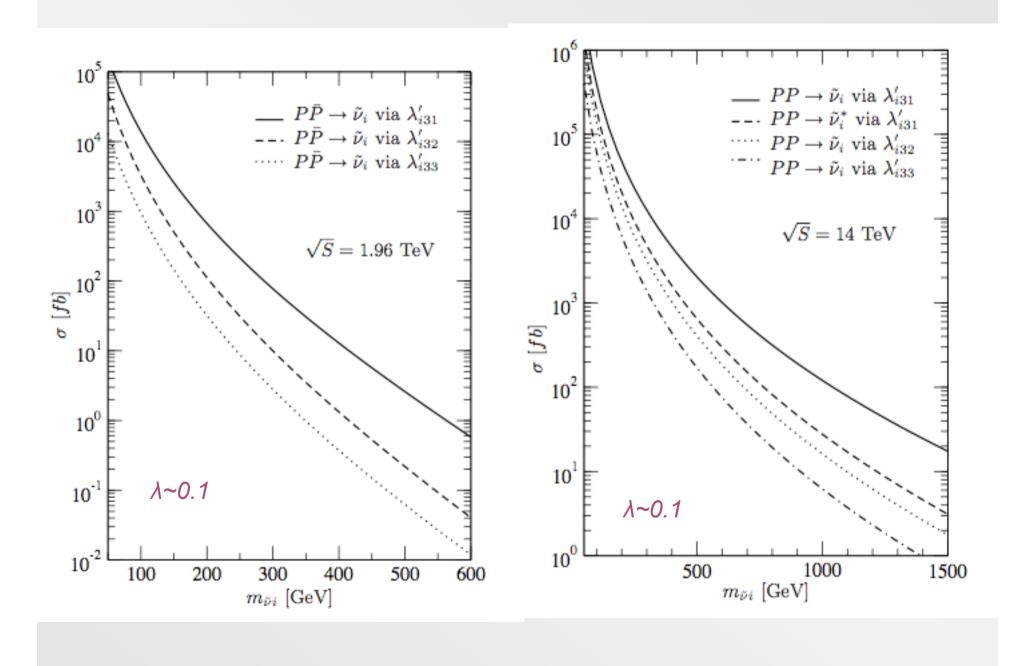


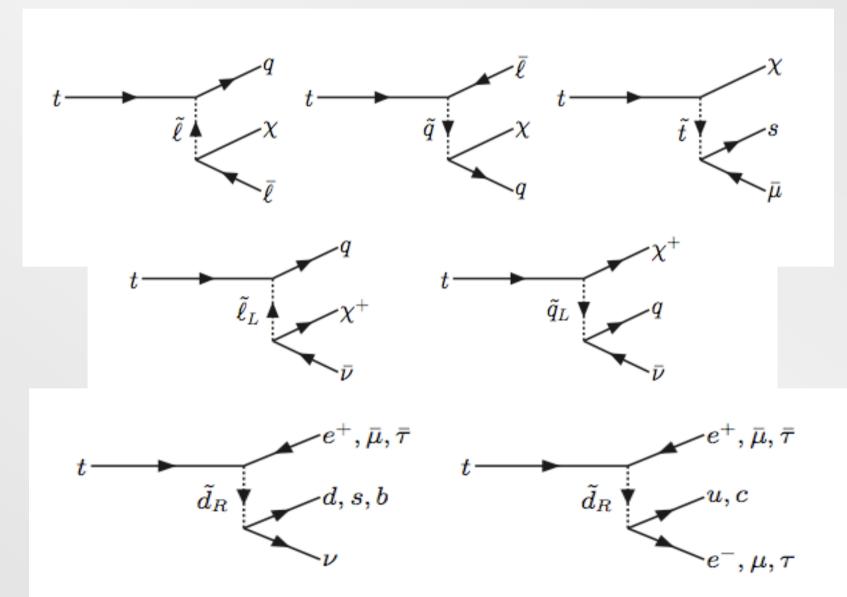
FIG. 2. Discovery contours at  $5\sigma$  (full line),  $3\sigma$  (dashed line) and limit at 95% *C.L.* (dotted line) presented in the plane  $\lambda'_{211}$  versus the  $m_0$  parameter, for different values of  $M_2$  and of luminosity.

### Single top-slepton production (Bernhard, Dreiner, Grab, Richardson)

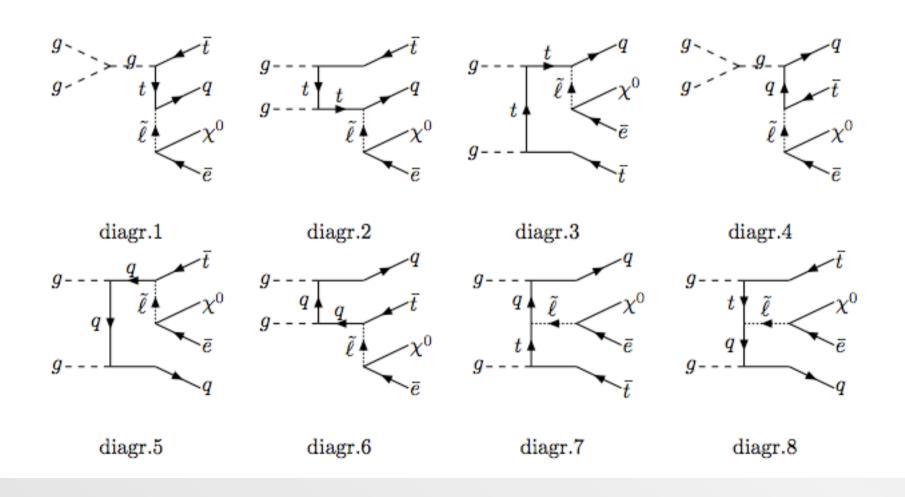


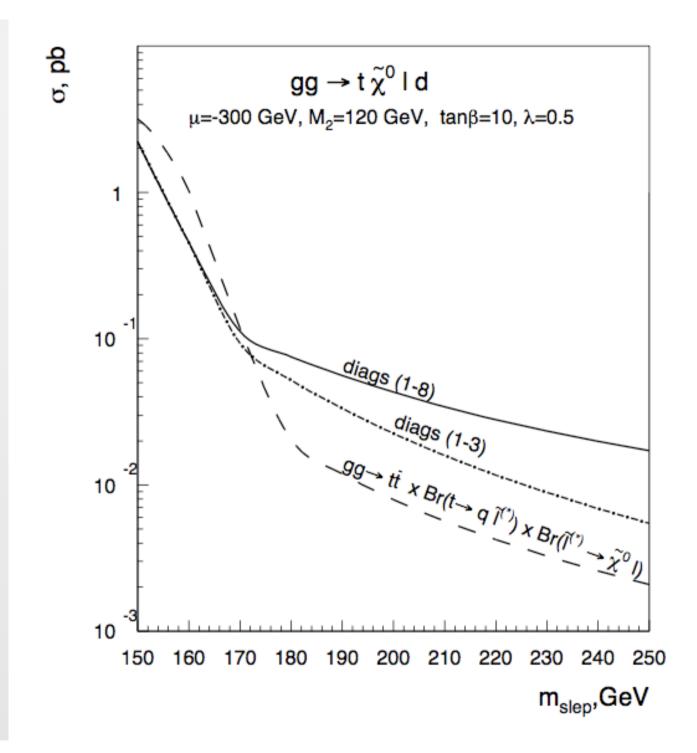




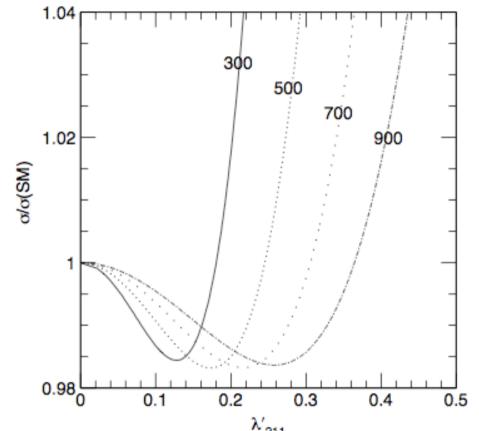


(Belyaev, Genest, Leroy, Mehdiyev)





### <u>Effects in Dilepton productions at LHC</u> (Choudhury, Godbole, Polesello)



**Figure 1:** Relative change of the dimuon  $\overset{\lambda'_{211}}{cross}$  section at the LHC as function of the coupling  $\lambda'_{211}$ . The assumed lower limit on the dilepton invariant mass is 500 GeV. The curves correspond to four different squark masses: 300, 500, 700 and 900 GeV respectively.

# **SUSY Dark Matter if R-parity is violated?**

In the MSSM, stable LSP a very good DM candidate In R-violation, LSP unstable. Is all hope for SUSY DM lost?

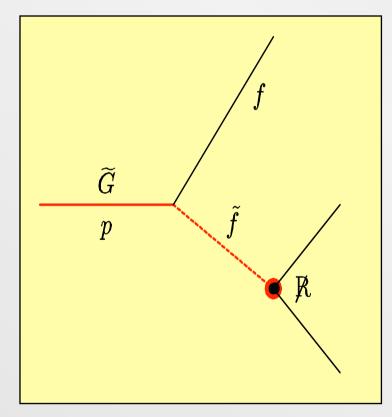
-If LSP a gravitino, its decays very suppressed by Mp -The lighter the gravitino, the longer the lifetime

Questions: (i)*can gravitinos be DM even with broken R-parity?* (*ii*) *Can we hope for* **BOTH** *DM,* **AND** *detectable R-violation in colliders?* 

Answer: depends on how gravitinos decay under R-violation

## <u>3-body trilinear R-violating decays</u>

### Chemtob, Moreau

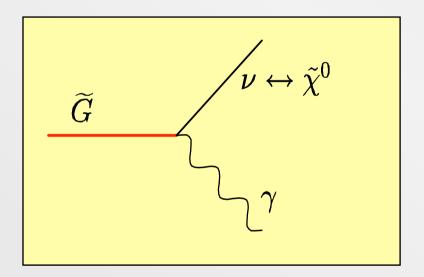


#### Suppressed by:

Gravitino vertex (~1/Mp)
Phase space / fermion masses
(for light gravitino and heavy fermions)

## **2-body bi-linear R-violating decays**

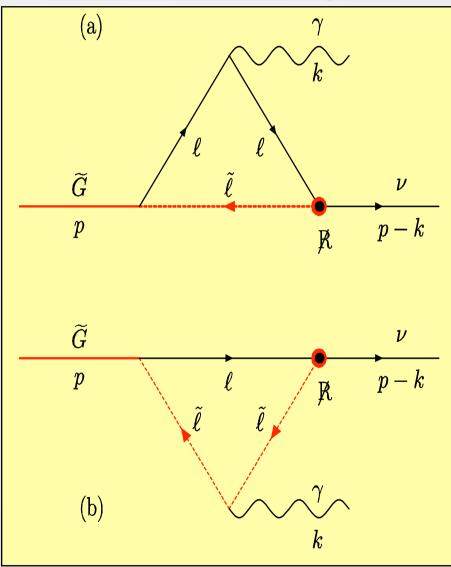
Takayama, Yamaguchi Buchmuler et al.

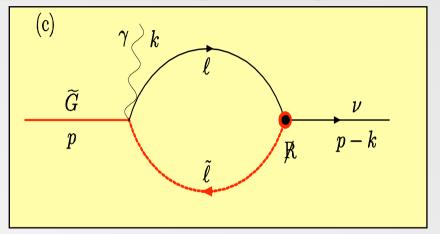


Suppressed by:

Gravitino vertex (~1/Mp)
Neutralino-neutrino mixing (model dependent)

# Radiative 2-body trilinear R-violating decays





#### Suppressed by:

- Gravitino vertex (~1/Mp)
- Loop factors (~ fermion mass)

### **Radiative decays dominate for:**

- Smaller gravitino masses
- R and L violation via operators of the 3<sup>rd</sup> generation
- Small neutrino-neutralino mixing

Large gravitino lifetime (can be DM), due to:

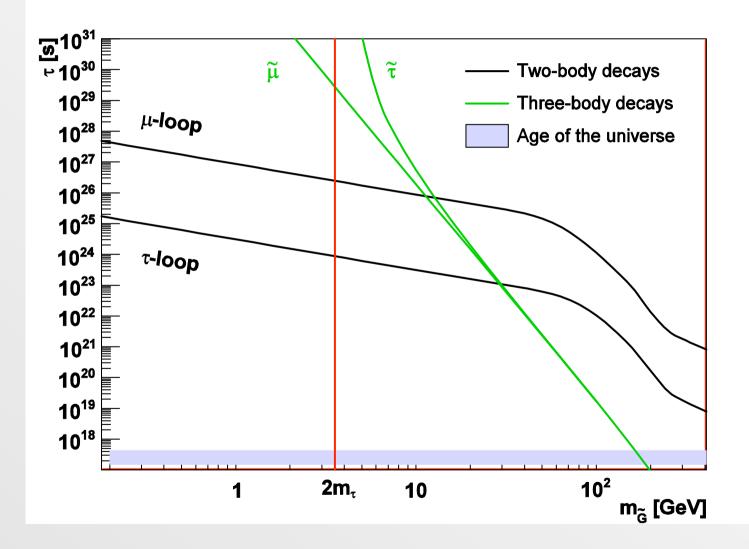
Gravitational suppression of its couplings

Smallness of R-violating vertices

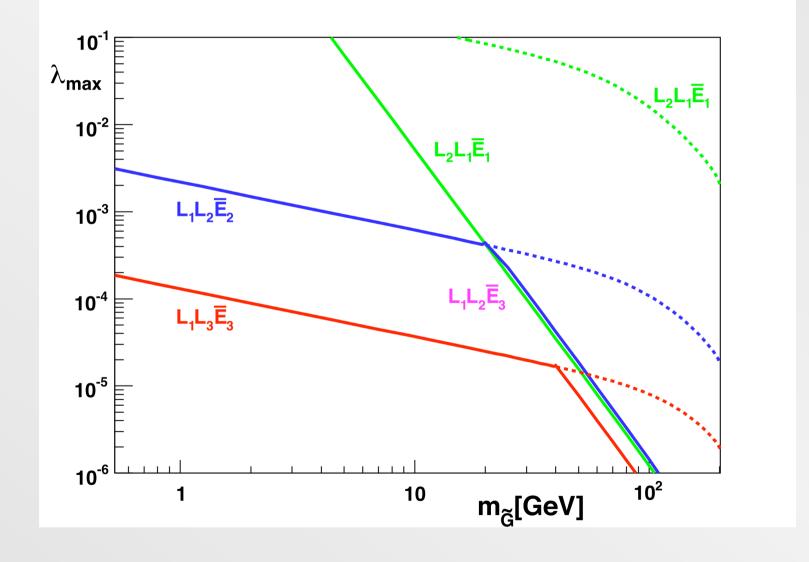
Loop, phase space, or mixing effects

 $\overline{U}_{3}\overline{D}_{j}\overline{D}_{k}$  *Maximum stability* (neither radiative nor tree-level decays)!

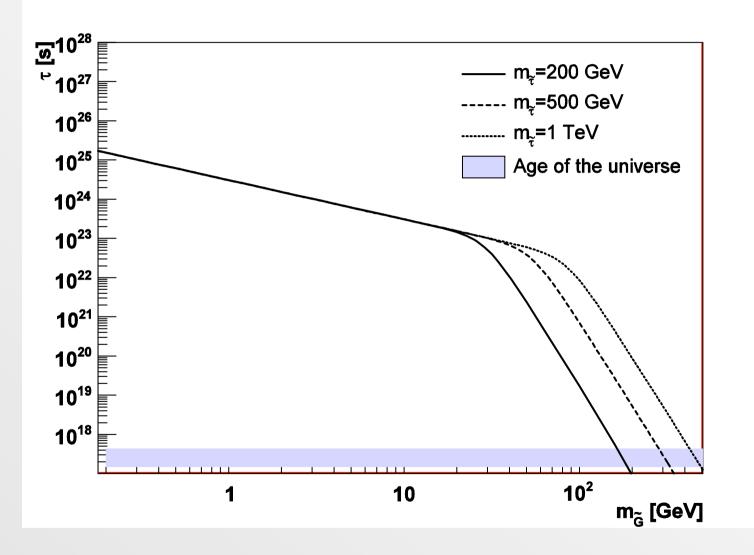
# Radiative versus 3-body decays



## **Constraints from DM & Photon Spectra**



### Lifetime versus SUSY masses



### **NLSP decays**

NLSP	$LLar{E}$	$LQ\bar{D}$	$\bar{U}\bar{D}\bar{D}$
$\chi^0$	$\ell_i^{\pm}\ell_j^{\mp} u$	$q_j ar q_k \ell^\pm (q_j ar q_k  u)$	$q_i q_j q_k (ar q_i ar q_j ar q_k)$
$\tilde{\nu}$	$\ell_i^{\pm}\ell_j^{\mp}$	$q_j \overline{q}_k$	
	$\ell_i^{\pm}\ell_j^{\mp}\nu u$	$q_j ar q_k \ell^\pm  u(q_j ar q_k  u  u)$	$ u q_i q_j q_k ( u ar q_i ar q_j ar q_k)$
$ au_R$	$\ell_i \nu$	$q_j \overline{q}_k$	
	$\ell_i^{\pm}\ell_j^{\mp} u au$	$q_j \bar{q}_k \ell^{\pm} \tau(q_j \bar{q}_k  u  au)$	$ au q_i q_j q_k ( au ar q_i ar q_j ar q_k)$

- No source of suppression other than R-violating couplings
- Decay well before BBN compatible with gravitino DM

# <u>Conclusions</u>

R-violating SUSY equally motivated with MSSM Interesting signals but also strong bounds ✓ Possible to have both gravitino DM AND observable R-violation in colliders Distinct differences in LFV predictions between SM and SUSY, but also between MSSM & R-violation Results sensitive to flavour structure of R-violating operators Through Collider Searches ALSO probe Flavour Structure of Fundamental Theory