

Dark Matter motivated SUSY collider signatures

Alexander Belyaev

Southampton University & Rutherford Appleton LAB



Helmholtz International School - Workshop
Calculations for Modern and Future Colliders

July 10 - 20, 2009, Dubna, Russia

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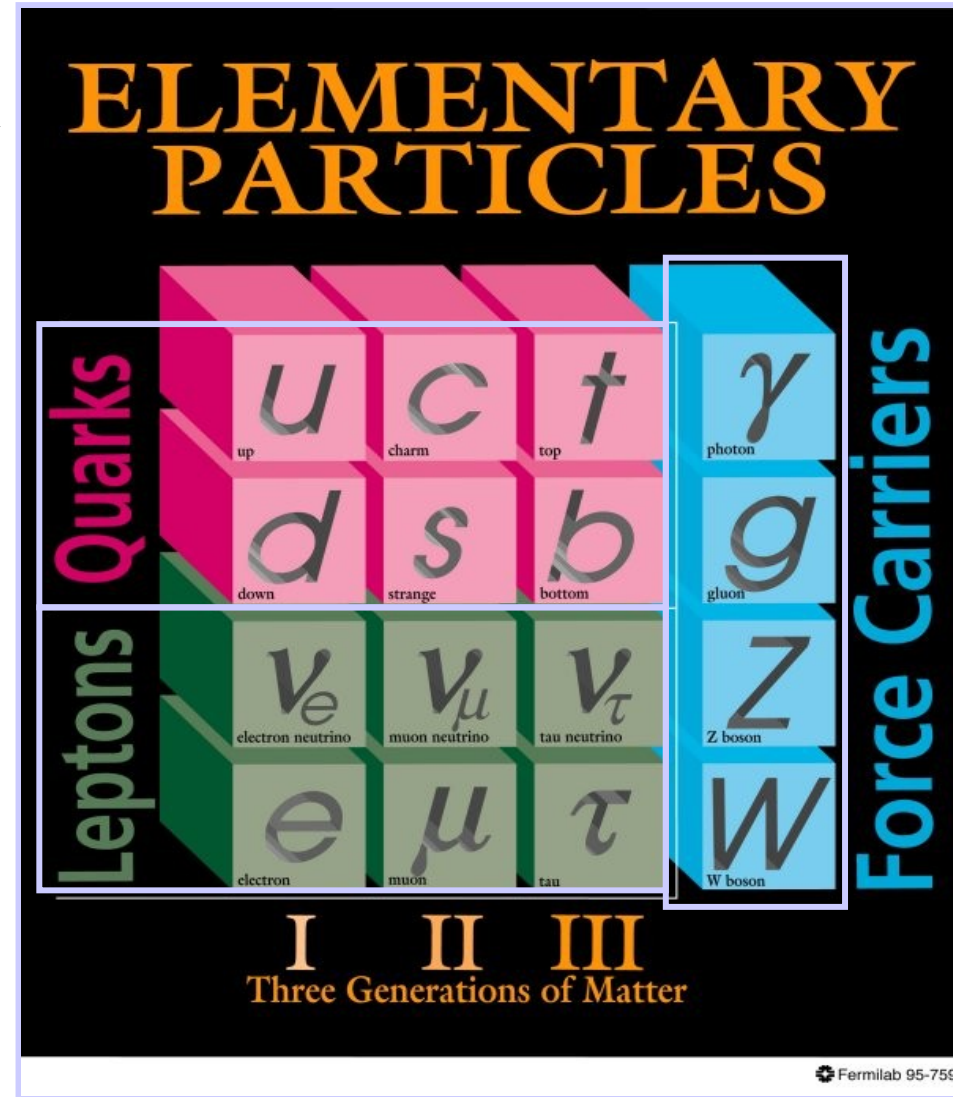
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OUTLINE

- SUSY as one of the best candidate for underlying theory
- Viable Supersymmetric models
 - ➔ *minimal Supergravity model as an example (mSUGRA)*
 - ➔ *theoretical and experimental constraints*
 - ➔ *problems of mSUGRA and motivation for non-universal models*
- Conclusions

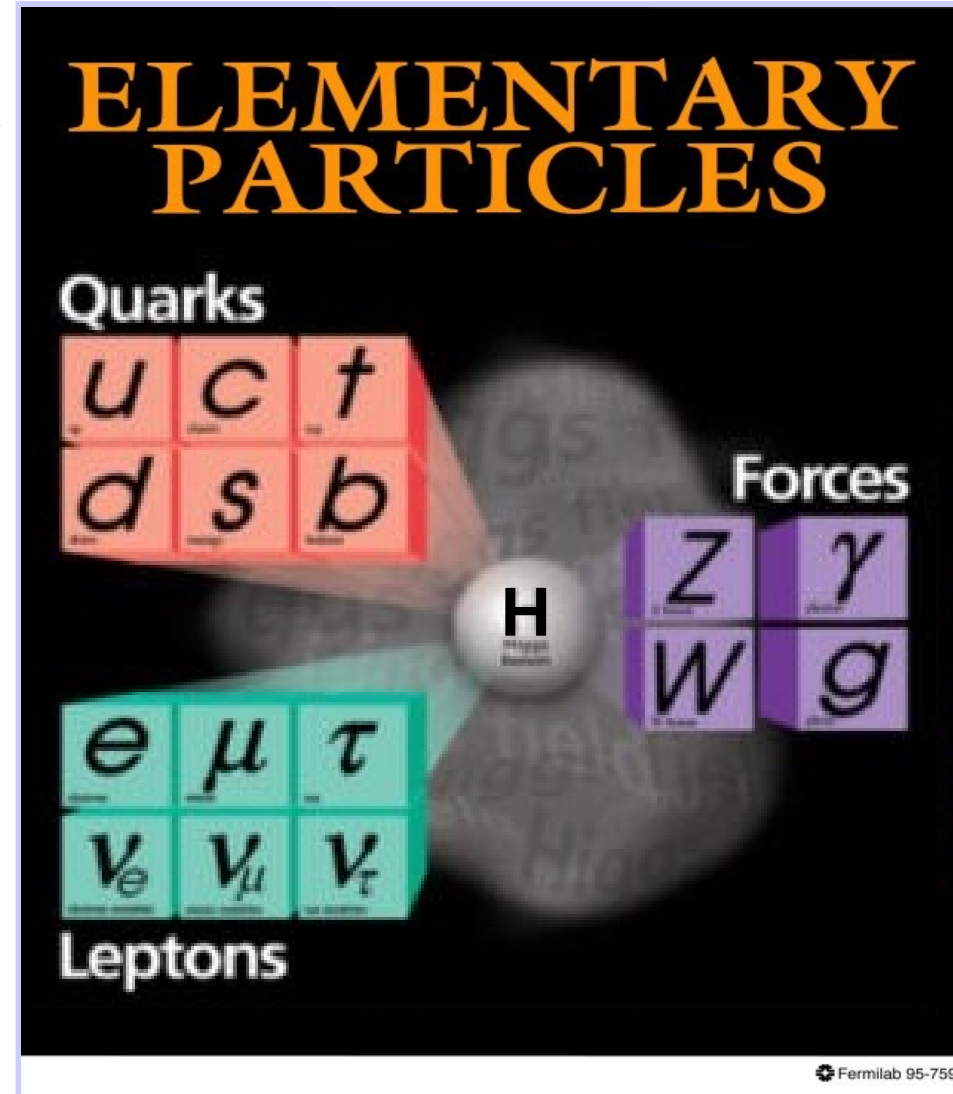
The present status of the SM

- Based on $SU(3) \times SU(2)_L \times U(1)_Y$ gauge symmetry spontaneously broken down to $SU(3) \times U(1)_e$:
- Matter: 3 generations of quarks and leptons



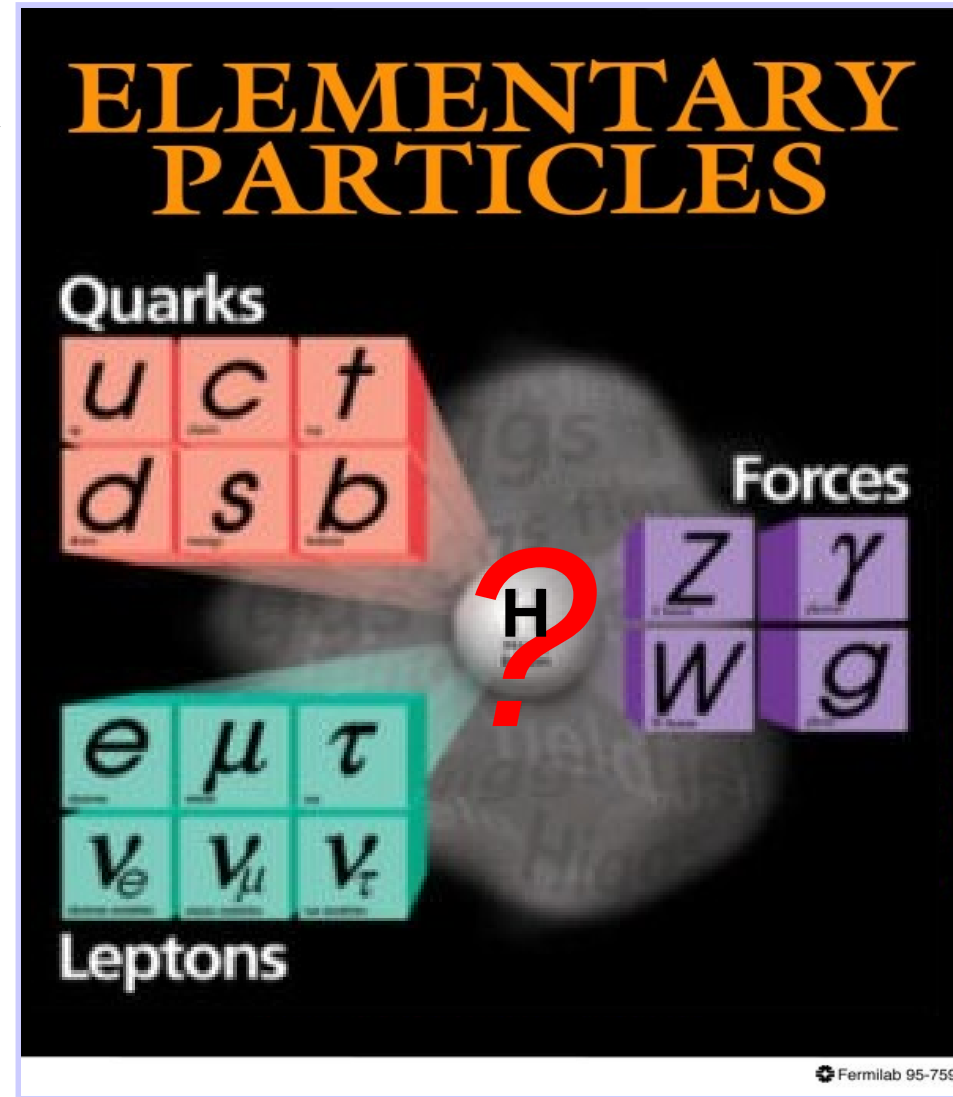
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- Matter: 3 generations of quarks and leptons
- One of the central role is played by Higgs field
 - ➔ *one higgs doublet, interacts with all fields*
 - ➔ *develops condensate*
 - ➔ *W,Z bosons, lepton and quarks and Higgs field itself acquires mass*



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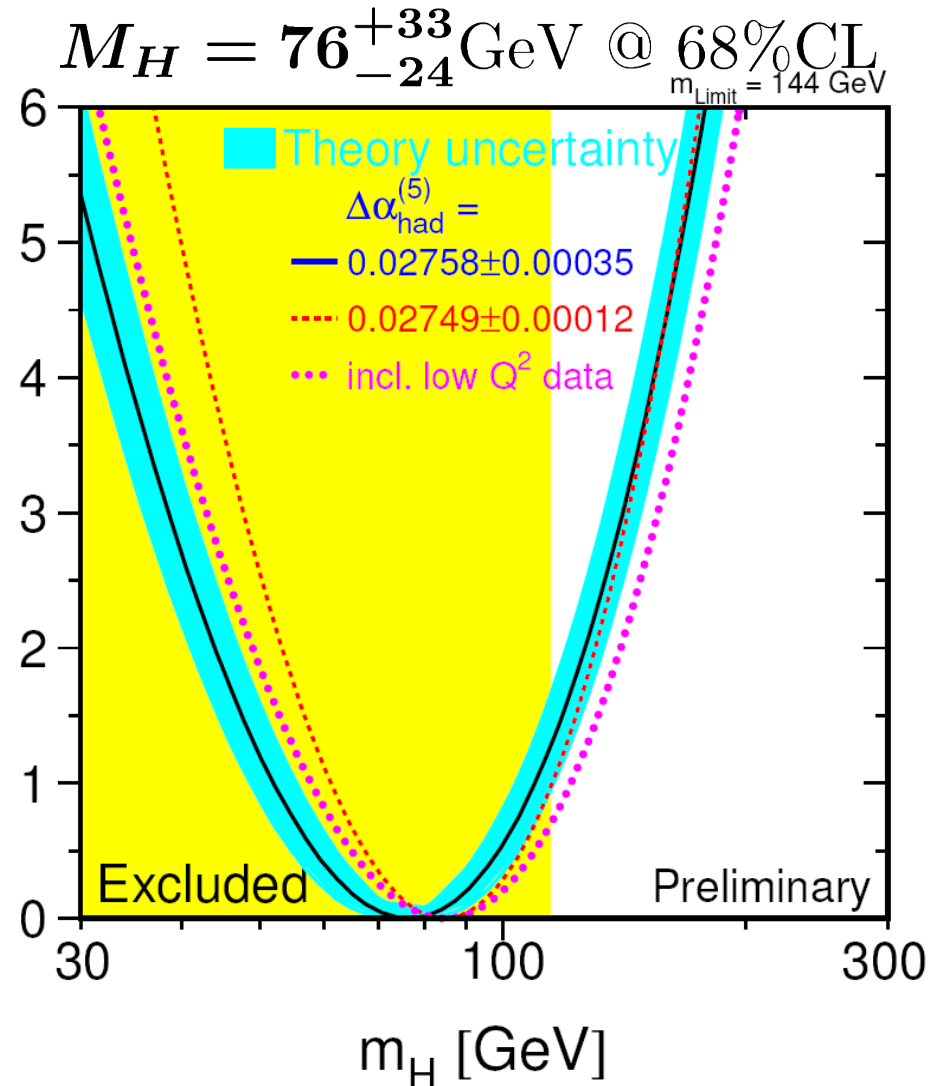
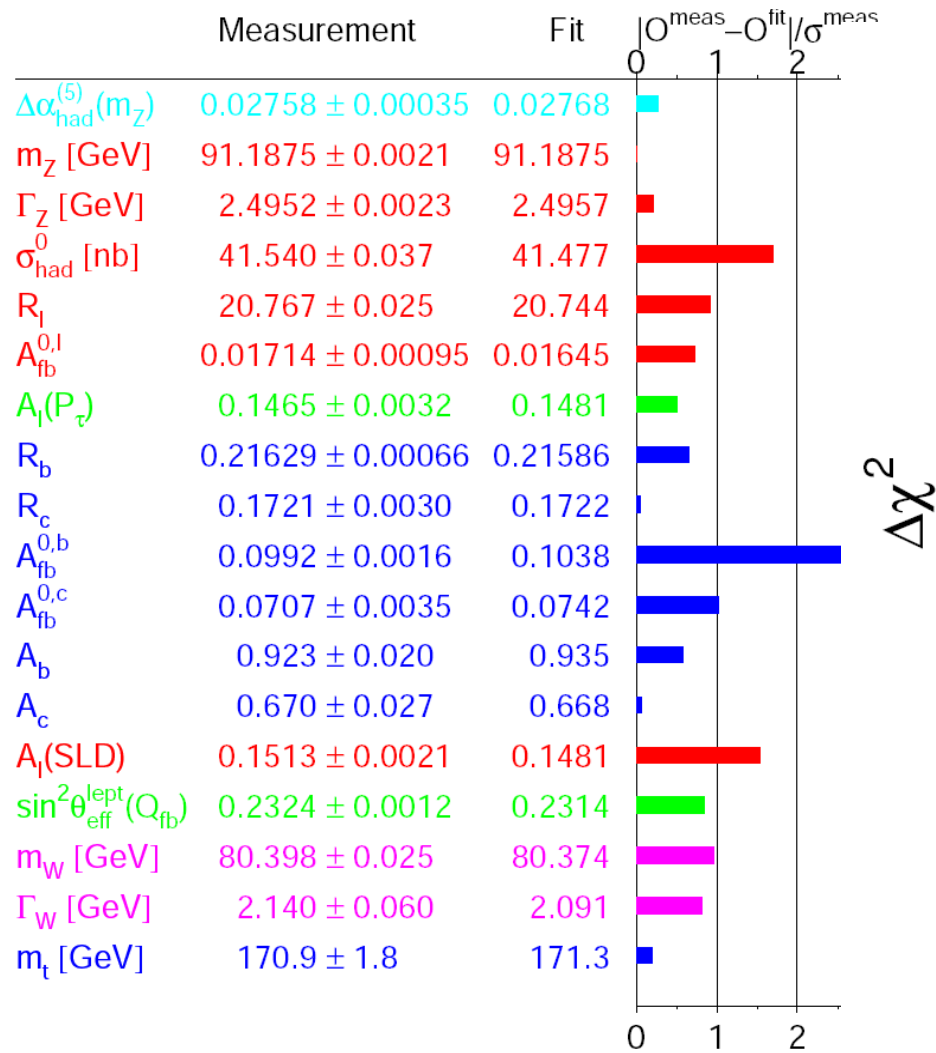
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Higgs boson is not found yet and is the most wanted particle!
The present Higgs mass limit is $M_H > 114.4$ GeV from LEP2

The present status of the SM

SM describes perfectly almost all data ...



EW Precision fits <http://lepewwg.web.cern.ch/LEPEWWG/>

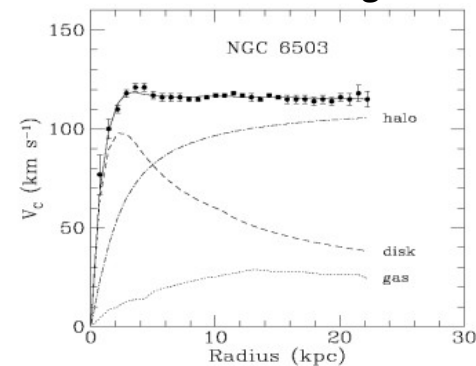
Open questions

SM describes perfectly almost all data ... but has serious problems

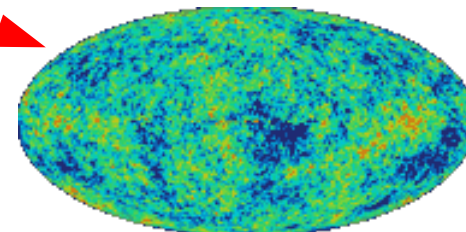
- **Experimental problems**

- **Evidence for Dark Energy & Dark Matter**
- **matter – anti-matter asymmetry: baryogenesis problem**
- **the origin of EWSB is unknown**
Higgs boson is not found yet ...

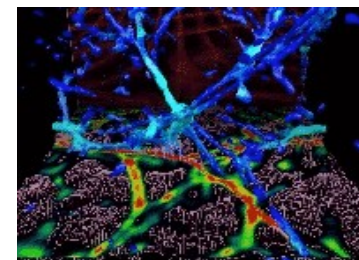
Rotation curves of galaxies



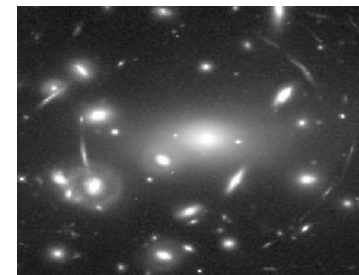
CMB



Large Scale Structure



Lensing



Open questions

SM describes perfectly almost all data ... but has serious problems

- **Experimental problems**

- ➔ Evidence for Dark Energy & Dark Matter
- ➔ matter – anti-matter asymmetry: **baryogenesis problem**
- ➔ the origin of EWSB is unknown
Higgs boson is not found yet ...

- **Theoretical problems**

- ➔ the problem of large quantum corrections: **fine-tuning problem**
- ➔ at very high energy forces **start to behave similar** due to effect of different 'running' of coupling constants for abelian and non-abelian fields. But **unification is not exact!**
- ➔ **gravity stays apart – not included into SM**

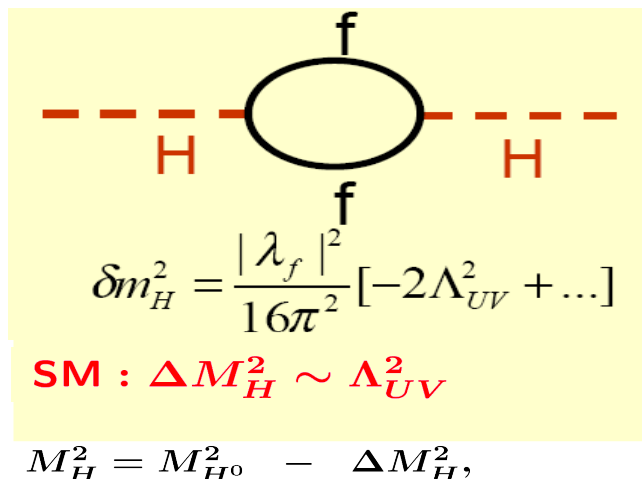
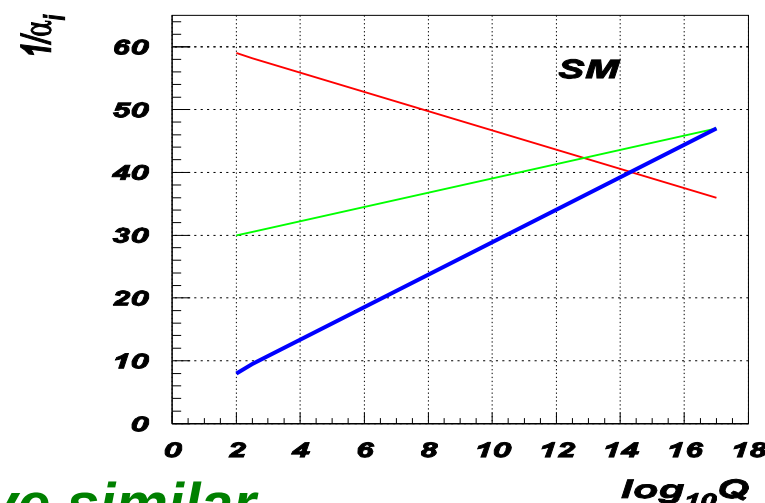


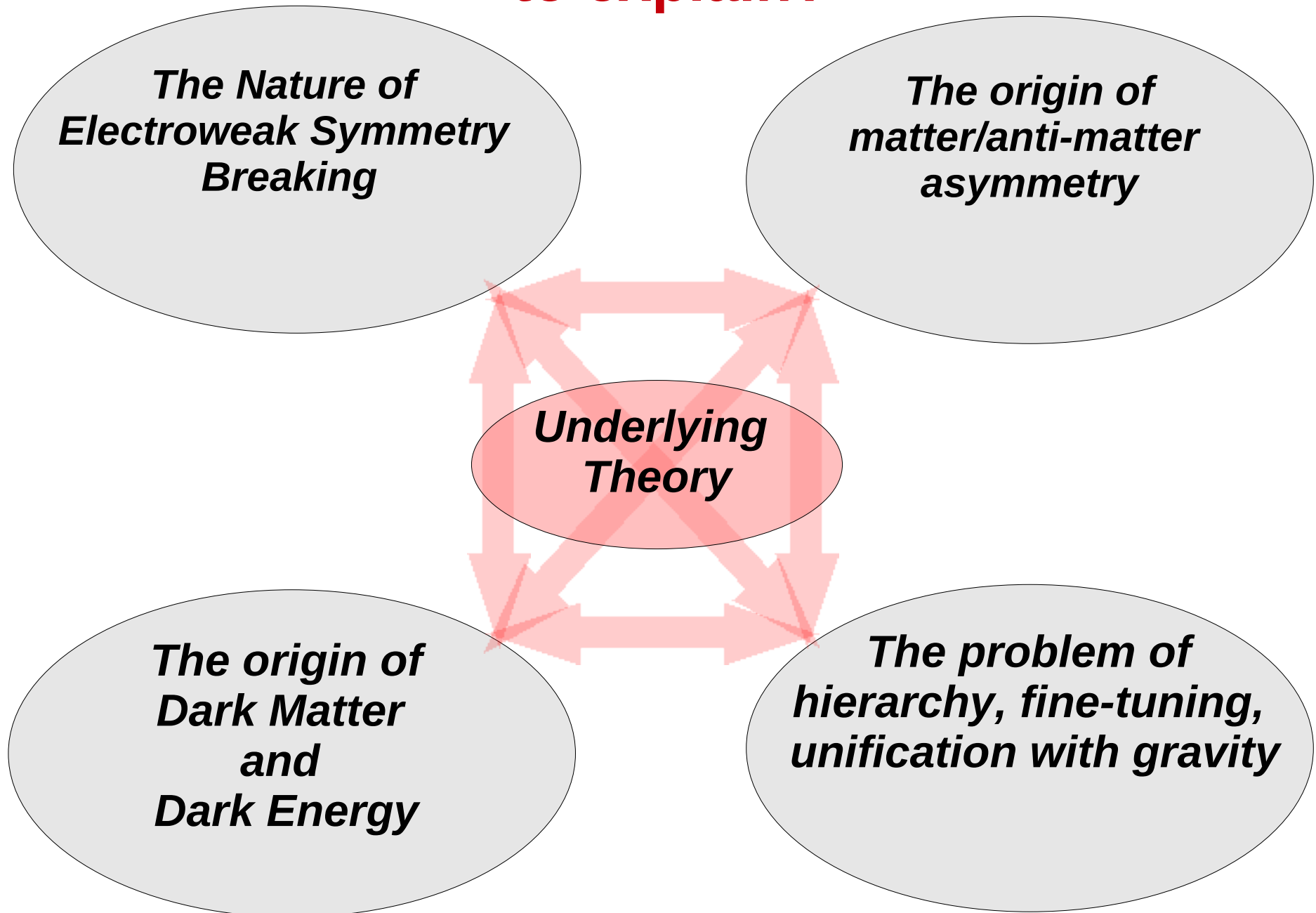
Diagram showing a fermion loop (circle) with Higgs bosons (H) and fermions (f) interacting. The equation below is:

$$\delta m_H^2 = \frac{|\lambda_f|^2}{16\pi^2} [-2\Lambda_{UV}^2 + \dots]$$

SM : $\Delta M_H^2 \sim \Lambda_{UV}^2$

$$M_H^2 = M_{H^0}^2 - \Delta M_H^2,$$


What do we expect from underlying theory to explain?



Supersymmetry

- *boson-fermion symmetry aimed to unify all forces in nature*

$$Q|BOSON\rangle = |FERMION\rangle, \quad Q|FERMION\rangle = |BOSON\rangle$$

- *extends Poincare algebra to Super-Poincare Algebra:
the most general set of space-time symmetries! (1971-74)*

$$\{f, f\} = 0, \quad [B, B] = 0, \quad \{Q_\alpha, \bar{Q}_\beta\} = 2\gamma_{\alpha\beta}^\mu P_\mu$$

Golfand and Likhtman'71; Ramond'71; Neveu, Schwarz'71; Volkov and Akulov'73; Wess and Zumino'74

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Particle	SUSY partner
e, ν, u, d <i>spin 1/2</i>	$\tilde{e}, \tilde{\nu}, \tilde{u}, \tilde{d}$ <i>spin 0</i>
γ, W, Z h, H, A, H <i>spin 1 and 0</i>	$\tilde{\chi}_R^+, \tilde{\chi}_R^+,$ $\tilde{\chi}_R^-, \dots, \tilde{\chi}_R^-$ <i>spin 1/2</i>

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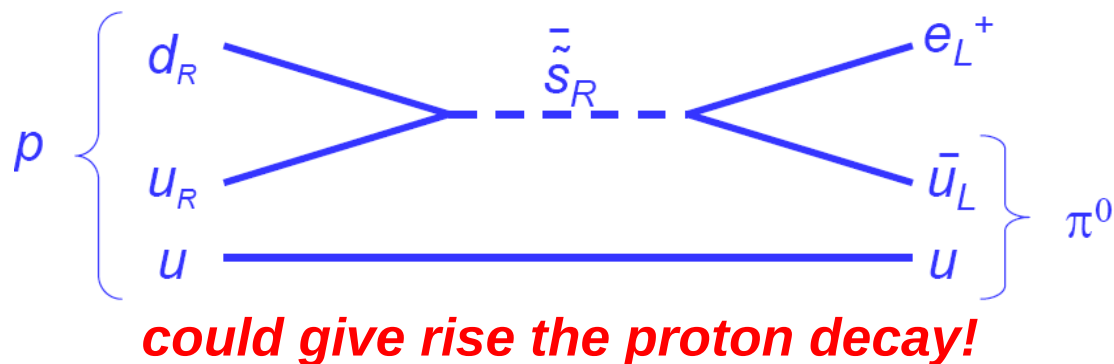
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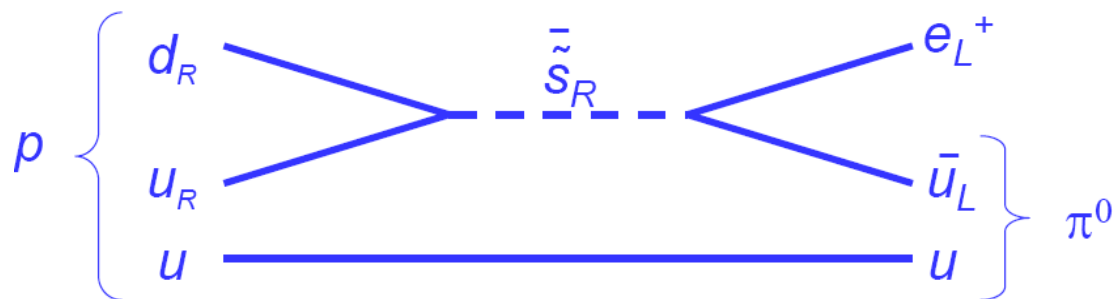
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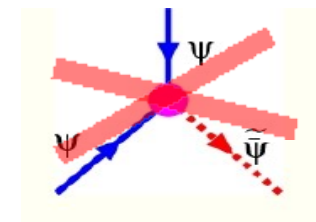
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the absence of proton decay suggests R-parity

$$R = (-1)^{3(B-L)+2S}$$



R-parity guarantees Lightest SUSY particle (LSP) is stable!

Supersymmetry

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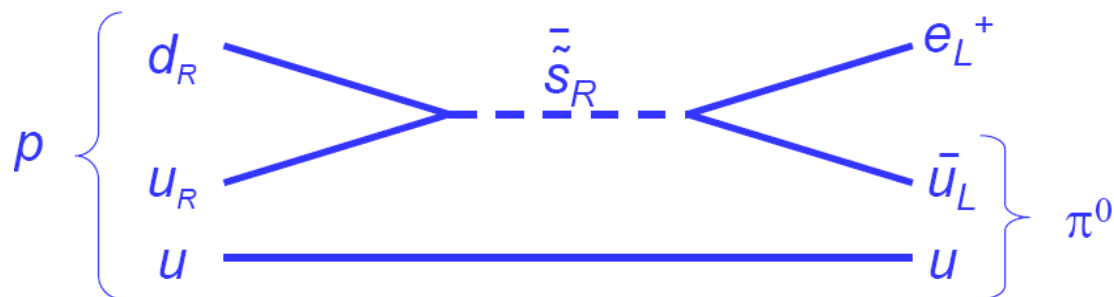
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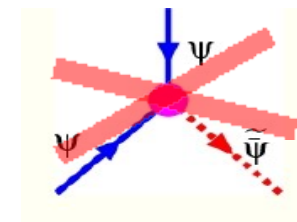
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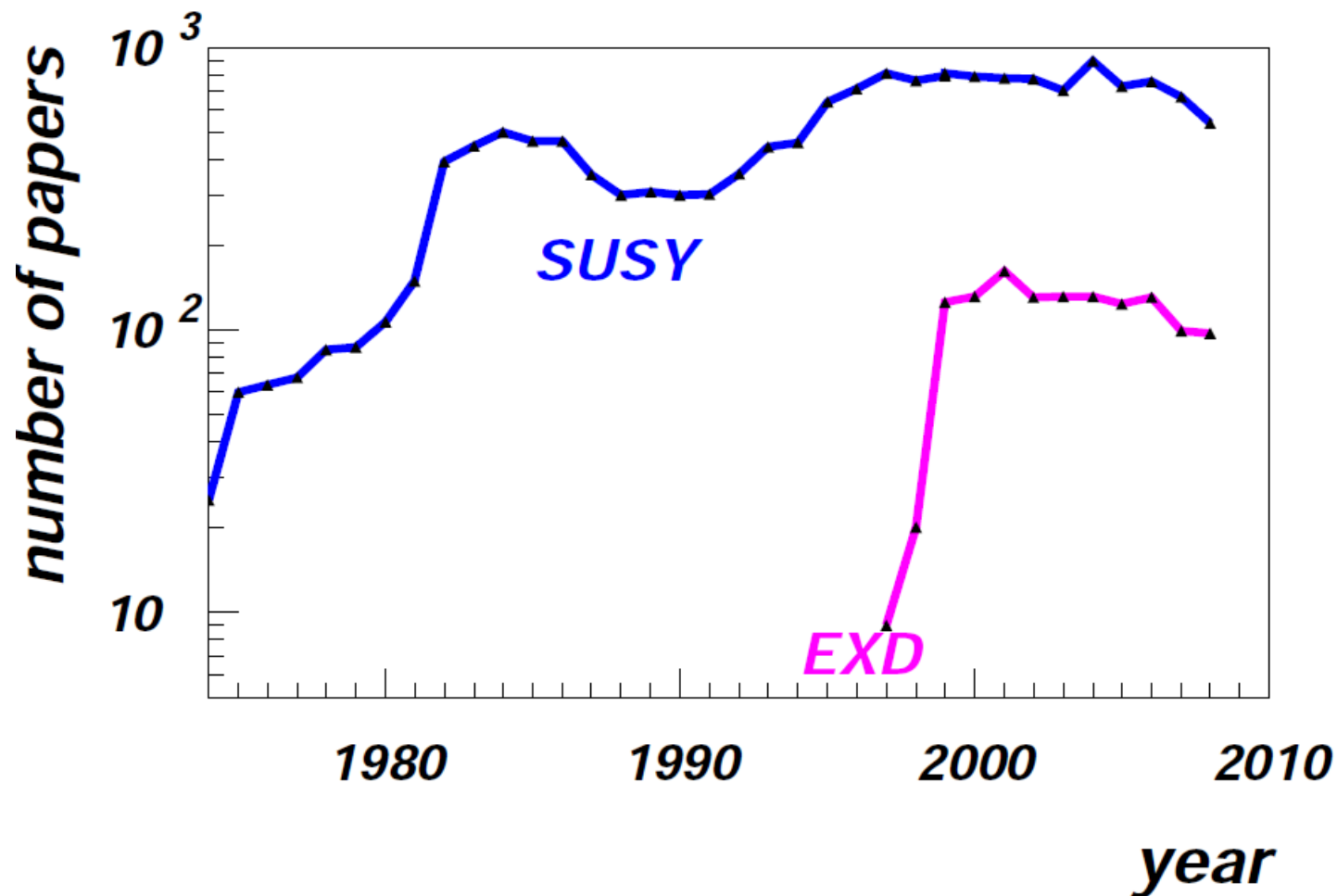
MSSM Higgs sector: two Higgs doublets

- ➔ *provide masses for up- and down-type fermions, cancellation of anomalies*
- ➔ *5 Higgs bosons h, H, A, H^\pm : $M_A, \tan\beta = v_u/v_d$ define Higgs sector at tree-level*

SUSY invented more than 30 years ago has 'little' problem

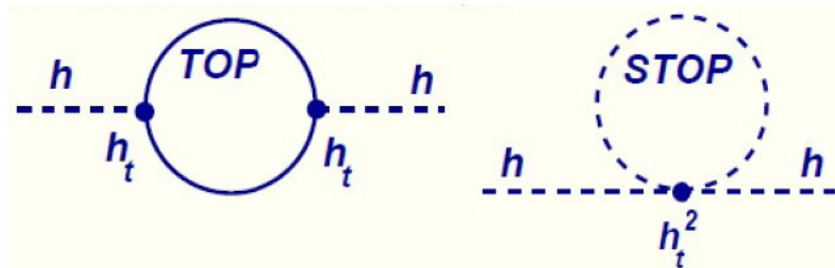
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it has not been found yet!**

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Why it is still so attractive?**

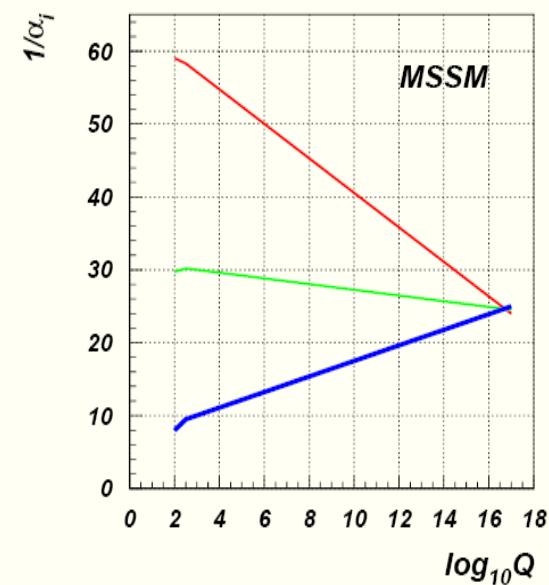
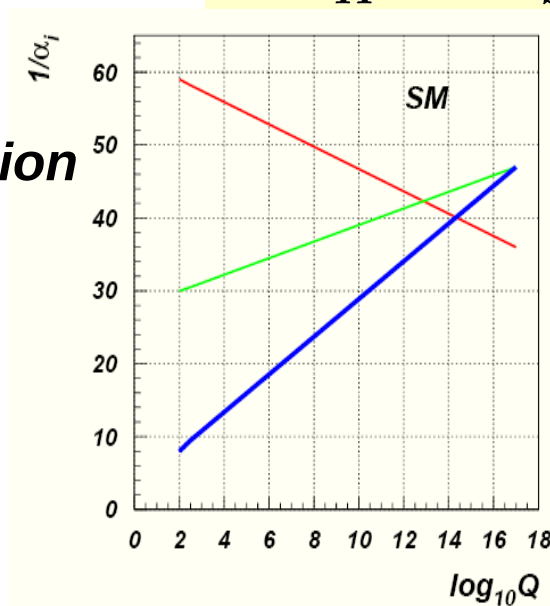


Consequences of SUSY

- Provides good DM candidate – LSP
- CP violation can be incorporated - baryogenesis via leptogenesis
- Radiative EWSB
- Solves fine-tuning problem
- Provides gauge coupling unification
- local supersymmetry requires spin 2 boson – graviton!
- allows to introduce fermions into string theories

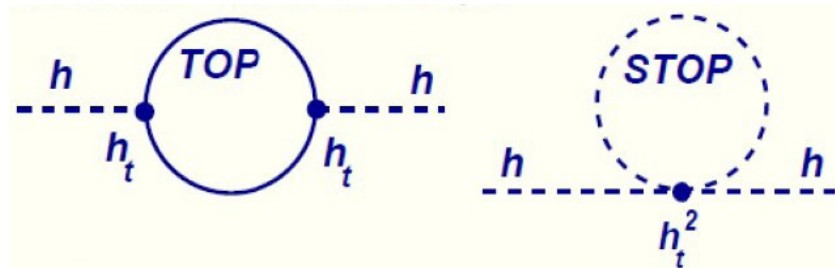


$$\Delta M_H^2 \sim M_{SUSY}^2 \log(\Lambda/M_{SUSY})$$

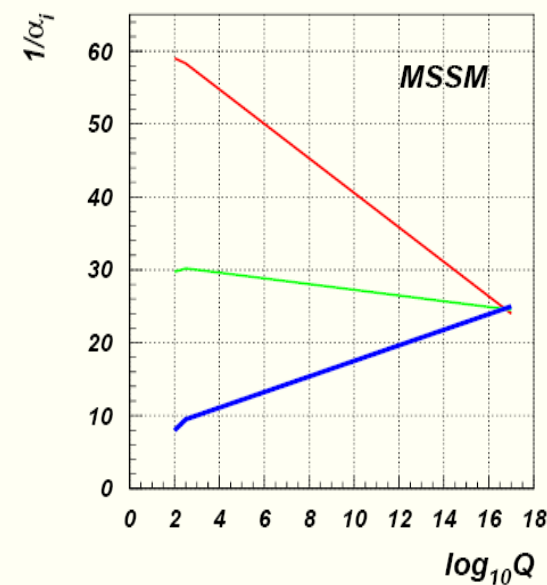
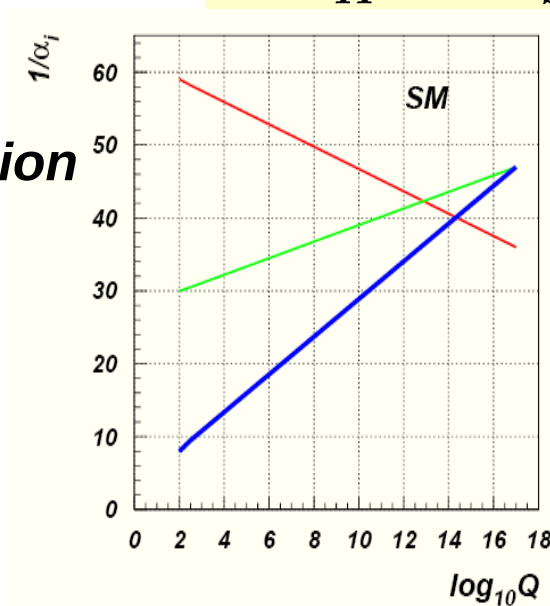


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**Contrary to many recent models
SUSY was not deliberately designed to solve the SM problems!**

SUSY breaking and mSUGRA scenario

► *SUSY is not observed* \Rightarrow *must be broken*



Gravity mediation
Gauge mediation
Anomaly mediation
Gaugino mediation

$$\mathcal{L}_{soft}^{MSSM} = \underbrace{\sum_{i,j} B_{ij} \mu_{ij} S_i S_j}_{\text{bilinear terms}} + \underbrace{\sum_{ij} m_{ij}^2 S_i S_j^\dagger}_{\text{scalar mass terms}} + \underbrace{\sum_{i,j,k} A_{ijk} f_{ijk} S_i S_j S_k}_{\text{trilinear scalar interactions}} + \underbrace{\sum_{A,\alpha} M_{A\alpha} \bar{\lambda}_{A\alpha} \lambda_{A\alpha}}_{\text{gaugino mass terms}}$$

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- **SUGRA:** the hidden sector communicates with visible one via gravity

– all soft terms are non-zero in general ($\sim m_{3/2}$ -gravitino mass)

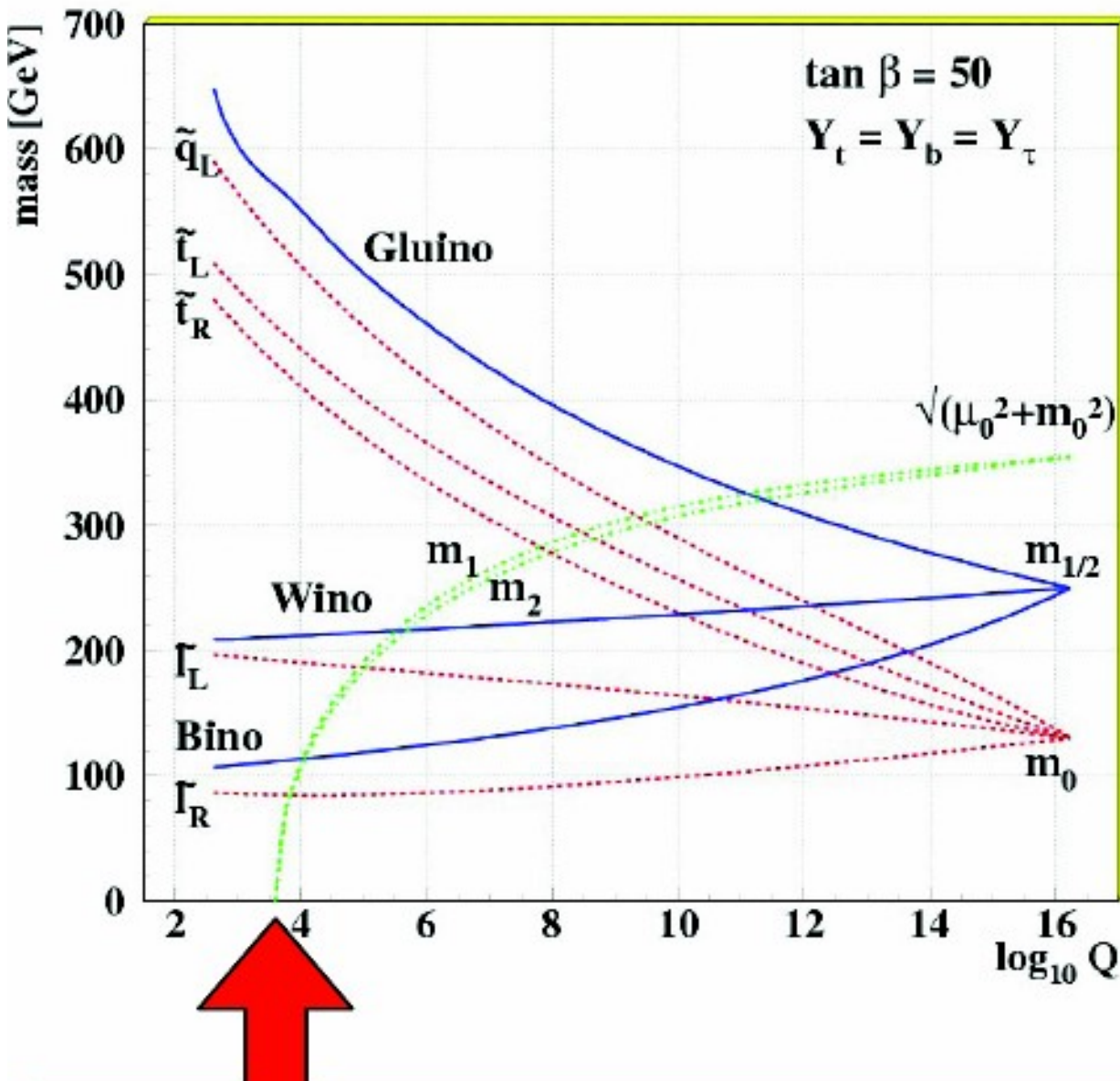
$$\text{SUGRA: } M_\alpha = f_\alpha \frac{\langle F \rangle}{M_P} \quad m_{ij}^2 = k_{ij} \frac{|\langle F \rangle|^2}{M_P^2} \quad A_{ijk} = y_{ijk} \frac{\langle F \rangle}{M_P}$$

$$\text{mSUGRA: } \quad \quad \quad \Rightarrow m_{1/2} \quad \quad \quad \Rightarrow m_0^2 \quad \quad \quad \Rightarrow A_0$$

flat Kähler metric takes care of constraining of Flavor violating processes

- $sign(\mu)$, μ^2 value is fixed by the minim condition for Higgs potential
- B - parameter – usually expressed via $\tan \beta$
- \Rightarrow **mSUGRA parameters:** $m_0, m_{1/2}, A_0, \tan \beta, sign(\mu)$

Minimal Supergravity Model (mSUGRA)



independent parameters:

- **m0** - universal scalar mass
- **m1/2** - universal gaugino masses
- **A** - trilinear soft parameter
- **tanβ** - parameter
(B traded for tanβ)
- **sign(μ)**, μ^2 value is fixed by the minimization condition for the Higgs potential

ISASUGRA, SPHENO, SUSPECT, SOFTSUSY

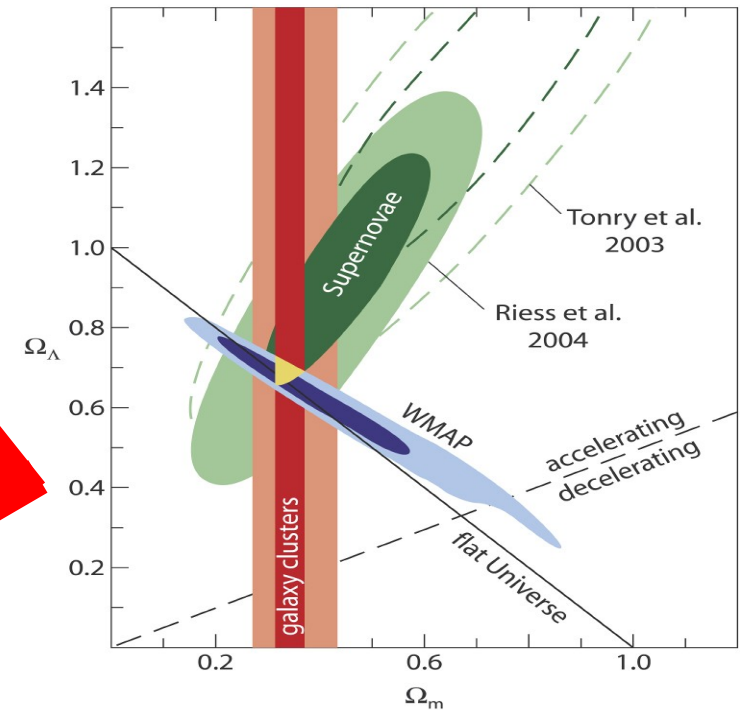
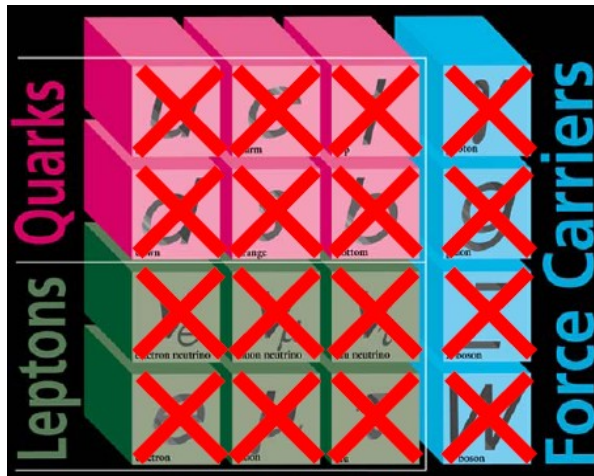
Crucial constraint from Cosmology: DM candidate should be heavy, neutral, stable, non-baryonic Dark Matter candidate

$$\Omega = \Omega_m + \Omega_\Lambda = \rho_{tot}/\rho_{crit} \simeq 1$$

Baryons: $4\% \pm 0.4\%$

Dark Matter: $23\% \pm 4\%$

Dark Energy: $73\% \pm 4\%$



Constraining the Cosmological Parameters

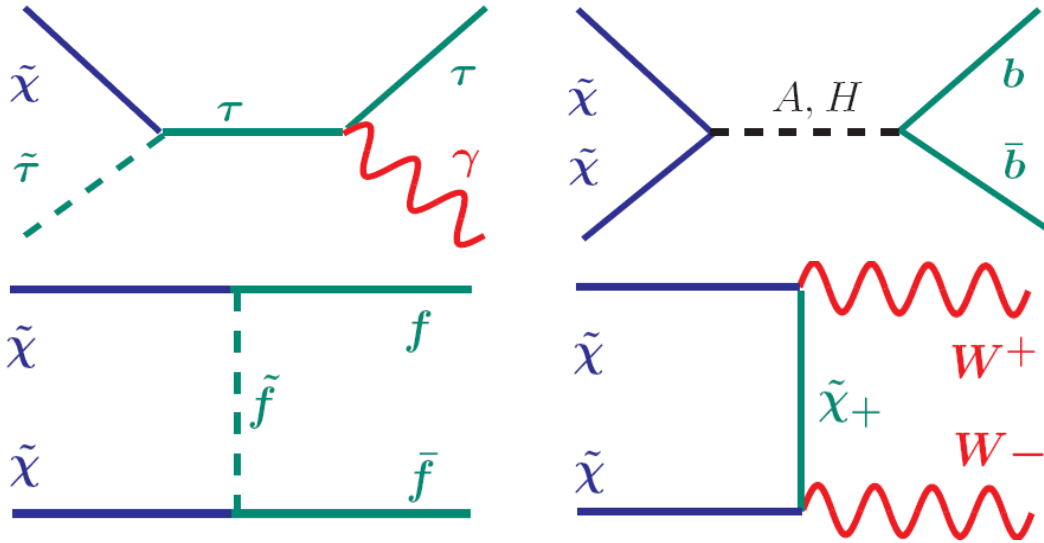
ESO PR Photo 18d/04 (3 June 2004)

© European Southern Observatory

SUSY has a perfect DM candidate, but this is only a beginning of the story ...

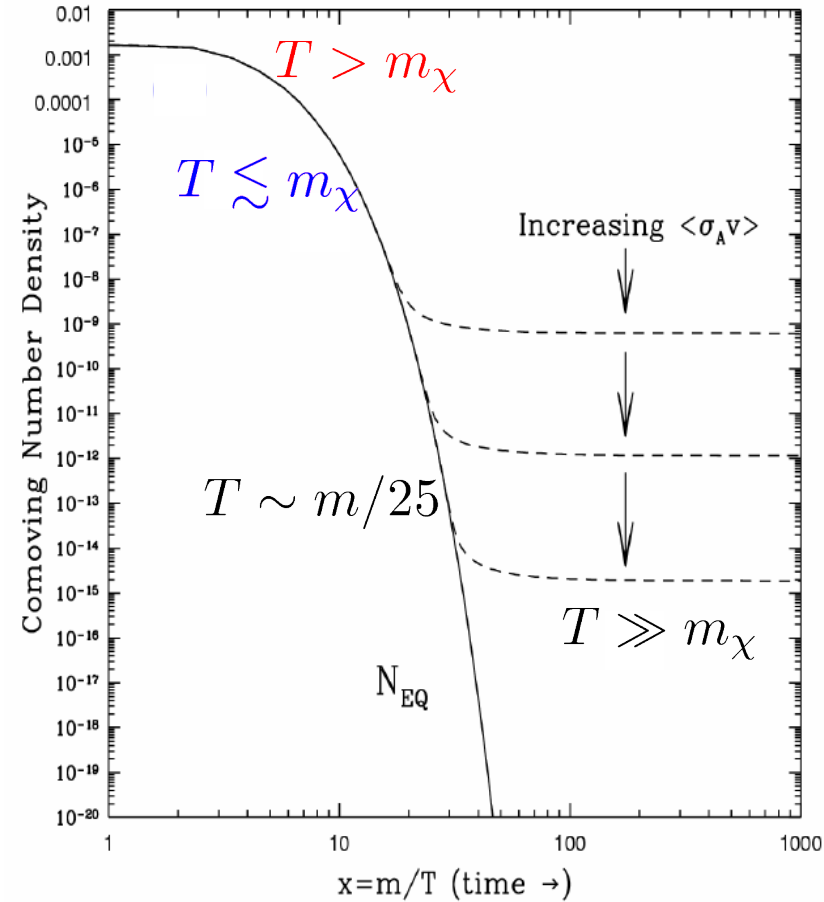
Evolution of neutralino relic density

Challenge is to evaluate thousands annihilation/co-annihilation diagrams



time evolution of number density is given by Boltzmann equation

$$dn/dt = -3Hn - \langle \sigma_A v \rangle (n^2 - n_{eq}^2)$$



relic density depends crucially on $\langle \sigma_A v \rangle$
 thermal equilibrium stage: $T > m_\chi$, $\chi\chi \leftrightarrow f\bar{f}$
 universe cools: $T \lesssim m_\chi$, $\chi\chi \not\leftrightarrow f\bar{f}$, $n = n_{eq} \sim e^{-m/T}$
 neutralinos "freeze-out" at $T_F \sim m/25$

ISARED code: complete set of processes

Baer, A.B., Balazs '02

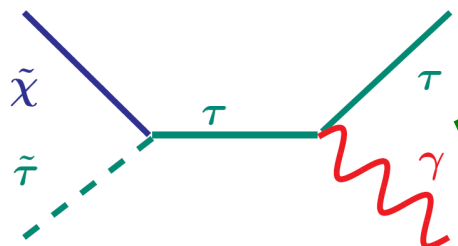
exact tree-level calculations using CompHEP

$$\Omega_\chi = \frac{10^{-10} \text{GeV}^{-2}}{\langle \sigma_A v \rangle} \simeq 10^{-1 \pm 1}$$

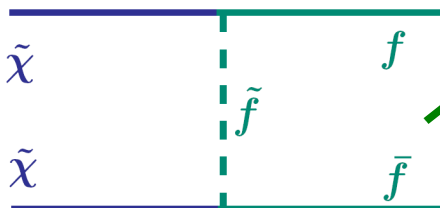
if $\langle \sigma_A v \rangle \sim \frac{\alpha^2}{m_W^2} 0.1 \sim 10^{-9 \pm 1}$

Neutralino relic density in mSUGRA

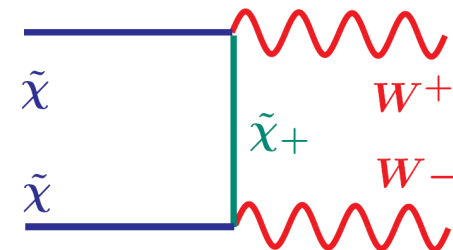
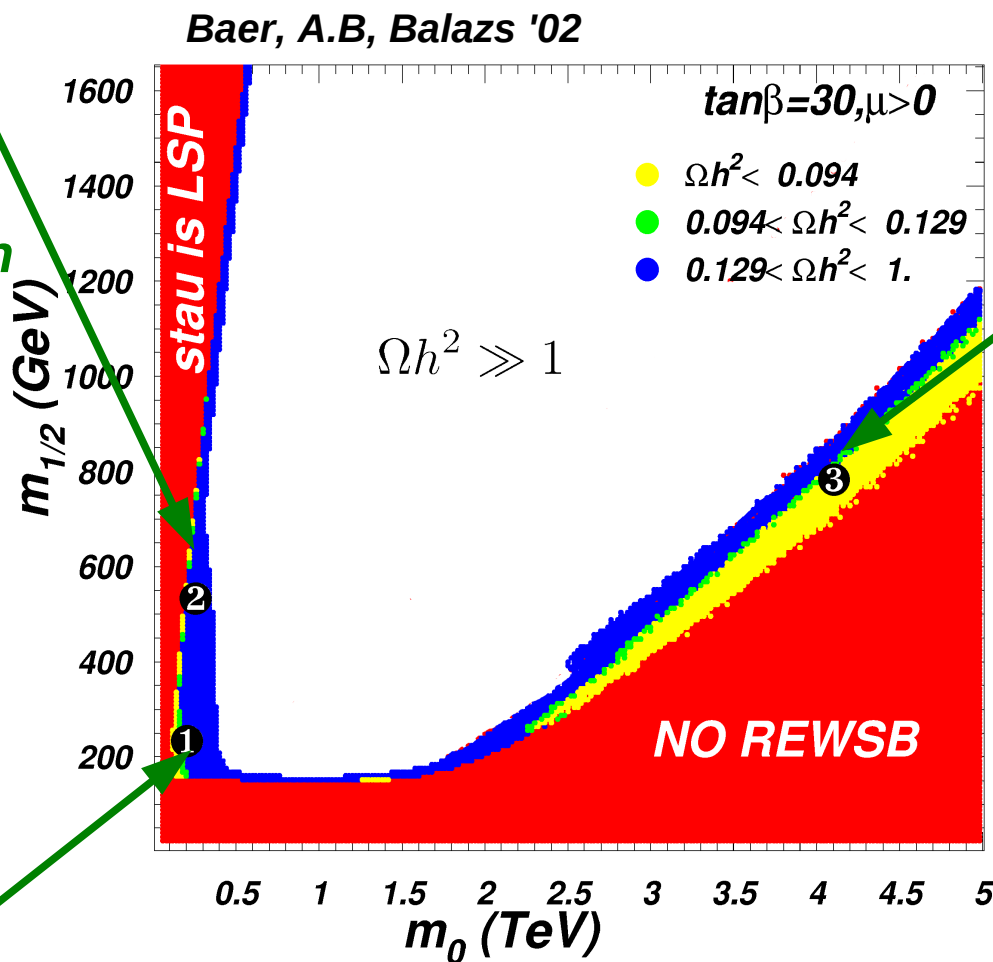
most of the parameter space is ruled out! $\Omega h^2 \gg 1$
 special regions with high σ_A are required to get $0.094 < \Omega h^2 < 0.129$



2. stau coannihilation
 degenerate χ and stau



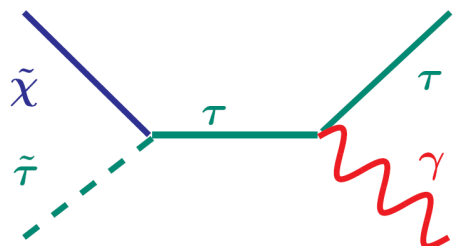
1. bulk region: light sfermions



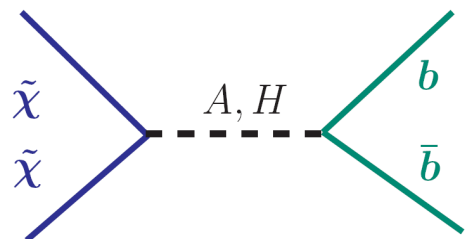
3. focus point:
 mixed neutralino,
 low μ , importance of
 higgsino-wino
 component
 $\mu^2 + M_Z^2 / 2 \approx -\epsilon m_0^2 + 2m_{1/2}^2$

Neutralino relic density in mSUGRA

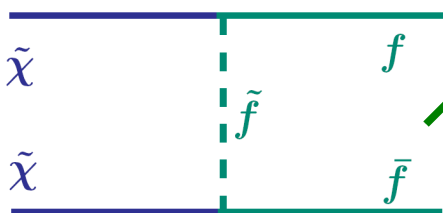
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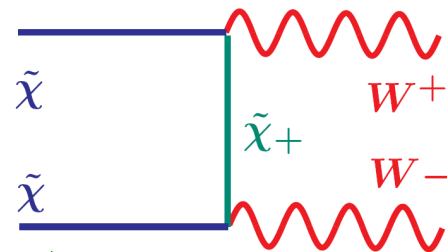
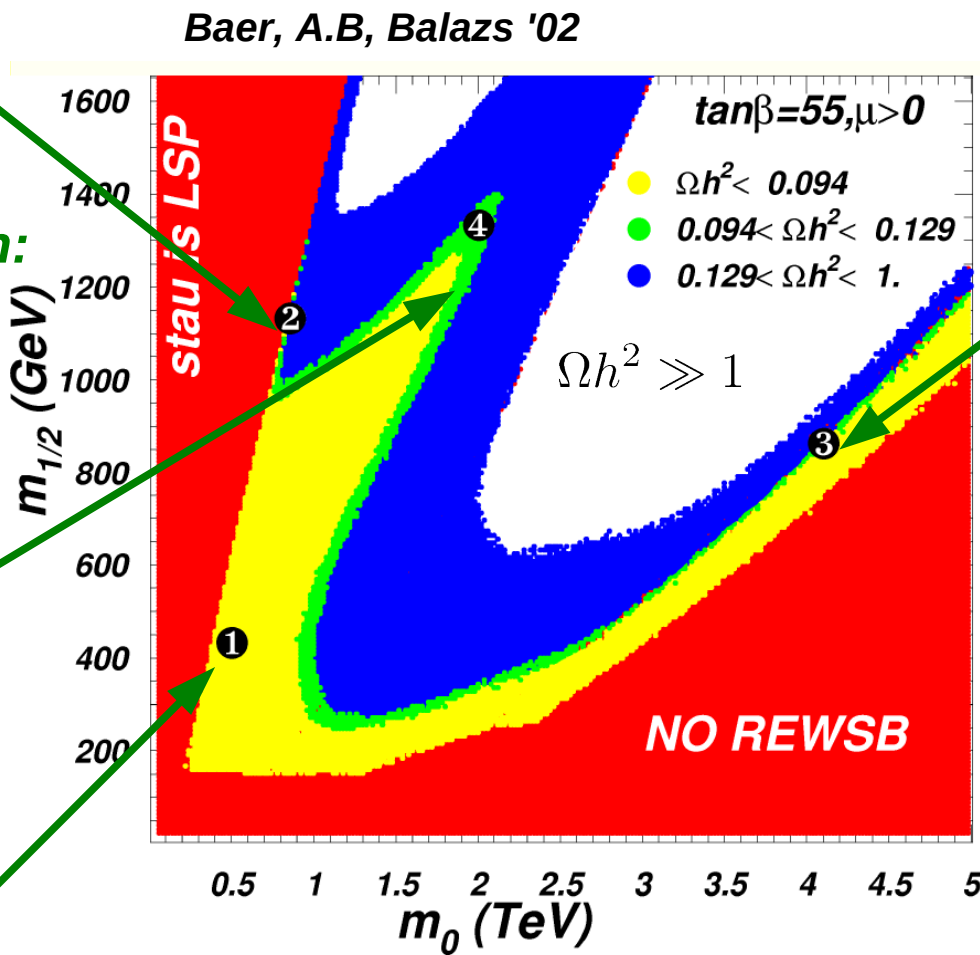
2. stau coannihilation:
degenerate χ and stau



4. funnel: (large $\tan\beta$)
annihilation via A, H



1. bulk region: light sfermions



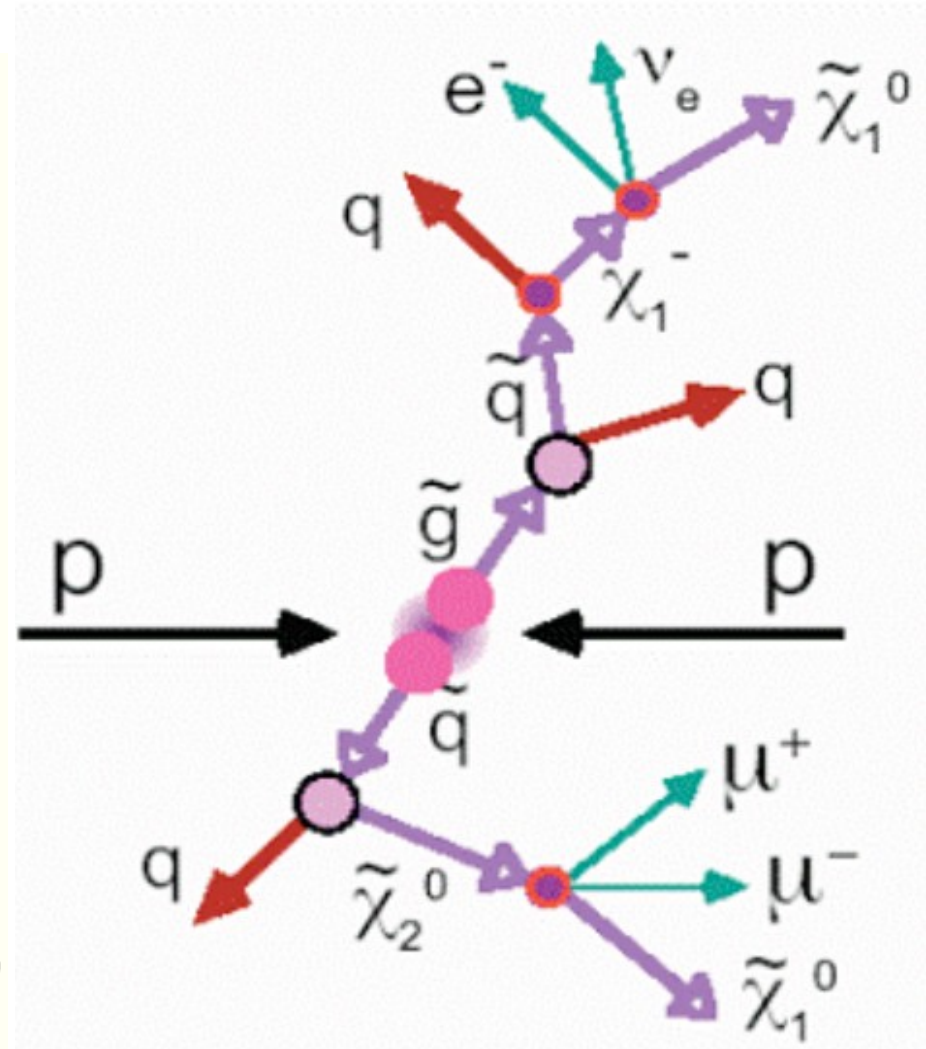
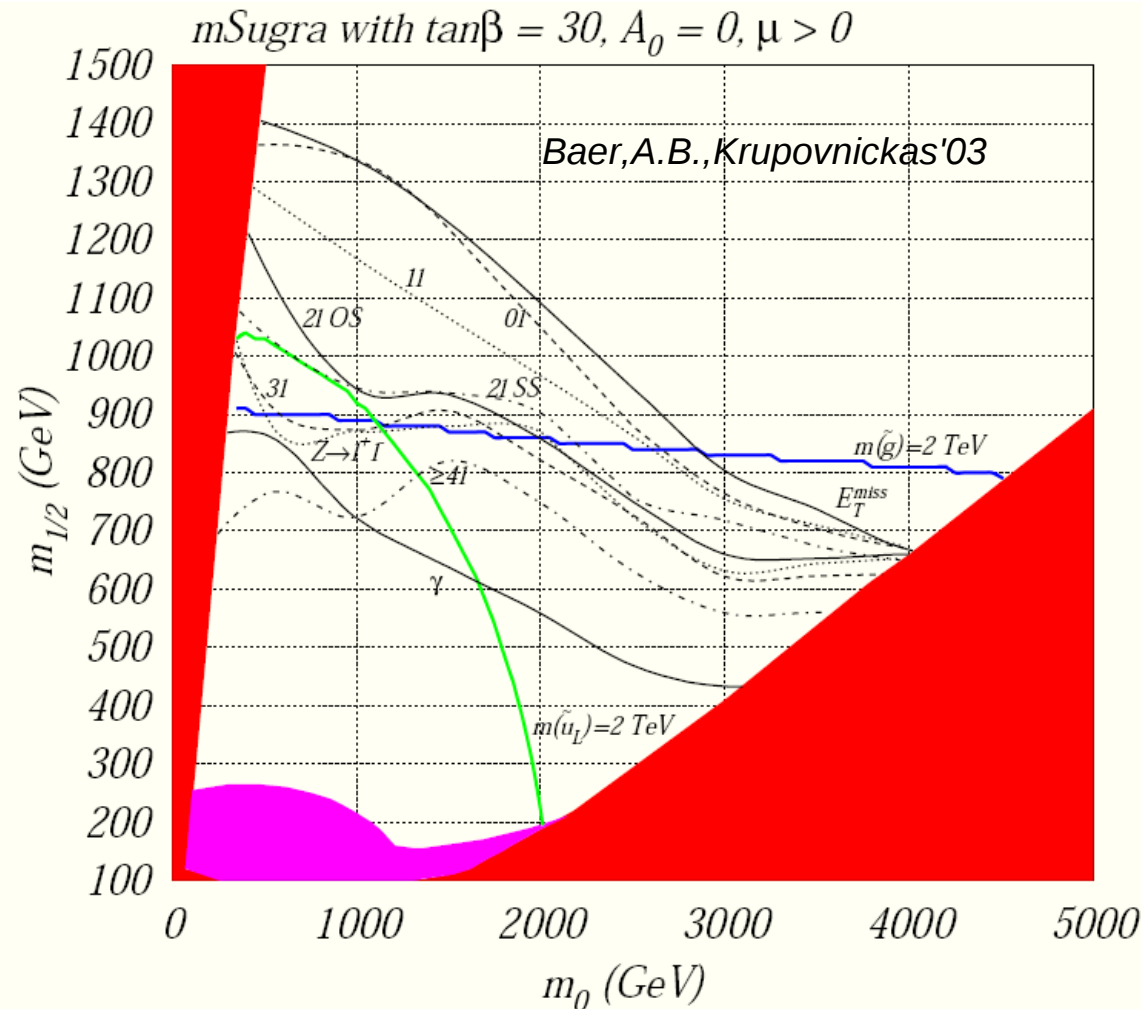
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additional regions:
Z/h annihilation
stop coannihilation

Collider signatures in DM allowed regions

$\tilde{g}\tilde{g}$, $\tilde{g}\tilde{q}$, $\tilde{q}\tilde{q}$ production dominant for $m \lesssim 1$ TeV BG: $W + jets$, $Z + jets$, $t\bar{t}$, $b\bar{b}$, WW , $4t$, ...

- $\cancel{E}_T + jets$
- $1l + \cancel{E}_T + jets$
- opposite - sign (OS) $2l + \cancel{E}_T + jets$
- same - sign (SS) $2l + \cancel{E}_T + jets$
- $3l + \cancel{E}_T + jets$
- $4l + \cancel{E}_T + jets$
- $5l + \cancel{E}_T + jets$



reach to $m_{\tilde{g}} \sim 1.8$ (3) TeV for high (low) m_0

Collider signatures in DM allowed regions

$\tilde{g}\tilde{g}, \tilde{g}\tilde{q}, \tilde{q}\tilde{q}$ production dominant for $m \lesssim 1$ TeV BG: $W + jets, Z + jets, t\bar{t}, b\bar{b}, WW, 4t, \dots$

- $\cancel{E}_T + jets$ • $1l + \cancel{E}_T + jets$ • *opposite - sign (OS)* $2l + \cancel{E}_T + jets$ • *same - sign (SS)* $2l + \cancel{E}_T + jets$
- $3l + \cancel{E}_T + jets$ • $4l + \cancel{E}_T + jets$ • $5l + \cancel{E}_T + jets$

★ $\cancel{E}_T > 200$ GeV

★ $N_j \geq 2$

where $p_T(jet) > 40$ GeV and $|\eta(jet)| < 3$

★ Grid of cuts for optimized S/B:

– $N_j \geq 2 - 10$

– $\cancel{E}_T > 200 - 1400$ GeV

– $E_T(j1) > 40 - 1000$ GeV

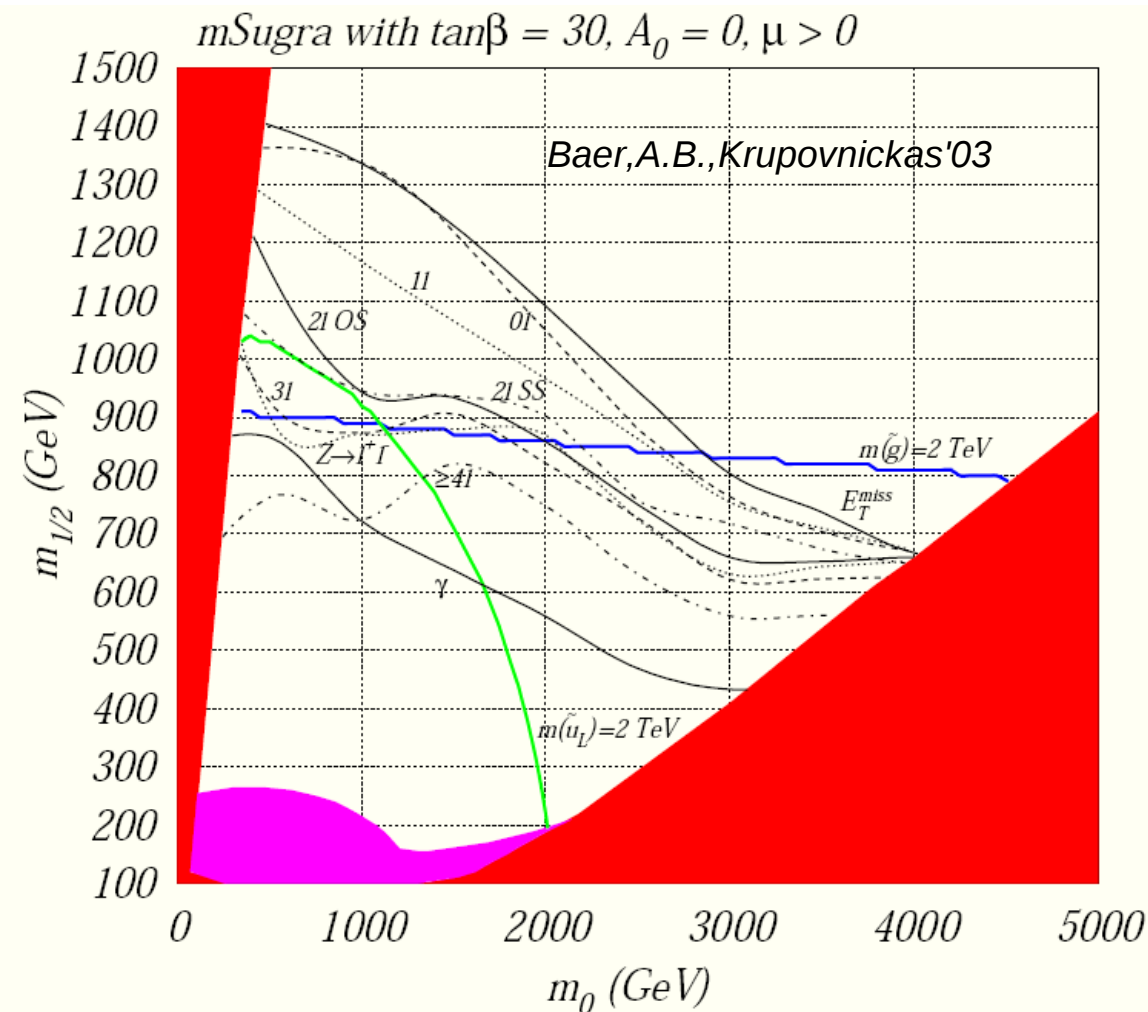
– $E_T(j2) > 40 - 500$ GeV

– $S_T > 0 - 0.2$

– muon isolation

★ $S > 10$ events for 100 fb^{-1}

★ $S > 5\sqrt{B}$ for optimal set of cuts



reach to $m_{\tilde{g}} \sim 1.8$ (3) TeV for high (low) m_0

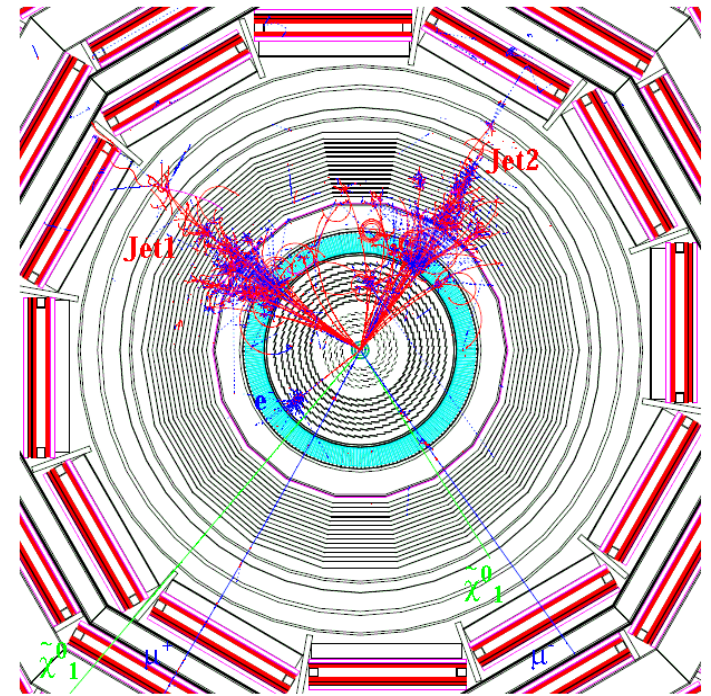
Collider signatures in DM allowed regions

$\tilde{g}\tilde{g}, \tilde{g}\tilde{q}, \tilde{q}\tilde{q}$ production dominant for $m \lesssim 1$ TeV BG: $W + jets, Z + jets, t\bar{t}, b\bar{b}, WW, 4t, \dots$

- $\cancel{E}_T + jets$ • $1l + \cancel{E}_T + jets$ • *opposite - sign (OS)* $2l + \cancel{E}_T + jets$ • *same - sign (SS)* $2l + \cancel{E}_T + jets$
- $3l + \cancel{E}_T + jets$ • $4l + \cancel{E}_T + jets$ • $5l + \cancel{E}_T + jets$

SUSY event with 3 lepton + 2 Jets signature

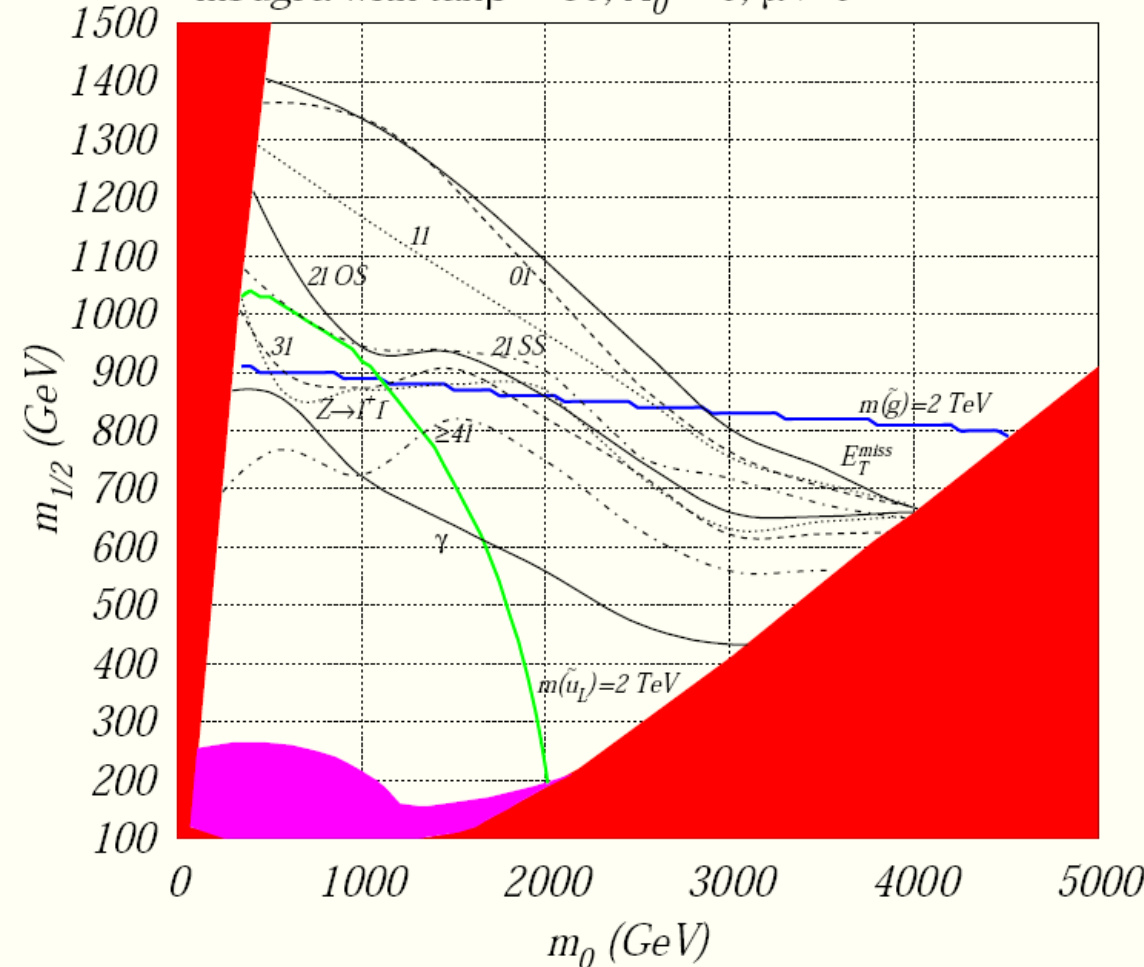
$m_0 = 100$ GeV, $m_{1/2} = 300$ GeV, $\tan\beta = 2, A_0 = 0, \mu < 0,$
 $m(\tilde{q}) = 686$ GeV, $m(\tilde{g}) = 766$ GeV, $m(\tilde{\chi}^0_2) = 257$ GeV,
 $m(\tilde{\chi}^0_1) = 128$ GeV.



Leptons:	Jets:	Sparticles:
$p_t(\mu^+) = 55.2$ GeV	$E_t(\text{Jet1}) = 237$ GeV	$p_t(\tilde{\chi}^0_1) = 95.1$ GeV
$p_t(\mu^-) = 44.3$ GeV	$E_t(\text{Jet2}) = 339$ GeV	$p_t(\tilde{\chi}^0_1) = 190$ GeV
$p_t(e) = 43.9$ GeV		

Charged particles with $p_t > 2$ GeV, $|\eta| < 3$ are shown; neutrons are not shown; no pile up events superimposed.

mSugra with $\tan\beta = 30, A_0 = 0, \mu > 0$

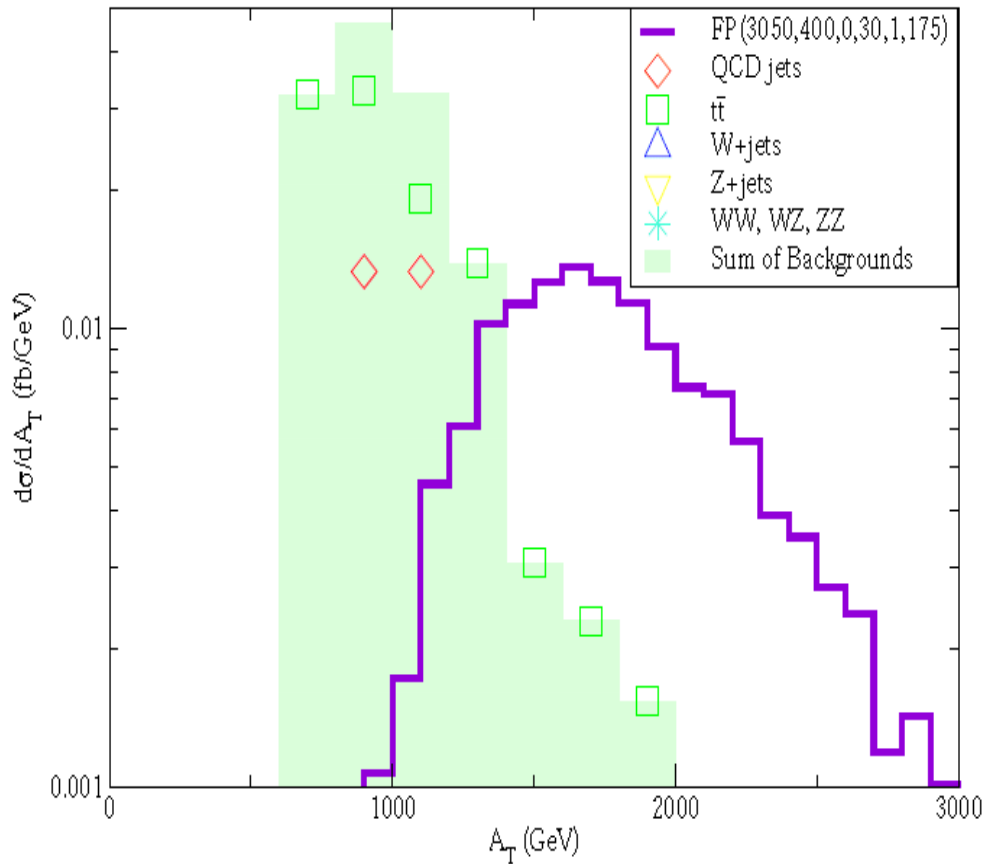


reach to $m_{\tilde{g}} \sim 1.8$ (3) TeV for high (low) m_0

Collider signatures in DM allowed regions

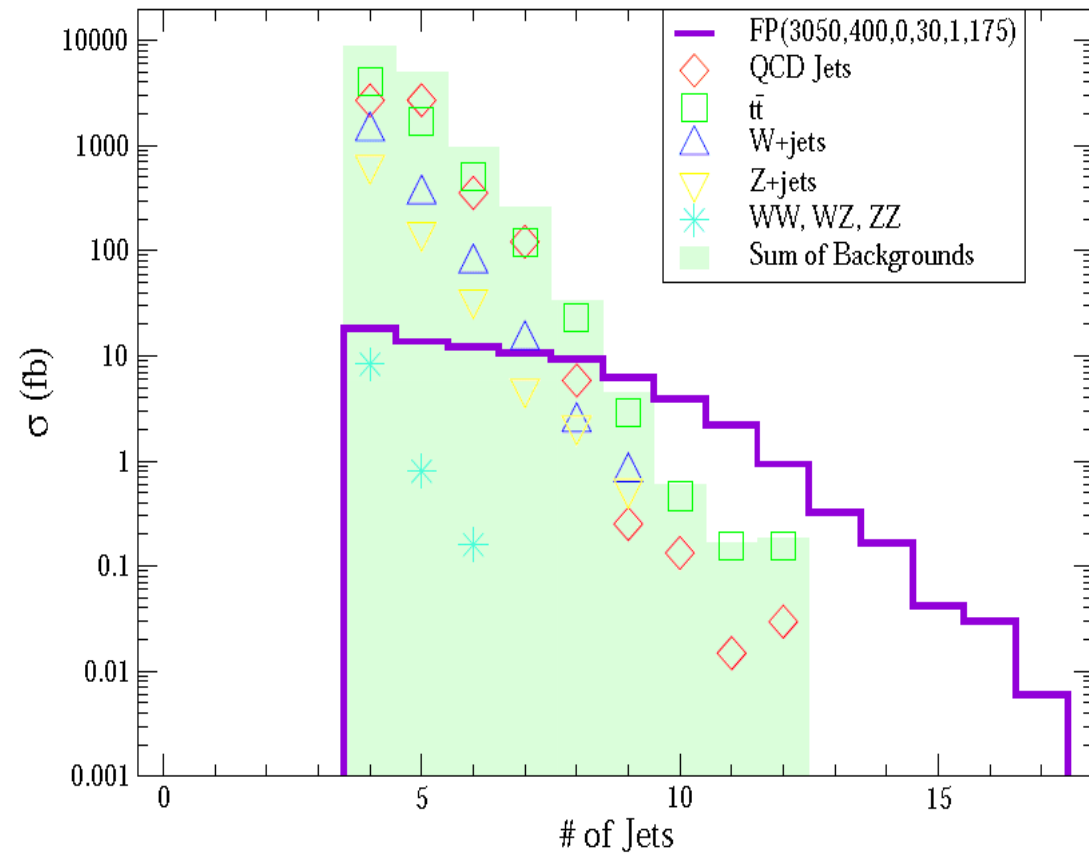
Augmented Effective Mass

Cuts C1, $n_{b\text{-jets}} \geq 2$ (60% eff.)



No. of Jets

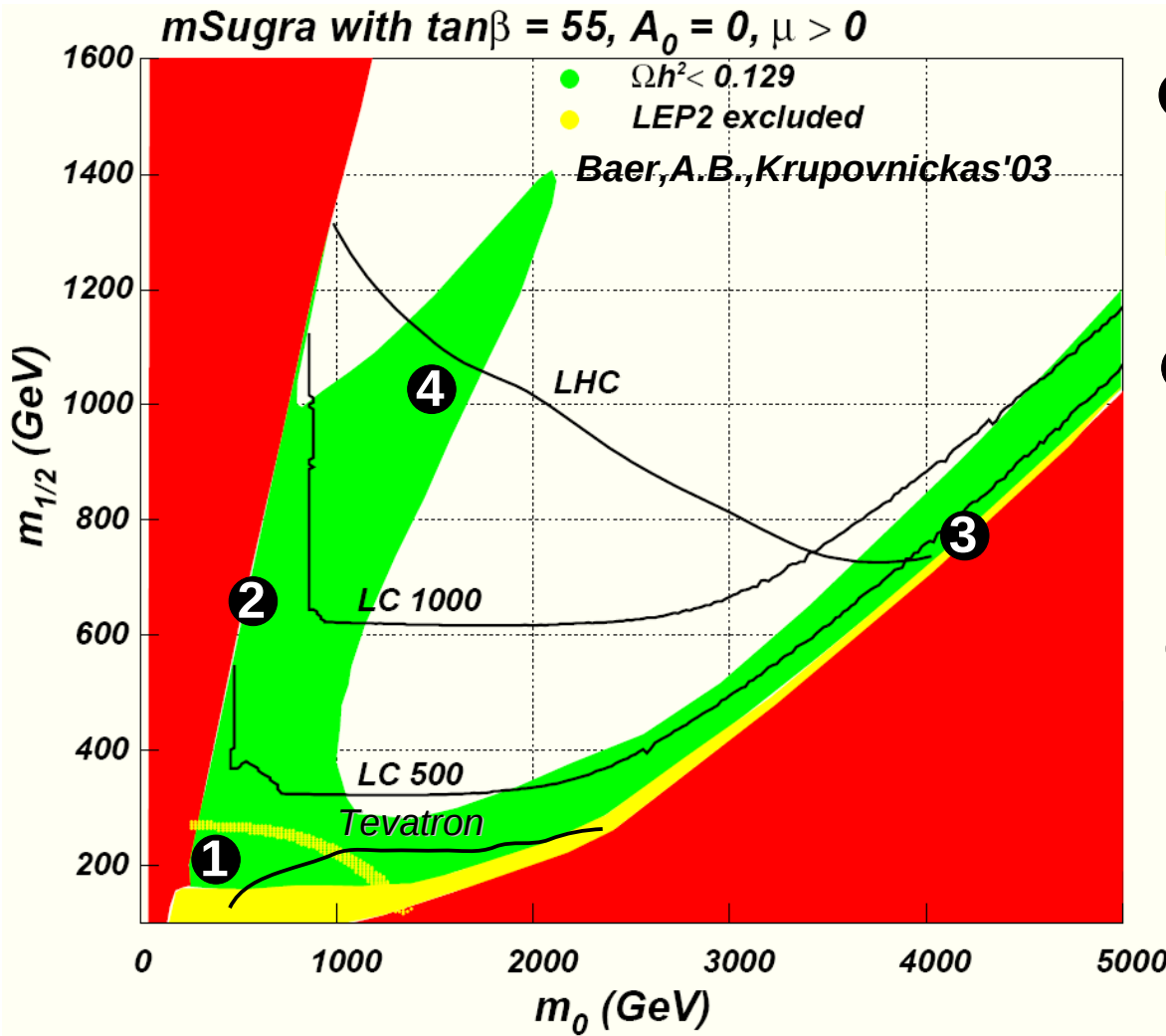
Cuts C1



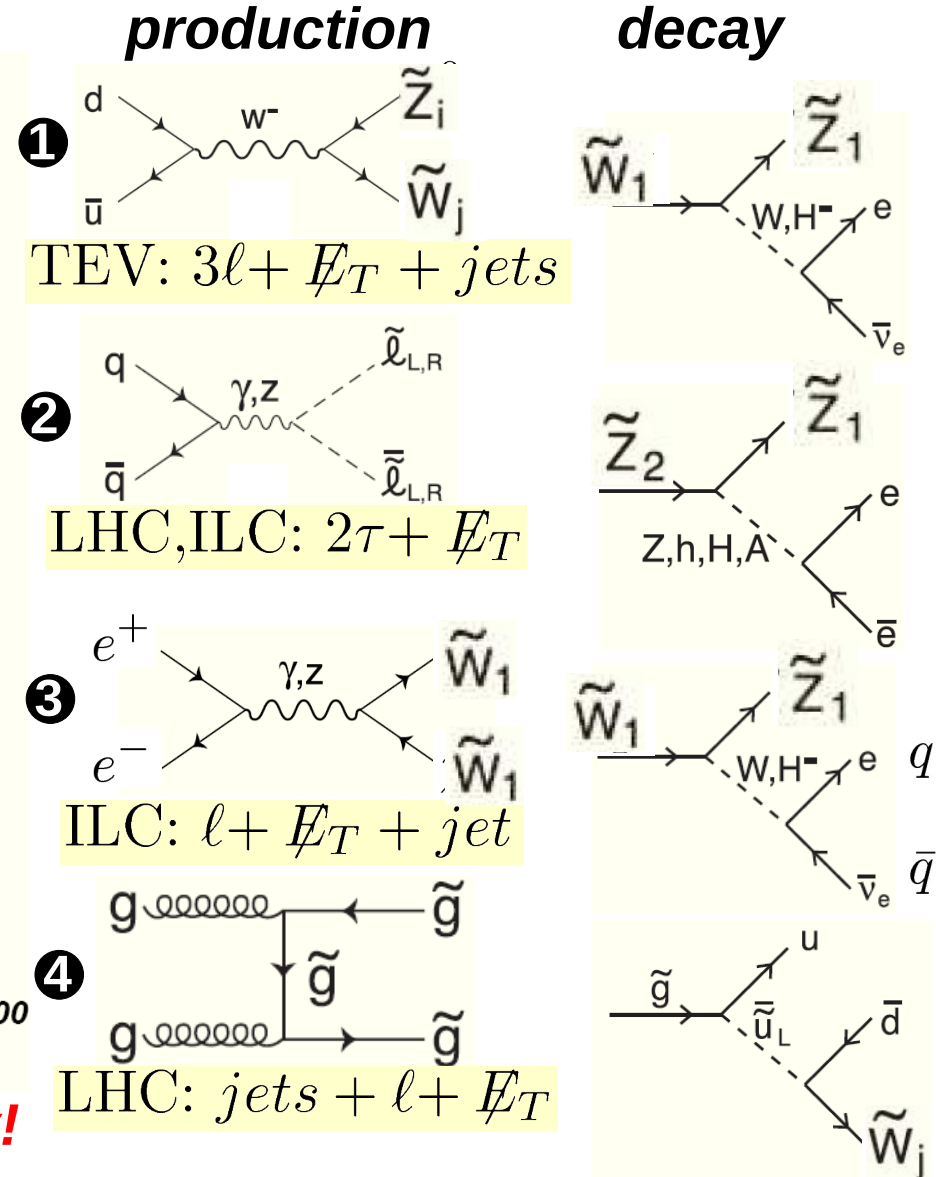
$$A_T = E_T^{miss} + \sum_{leptons} E_T + \sum_{jets} E_T$$

H. Baer, V. Barger, H. Summy, L-T. Wang
hep-ph/0703298

Collider signatures in DM allowed regions



LHC and ILC are highly complementary!



Why FP region is important

- small value of $|\mu|$ -parameter: mixed higgsino-bino LSP
- Light mass spectrum of chargino and neutralinos
- low value of $|\mu|$ -parameter was advocated as “fine-tuning” measure
- DM motivated mSUGRA region with 'natural' neutralino mass ~ 100 GeV !
- ILC connection: the signal observation at the LHC is crucial for the fate of ILC

$$\chi = a_{\tilde{B}} \tilde{B} + a_{\tilde{W}} \tilde{W}^0 + a_{\tilde{H}_u} \tilde{H}_u^0 + a_{\tilde{H}_d} \tilde{H}_d^0$$

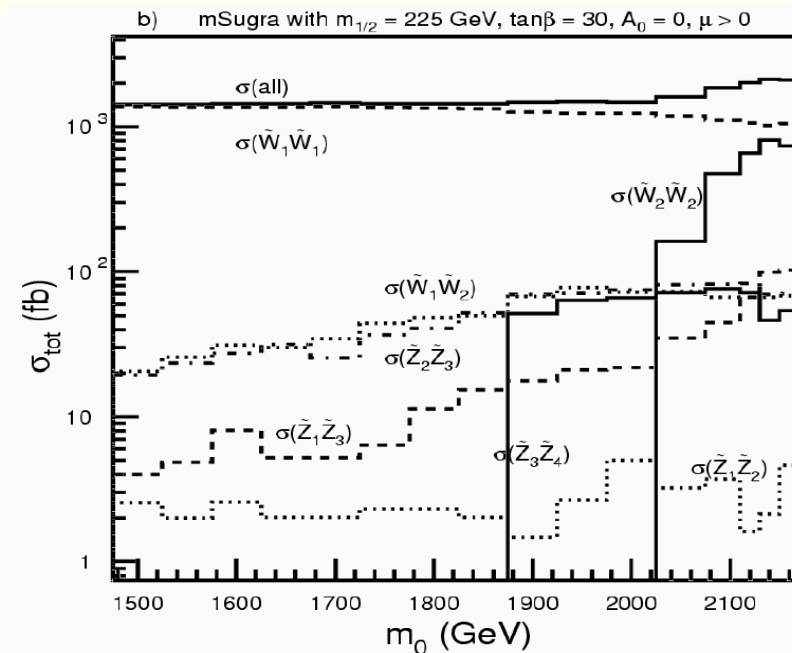
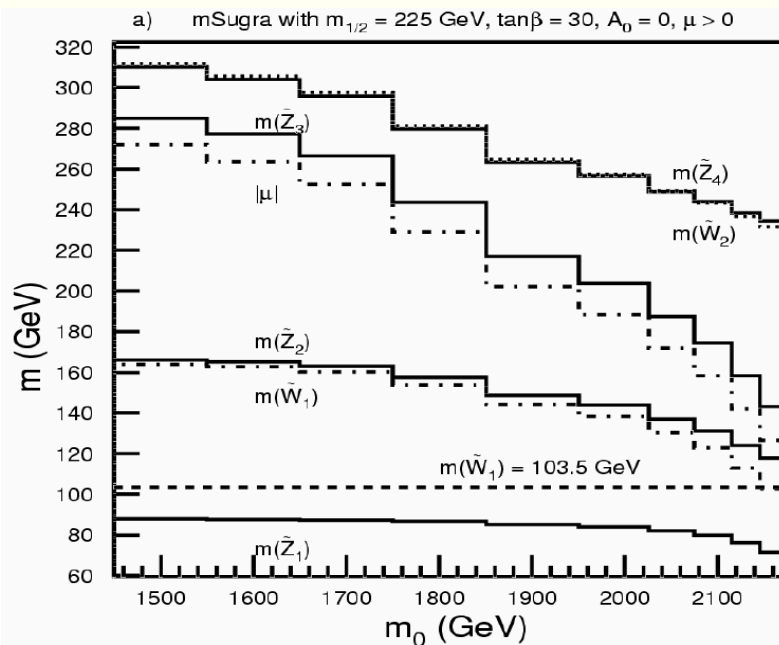
$$\begin{pmatrix} M_1 & 0 & -m_Z c \beta s_W & m_Z s \beta s_W \\ 0 & M_2 & m_Z c \beta c_W & -m_Z s \beta c_W \\ -m_Z c \beta s_W & m_Z c \beta c_W & 0 & -\mu \\ m_Z s \beta s_W & -m_Z s \beta c_W & -\mu & 0 \end{pmatrix}$$

$$\begin{pmatrix} M_2 & \sqrt{2} s_\beta m_W \\ \sqrt{2} c_\beta m_W & \mu \end{pmatrix}$$

neutralino and chargino mass matrices

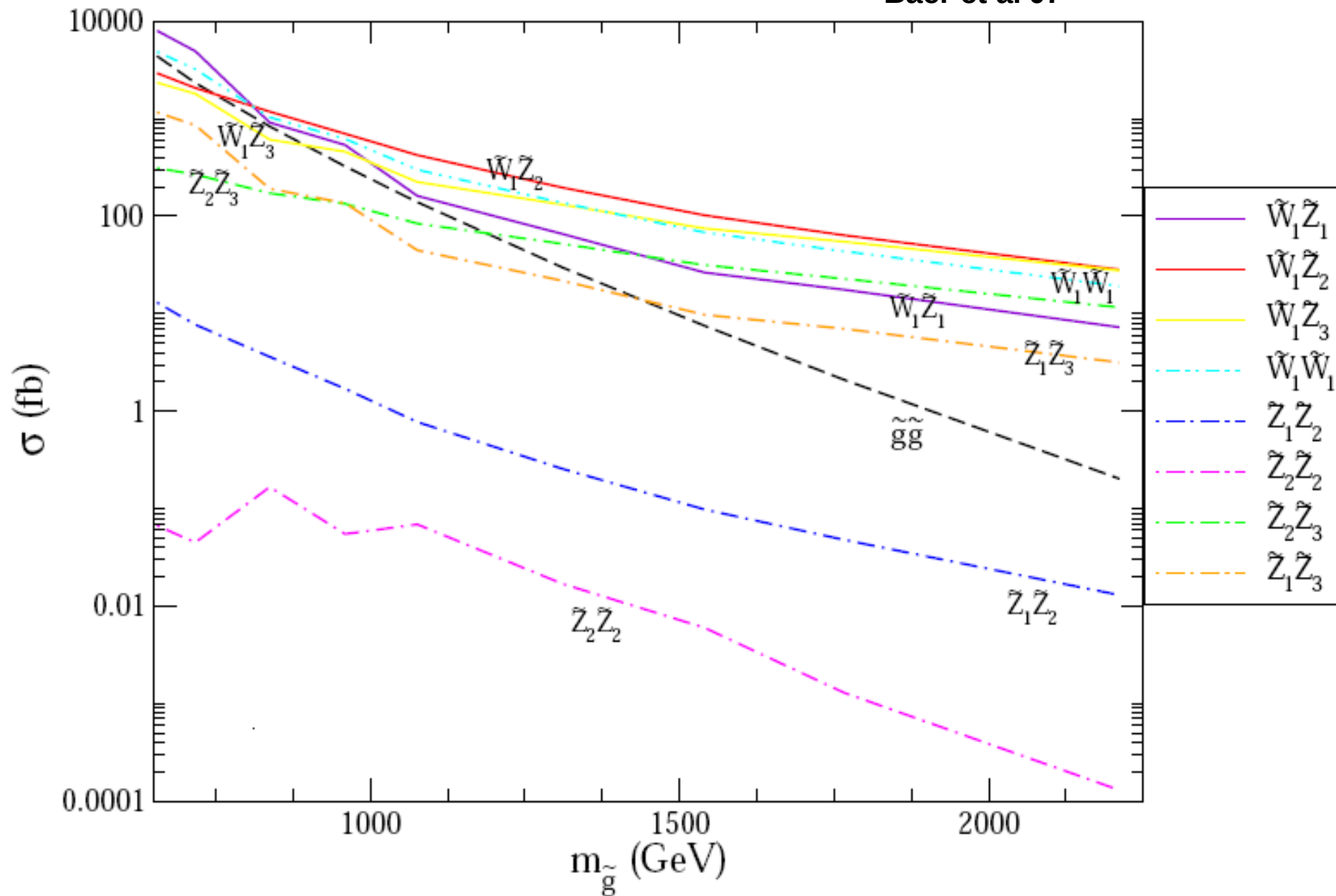
Chan, Chattopadhyay, Nath '97;
Feng, Matchev, Moroi '99; Baer, Chen, Paige, Tata '95,
Chattopadhyay, Datta's, Roy '00

HB/FP region for $m_{1/2} = 225$ GeV, $\tan \beta = 30$, $A_0 = 0$, $\mu > 0$: $\sqrt{s} = 500$ GeV



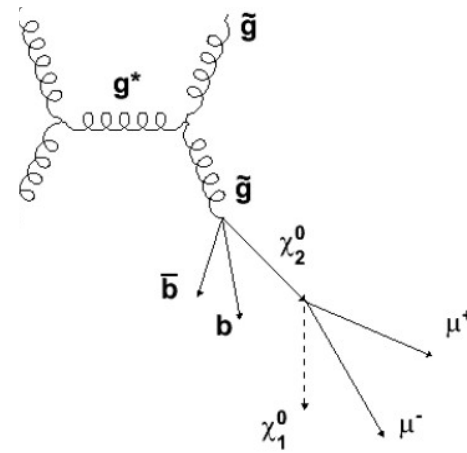
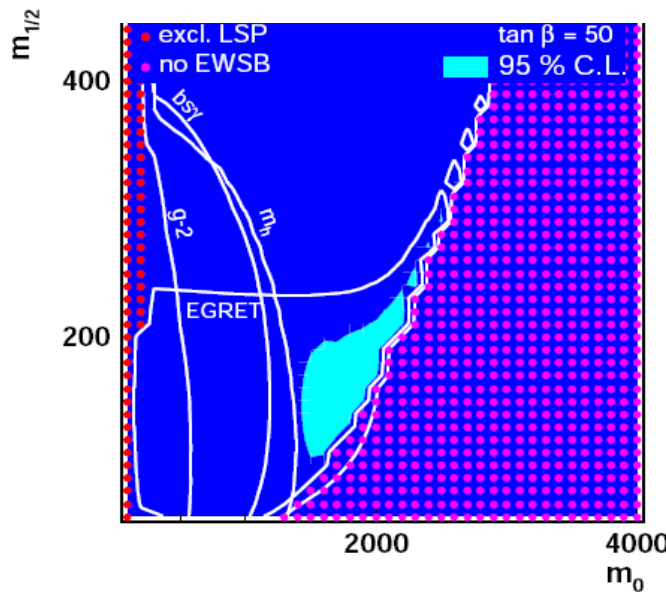
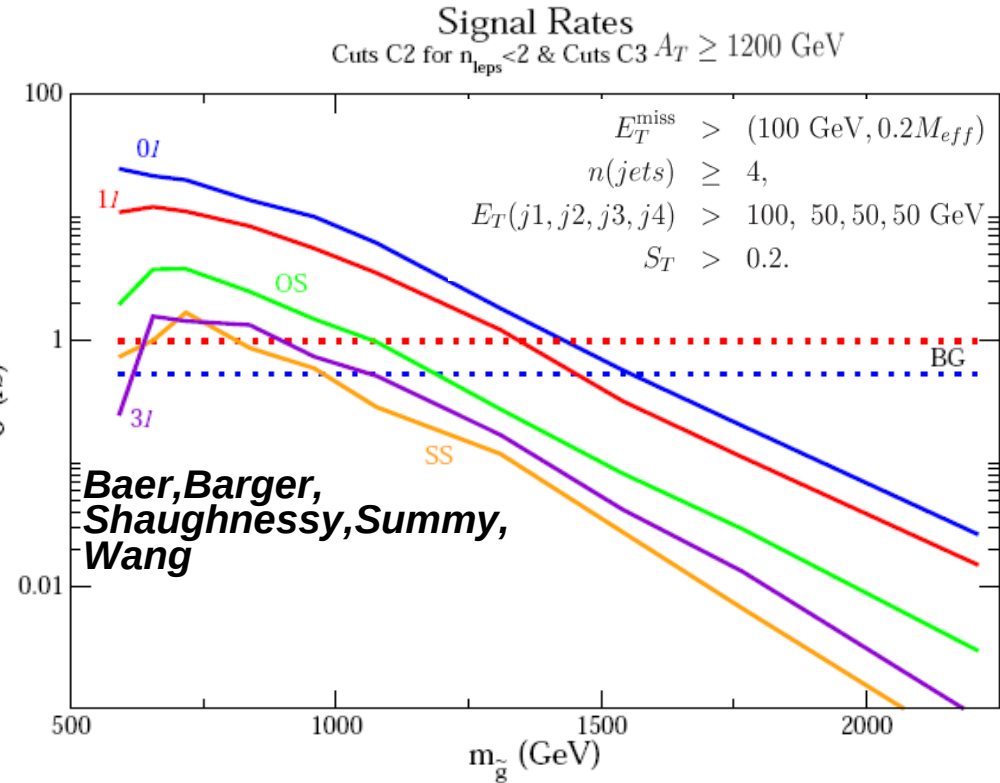
FP cross sections

Baer et al'07

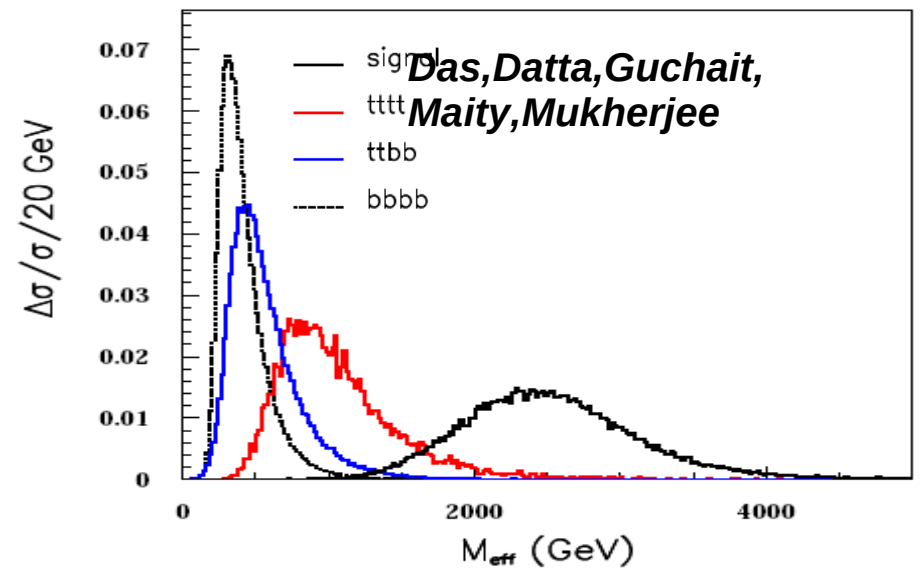


Recent Studies in FP region

Point	m_0	$m_{1/2}$	$M_{\tilde{g}}$	$\delta M_{\tilde{g}}/M_{\tilde{g}}$	$\Gamma_{\tilde{g}}$
FP0	2300	200	591	LEP2 excl.	0.2
FP1	2450	225	655	LEP2 excl.	0.4
FP2	2550	250	717	$\pm 10\%$	0.6
FP3	2700	300	838	$\pm 8\%$	1.1
FP4	2910	350	959	$\pm 7\%$	1.8
FP5	3050	400	1076	$\pm 8\%$	2.7
FP6	3410	500	1310	$\pm 8\%$	5.1
FP7	3755	600	1540	—	8.1
FP8	4100	700	1766	—	11.8
FP9	4716	900	2211	—	20.7



Bednyakov, Budagov, Gladyshev, Kazakov, Khorauli, Khubua, Khramov

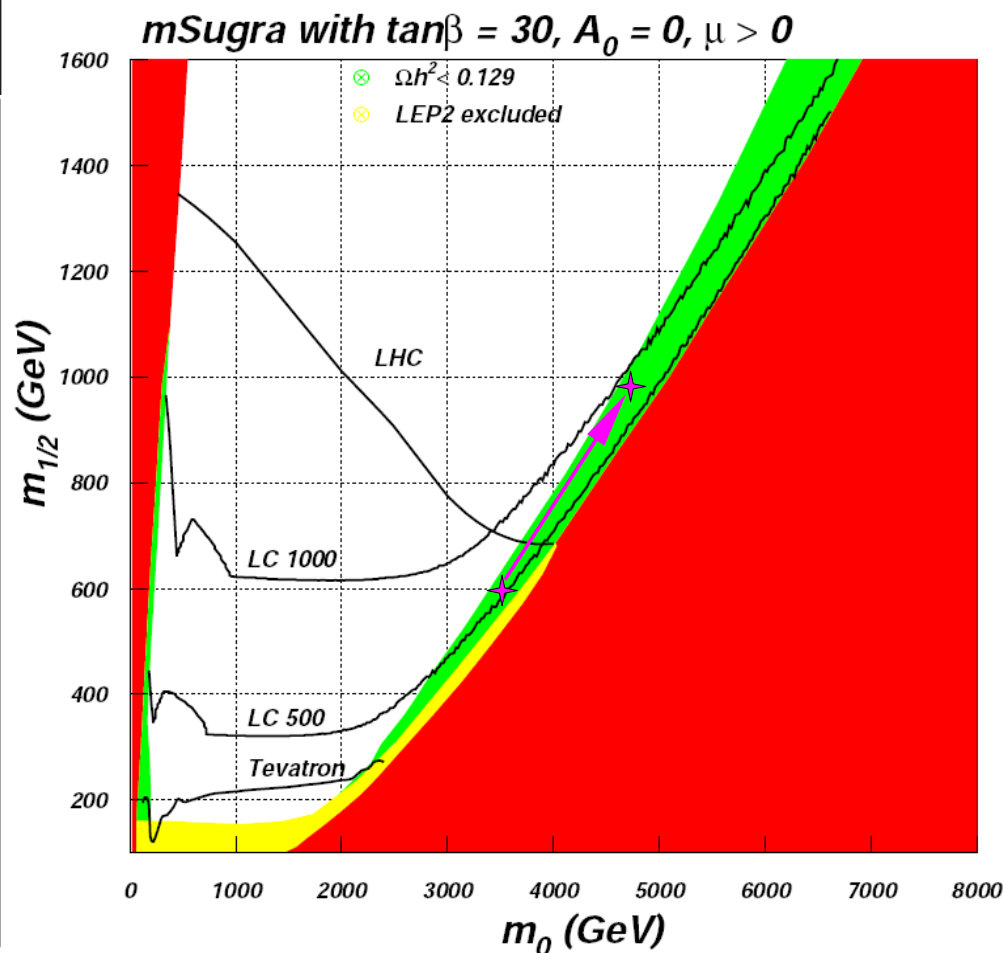


'Far' FP analysis at the LHC

A.B, Genest, Leroy, Mehdiyev'07

- **'far'** FP region dominated by EW chargino-neutralino production - requires special cuts/analysis
- the signal observation in the **'far'** FP region could be crucial for the fate of ILC

Particle	[3500,600] GeV Mass(GeV)	[4670,975] GeV Mass(GeV)
\tilde{Z}_1	239.12	403.54
\tilde{Z}_2	317.22	485.37
\tilde{Z}_3	324.92	486.23
\tilde{Z}_4	528.59	841.62
\tilde{W}_1^\pm	315.53	488.41
\tilde{W}_2^\pm	517.21	832.74
\tilde{g}	1531.37	2365.94
\tilde{u}_L	3653.71	4976.93
h	120.80	122.14
H^0	3033.45	4085.70
A^0	3013.62	4058.99
H^\pm	3034.72	4086.65



Improved strategy: softer preselection + new kinematical cuts

Cut Set 3 The pre-selection cuts

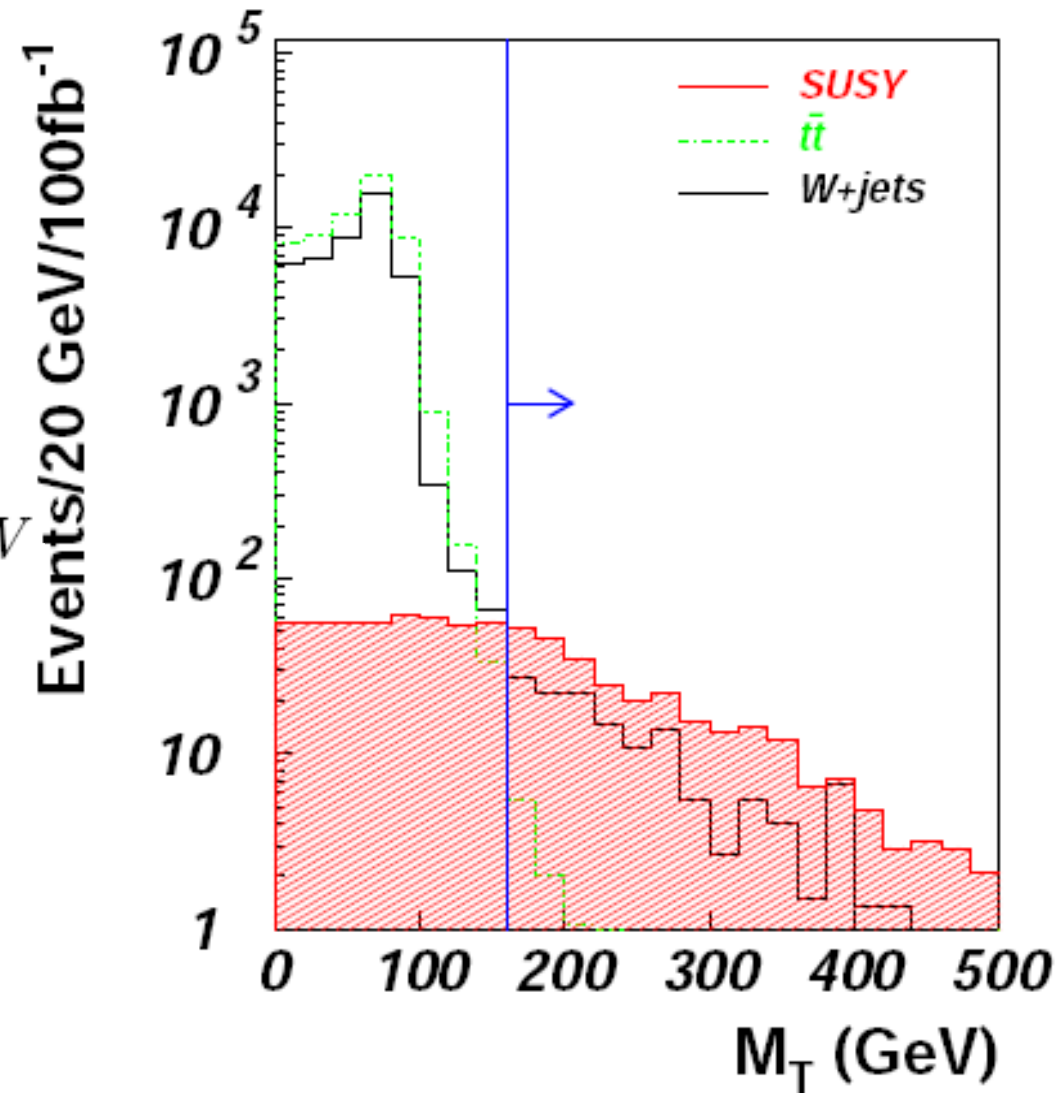
- One lepton with $p_T^{lep} > 20 \text{ GeV}$
- At least four jets with $p_T^J > 20 \text{ GeV}$
- A leading jet with $p_T^{J_1} \geq 40 \text{ GeV}$
- $\cancel{E}_T \geq 200 \text{ GeV}$.
- $M_{jj} = \sqrt{((\sum E_i)^2 - (\sum \vec{p}_i)^2)} > 60 \text{ GeV}$

Cut Set 4 The analysis cuts

- $N_j \quad \cancel{E}_T$.
- $p_T^{lep(max)}$
- transverse mass of the lepton and missing energy,

$$M_T = \sqrt{2p_T^{lep} \cancel{E}_T (1 - \cos\phi(\cancel{E}_T, p_T^{lep}))}$$

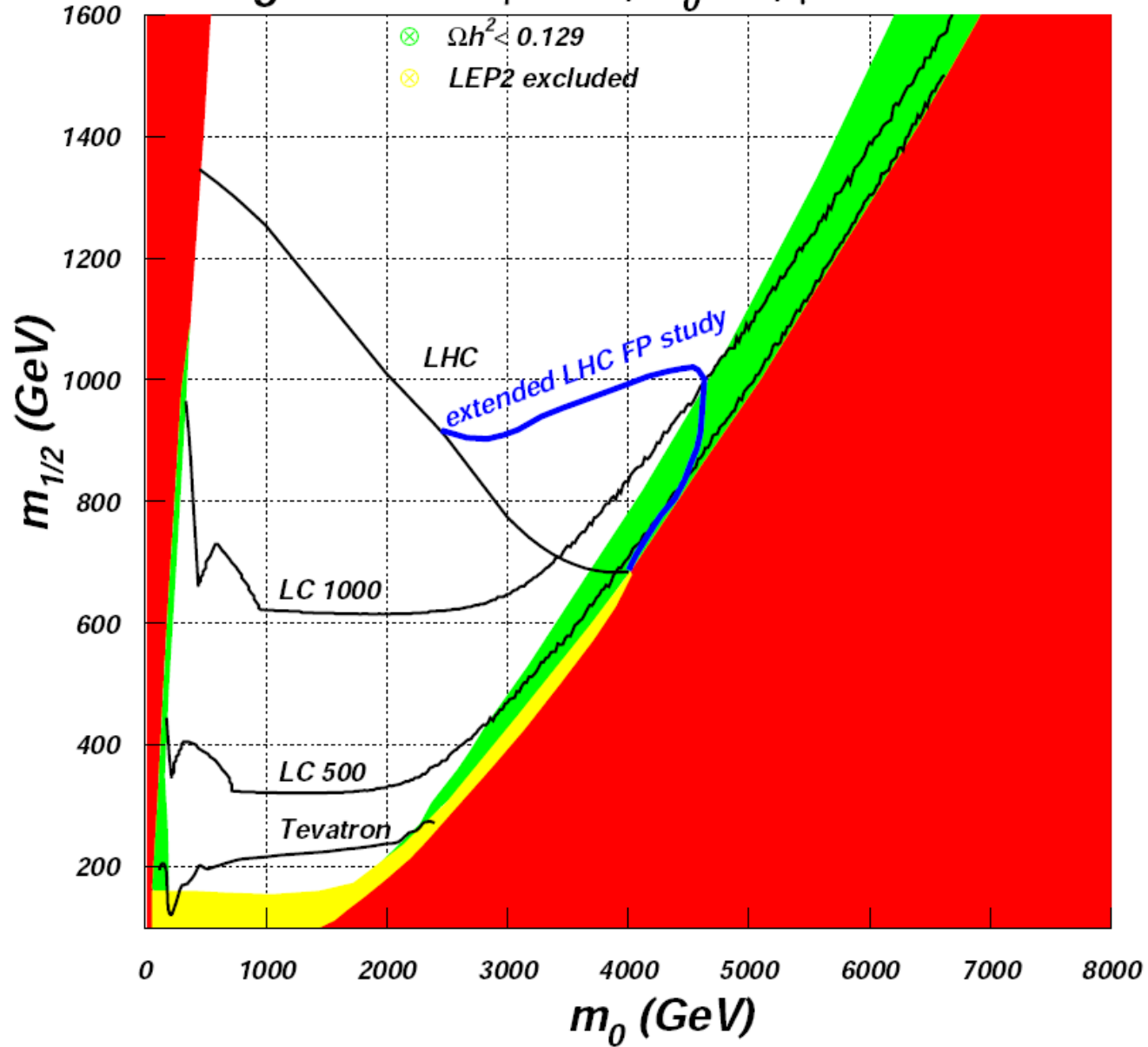
- $R = p_T^{J_1} / \left| \sum_i \vec{p}_{T,i} \right|$.



$$M_T = \sqrt{2p_T(l) \cancel{E}_T (1 - \cos\phi(\cancel{E}_T, p_T(l)))}$$

Extended LHC reach

mSugra with $\tan\beta = 30, A_0 = 0, \mu > 0$



A.B, Genest, Leroy, Mehdiyev'07

Relative contributions of SUSY subprocesses (after cuts)

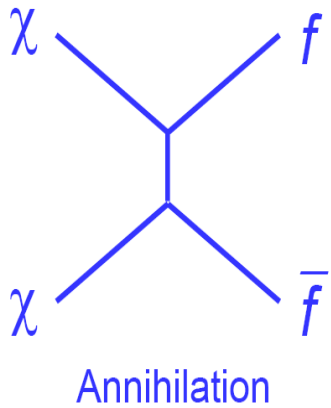
Selected sparticles	[3500,600] GeV	[4670,975] GeV
	Fraction of SUSY events(%)	Fraction of SUSY events(%)
$\tilde{W}_1 + \tilde{W}_1$	8.25	12.60
$\tilde{W}_2 + \tilde{W}_2$	13.59	19.60
$\tilde{W}_1 + \tilde{W}_2$	< 0.49	0.35
$\tilde{Z}_1 + \tilde{W}_1$	2.43	4.90
$\tilde{Z}_1 + \tilde{W}_2$	< 0.49	< 0.35
$\tilde{Z}_2 + \tilde{W}_1$	6.31	14.00
$\tilde{Z}_2 + \tilde{W}_2$	< 0.49	0.30
$\tilde{Z}_3 + \tilde{W}_1$	7.77	12.90
$\tilde{Z}_3 + \tilde{W}_2$	0.97	0.35
$\tilde{Z}_4 + \tilde{W}_2$	26.21	31.50
$\tilde{Z}_4 + \tilde{W}_1$	1.94	0.70
$\tilde{Z}_1 + \tilde{Z}_1$	< 0.49	< 0.35
$\tilde{Z}_1 + \tilde{Z}_2$	< 0.49	< 0.35
$\tilde{Z}_1 + \tilde{Z}_3$	0.49	< 0.35
$\tilde{Z}_2 + \tilde{Z}_3$	0.49	0.70
$\tilde{Z}_2 + \tilde{Z}_4$	< 0.49	0.35
$\tilde{Z}_3 + \tilde{Z}_3$	< 0.49	< 0.35
$\tilde{g} + \tilde{g}$	29.61	1.40

Complementarity of Direct and Indirect DM search

Baer, A.B., Krupovnikas, O'Farrill '04

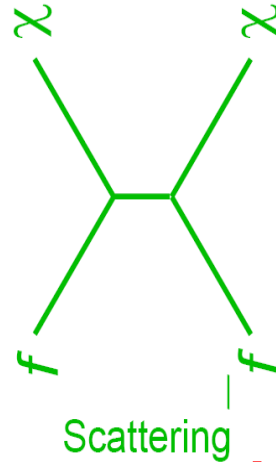
mSUGRA, $A_0=0$, $\tan\beta=55$, $\mu>0$

DM direct detection:
neutralino scattering off nuclei



Isared code

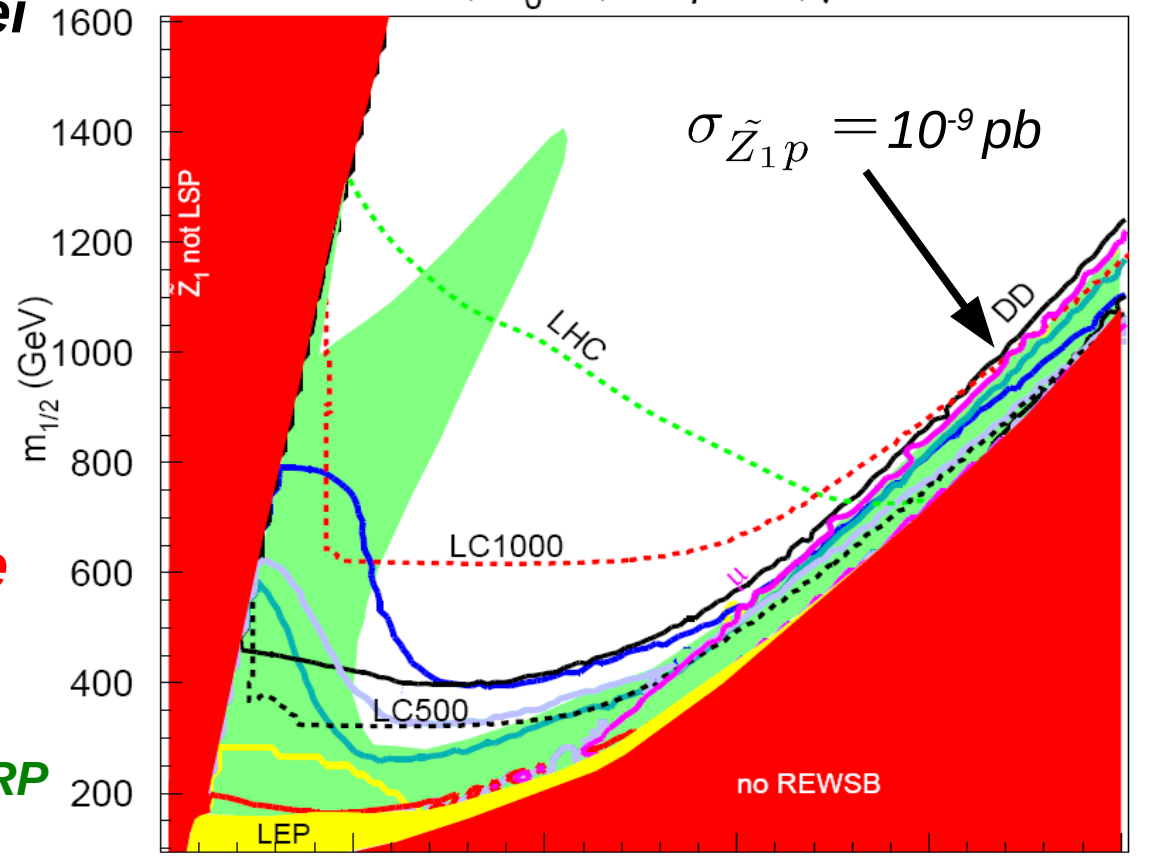
Crossing
symmetry
→



Isares code

- Stage 1: CDMS1, Edelweiss, Zeplin1
- Stage 2: CDMS2, CRESST2, Zeplin2
- Stage 3: SuperCDMS, Zeplin 1 ton, WARP

DM indirect detection:
signatures from neutralino annihilation
in halo, core of the Earth and Sun
photons, anti-protons, positrons, neutrinos

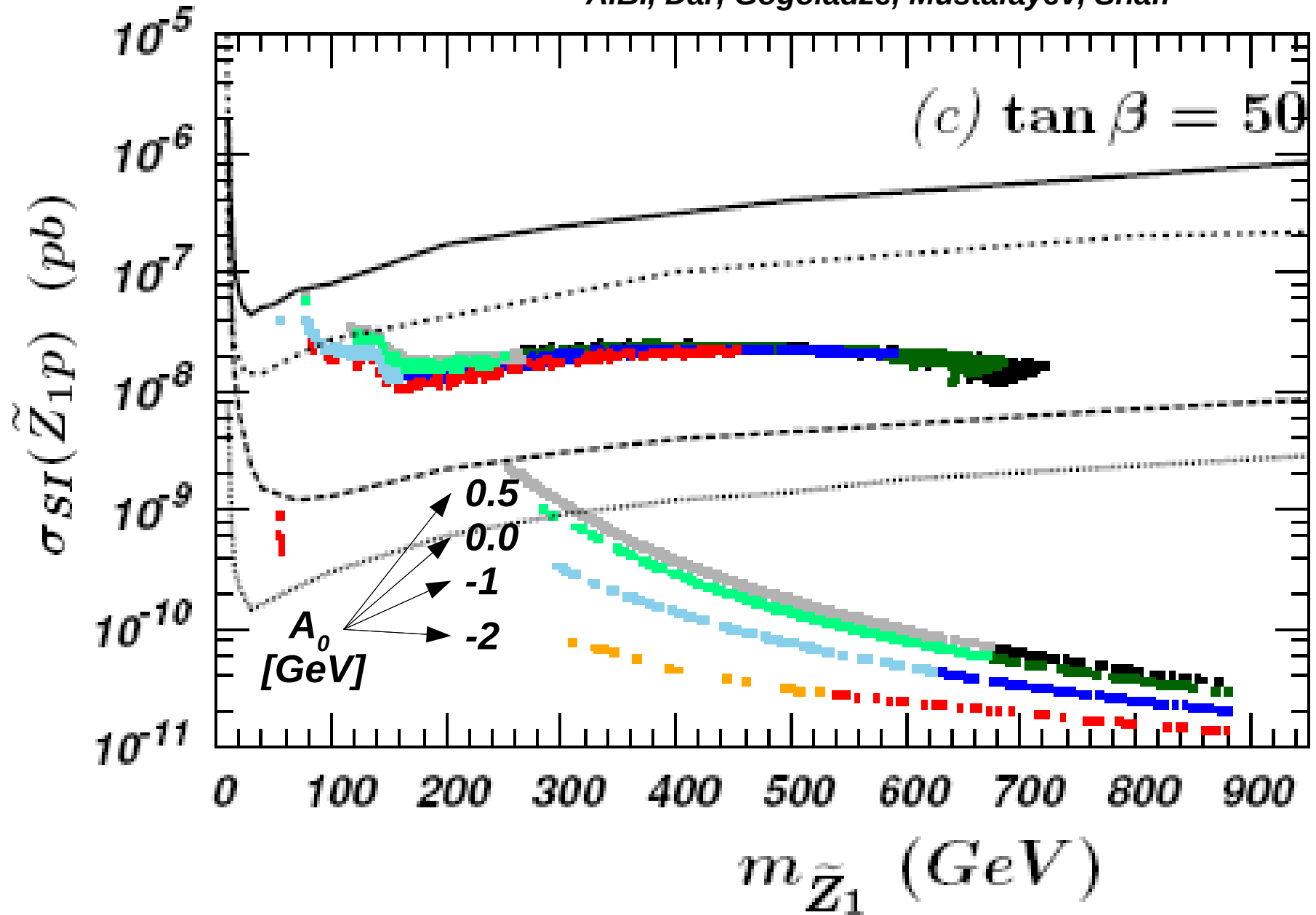


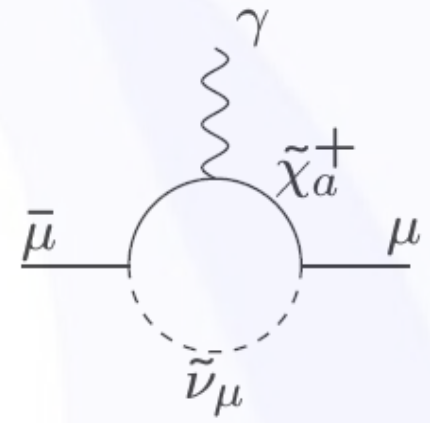
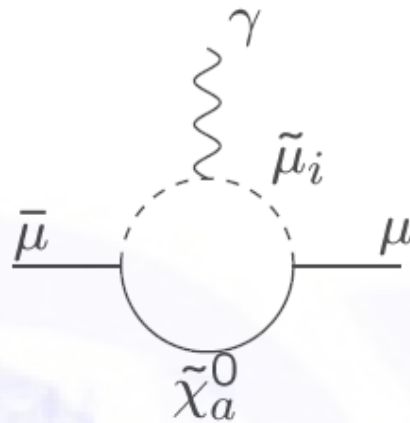
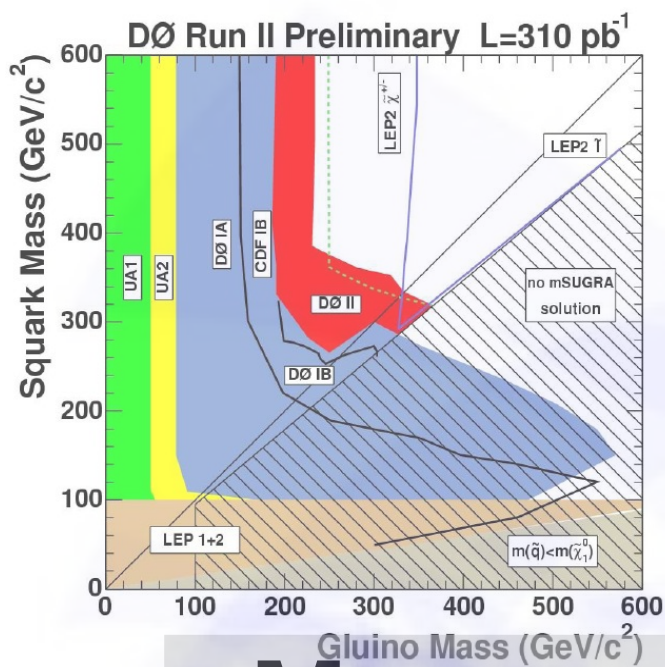
- $\Phi(p^-) = 3e^{-7} \text{ GeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$
- $\Phi(\gamma) = 10^{-10} \text{ cm}^{-2} \text{ s}^{-1}$
- $\Phi^{\text{earth}}(\mu) = 40 \text{ km}^{-2} \text{ yr}^{-1}$
- $\Phi^{\text{sun}}(\mu) = 40 \text{ km}^{-2} \text{ yr}^{-1}$
- $m_h = 114.4 \text{ GeV}$
- $(S/B)_{e^+} = 0.01$
- $\sigma(\tilde{Z}_1 p) = 10^{-9} \text{ pb}$
- $0 < \Omega h^2 < 0.129$

Neutrino telescopes: Amanda, Icecube, Antares

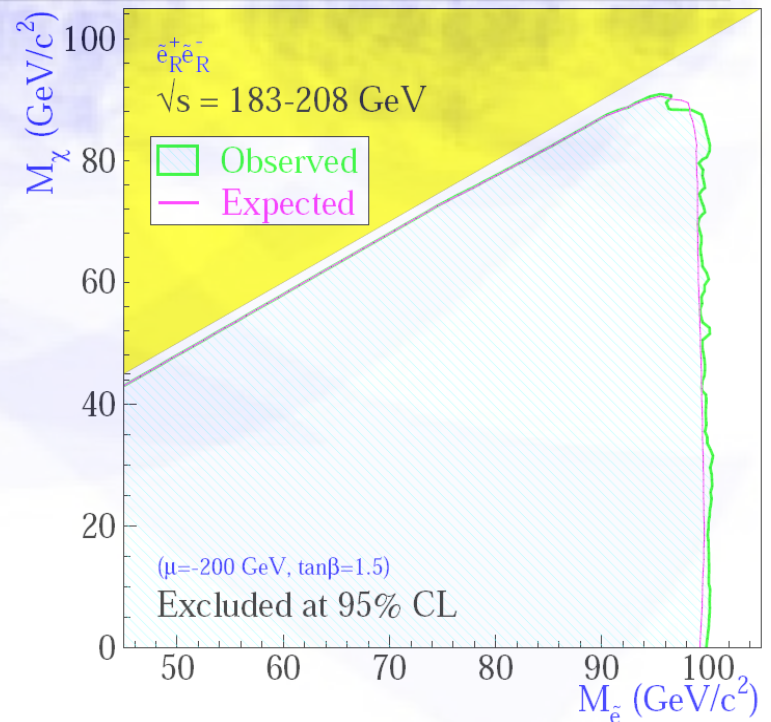
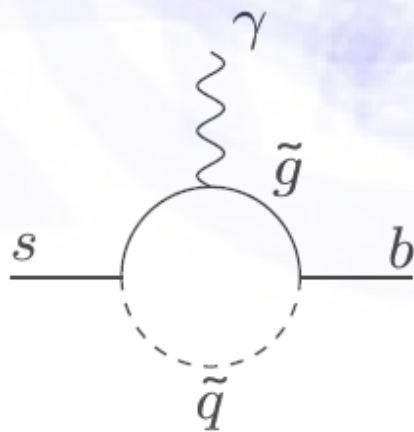
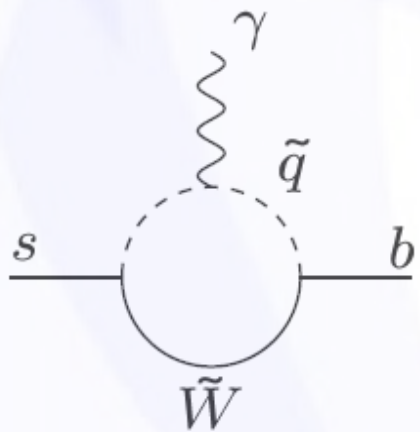
mSUGRA DD search

A.B., Dar, Gogoladze, Mustafayev, Shafi





More on SUSY constraints ...

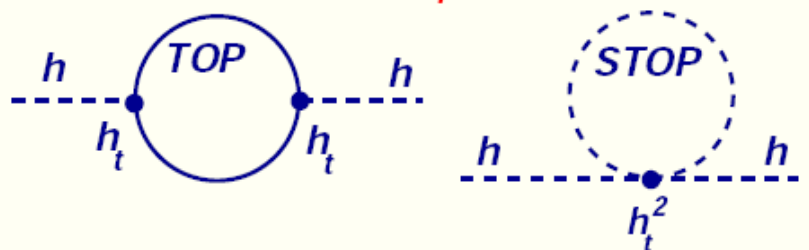


LEP2 constraints

- Light Higgs mass and LEP2 constraints: $M_H^{SM} > 114$ GeV pushes SUSY scale to 1TeV

$$M_h^2 = \frac{1}{2} \left[m_A^2 + M_Z^2 - \sqrt{(M_A^2 + M_Z^2)^2 - 4m_A^2 M_Z^2 \cos^2 2\beta} \right] \Rightarrow M_h \simeq M_Z |\cos 2\beta| \text{ for } M_A \gg M_Z$$

Top-stop Radiative corrections to the light Higgs mass drive its mass up!

$$\delta M_h = \frac{3g^2 m_t^4}{8\pi^2 m_W^2} \left[\ln \left(\frac{M_S^2}{m_t^2} \right) + x_t^2 \left(1 - \frac{x_t^2}{12} \right) \right]$$


$M_h \leq 135$ GeV for $M_S \sim 1$ TeV, for $x_t = \sqrt{6}$ (max mixing)

- Top-quark mass and EW fit: $m_t : 170.9 \rightarrow 178.0$ GeV $\Rightarrow M_H : 76 \rightarrow 117.0$ GeV

- LEP2 SUSY particle search

◆ pair slepton production: $e^+ e^- \rightarrow \tilde{\ell}_{L,R}^+ \tilde{\ell}_{L,R}^- \rightarrow l^+ \tilde{Z}_1 l^- \tilde{Z}_1$

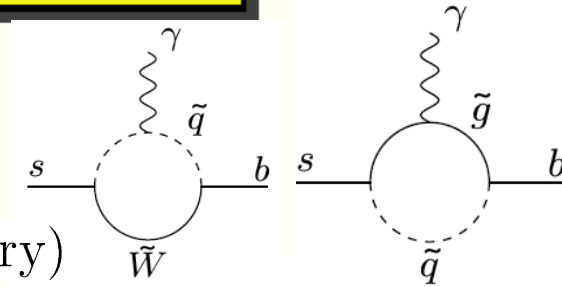
$\Rightarrow m_{\tilde{e}} > 99.6$ GeV, $m_{\tilde{\mu}} > 94.6$ GeV, $m_{\tilde{\tau}} > 85.9$ GeV

◆ pair chargino production: $e^+ e^- \rightarrow \tilde{W}_1^+ \tilde{W}_1^-$, $\tilde{W}_1 \rightarrow \tilde{Z}_1 l \nu (\tilde{Z}_1 q q')$, $\Rightarrow m_{\tilde{W}_1} \gtrsim 100$ GeV

$b \rightarrow s\gamma, (g-2)_\mu/2, B_s \rightarrow \mu^+ \mu^-$ constraints

◆ $b \rightarrow s\gamma$: $BF(b \rightarrow s\gamma) = (3.55 \pm 0.26) \times 10^{-4}$ [BELLE, CLEO and ALEPH]

Theory: $(3.15 \pm 0.23) \times 10^{-4}$ **Misiak, Steinhauser '06**



$2.85 \times 10^{-4} \leq Br(b \rightarrow s\gamma) \leq 4.24 \times 10^{-4}$ (95% CL incl 10% theory)

no significant deviation from SM $\implies m_{\tilde{t}_{1,2}}, m_{\tilde{W}_{1,2}}, m_{H^\pm}$ should be heavy! $BR(b \rightarrow s\gamma)|_{\chi^\pm} \propto \mu A_t \tan \beta$

◆ $(g-2)_\mu/2$ results

$(g-2)_\mu/2 = 11659 208(6)$ [g-2 collaboration] **← experiment**

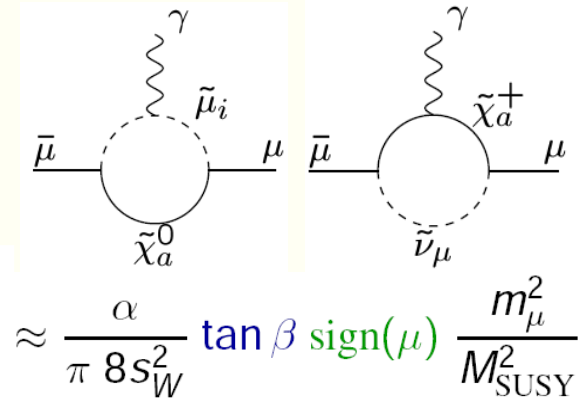
$\Delta a_\mu = (27.1 \pm 9.4) \times 10^{-10}$ (Davier et al.) **← Theory based on e+e- data**

$\Delta a_\mu = (31.7 \pm 9.5) \times 10^{-10}$ (Hagiwara et al.)

(τ decay data $\Delta a_\mu = (12.4 \pm 8.3) \times 10^{-10}$ (Davier et al.))

There are growing consensus that $e^+ e^-$ data are more to be trusted since they offer a direct determination of the hadronic vacuum polarization

$\sim 3\sigma \implies$ second generation of slepton are relatively light!



◆ $BF(B_s \rightarrow \mu^+ \mu^-) < 1.0 \times 10^{-7}$ (CDF), (SM: 3.4×10^{-9})

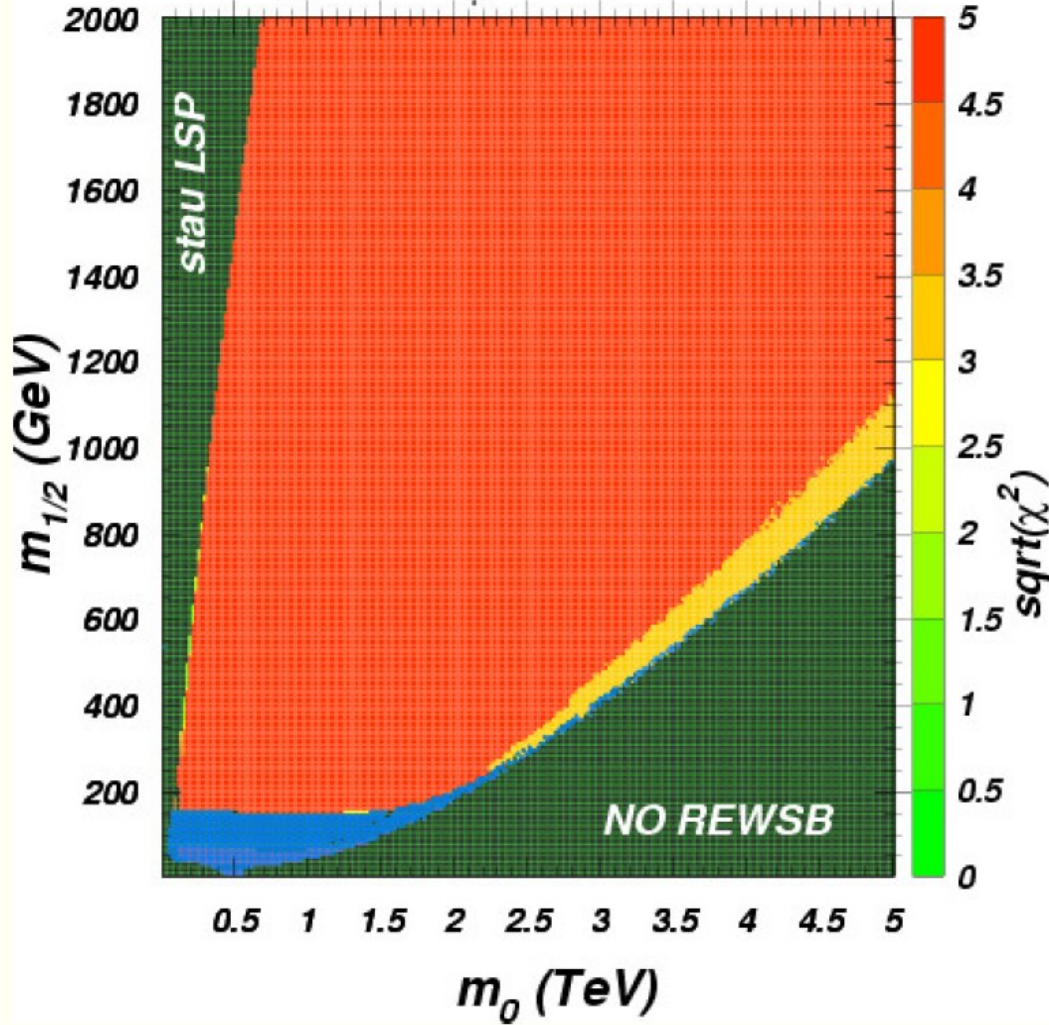
amplitude for H-mediated decay grows as $\tan \beta^3$ (!) \implies relevant to high $\tan \beta$ scenario

[Babu, Kolda; Dedes, Dreiner, Nierste; Arnowitt, Dutta, Tanaka; Mizukoshi, Tata, Wang]

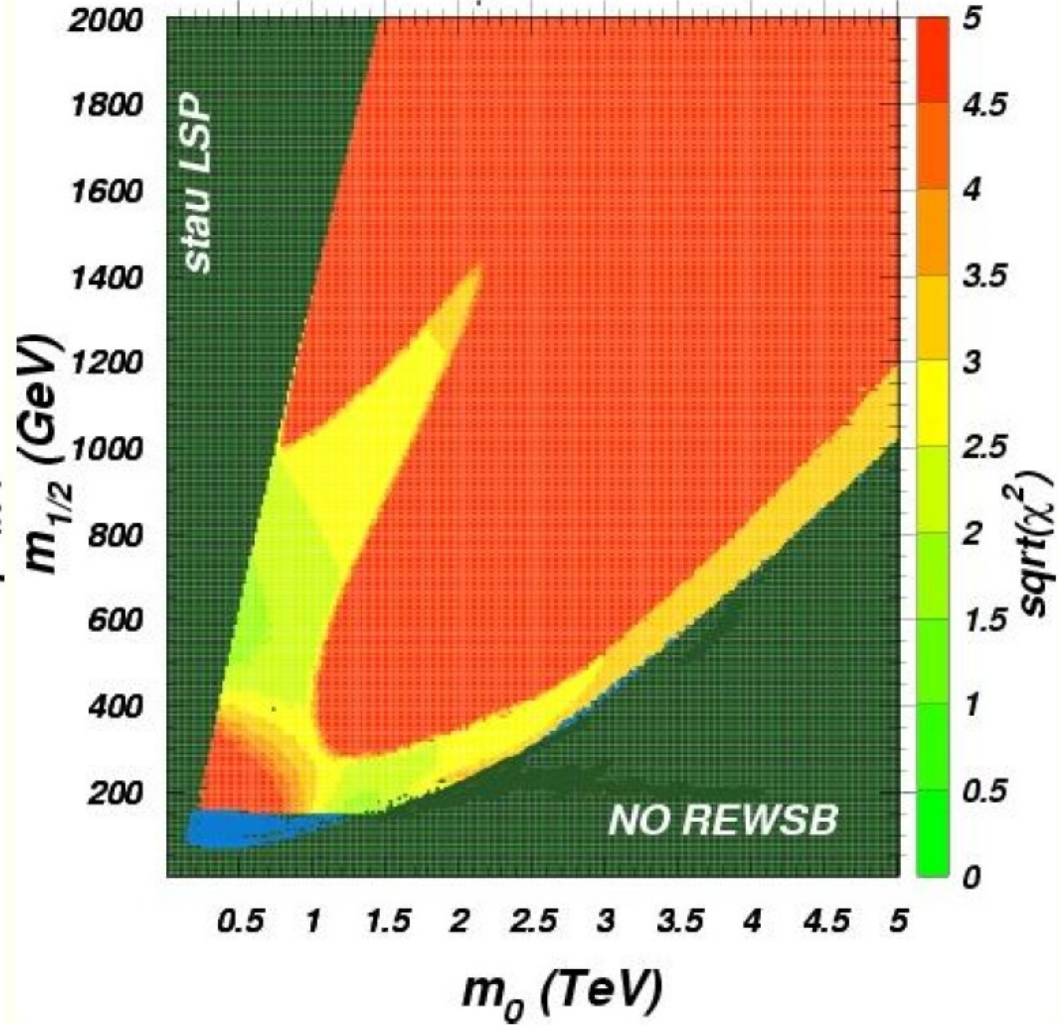
mSUGRA: $\chi^2 = \chi_{\delta a_\mu}^2 + \chi_{\Omega h^2}^2 + \chi_{b \rightarrow s \gamma}^2$ analysis

◆ Δa_μ favors light second generation sleptons, while $BF(b \rightarrow s \gamma)$ prefers heavy third generation: *hard to realize in mSUGRA model.*

mSUGRA, $\tan\beta=30$, $\mu>0$, $A_0=0$, $m_{top}=175$ GeV
 e^+e^- input for δa_μ ● LEP2 excluded



mSUGRA, $\tan\beta=55$, $\mu>0$, $A_0=0$, $m_{top}=175$ GeV
 e^+e^- input for δa_μ ● LEP2 excluded

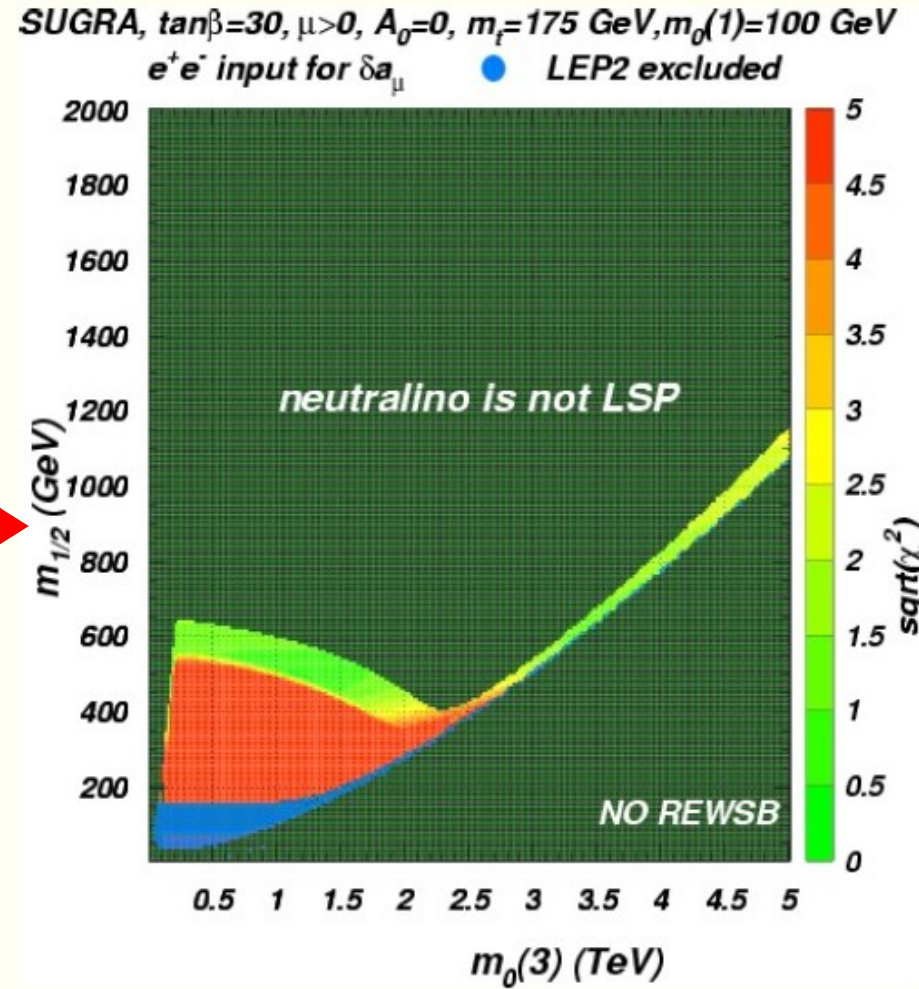
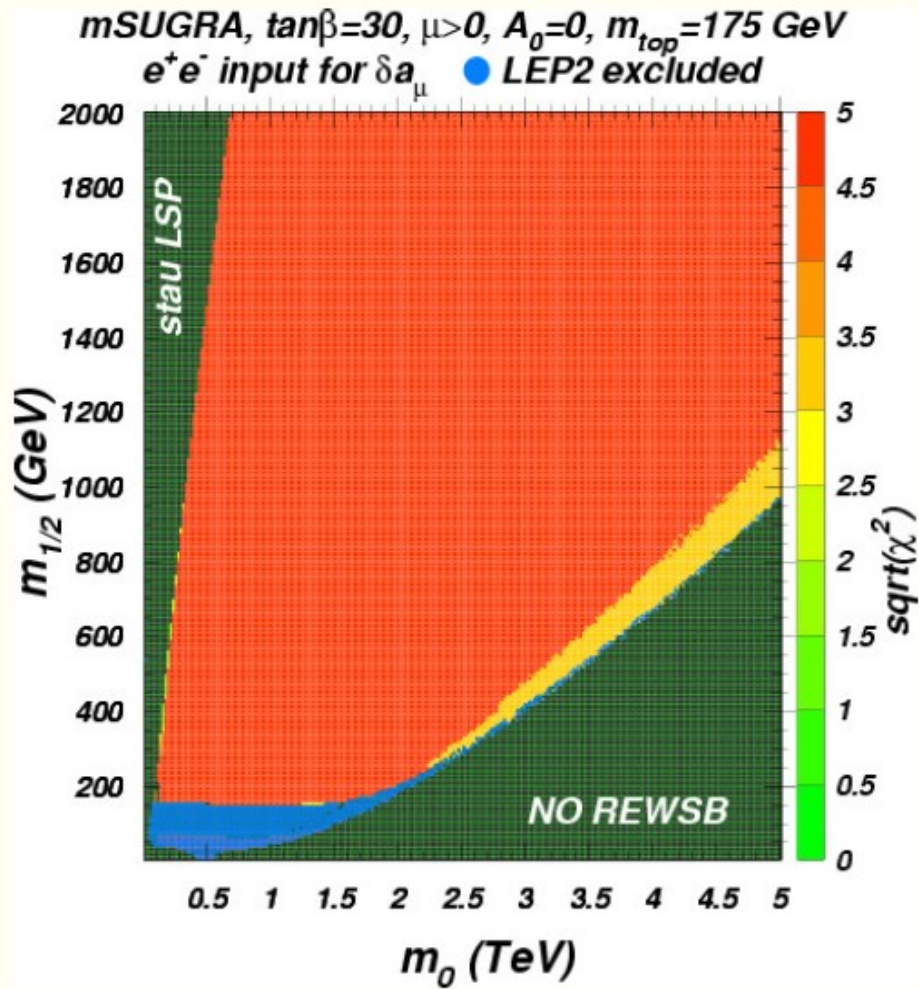


Baer, A.B., Krupovnickas, Mustafayev hep-ph/0403214

SUGRA: normal mass hierarchy (NMH)

◆ Δa_μ favors light second generation sleptons, while $BF(b \rightarrow s\gamma)$ prefers heavy third generation: *hard to realize in mSUGRA model.*

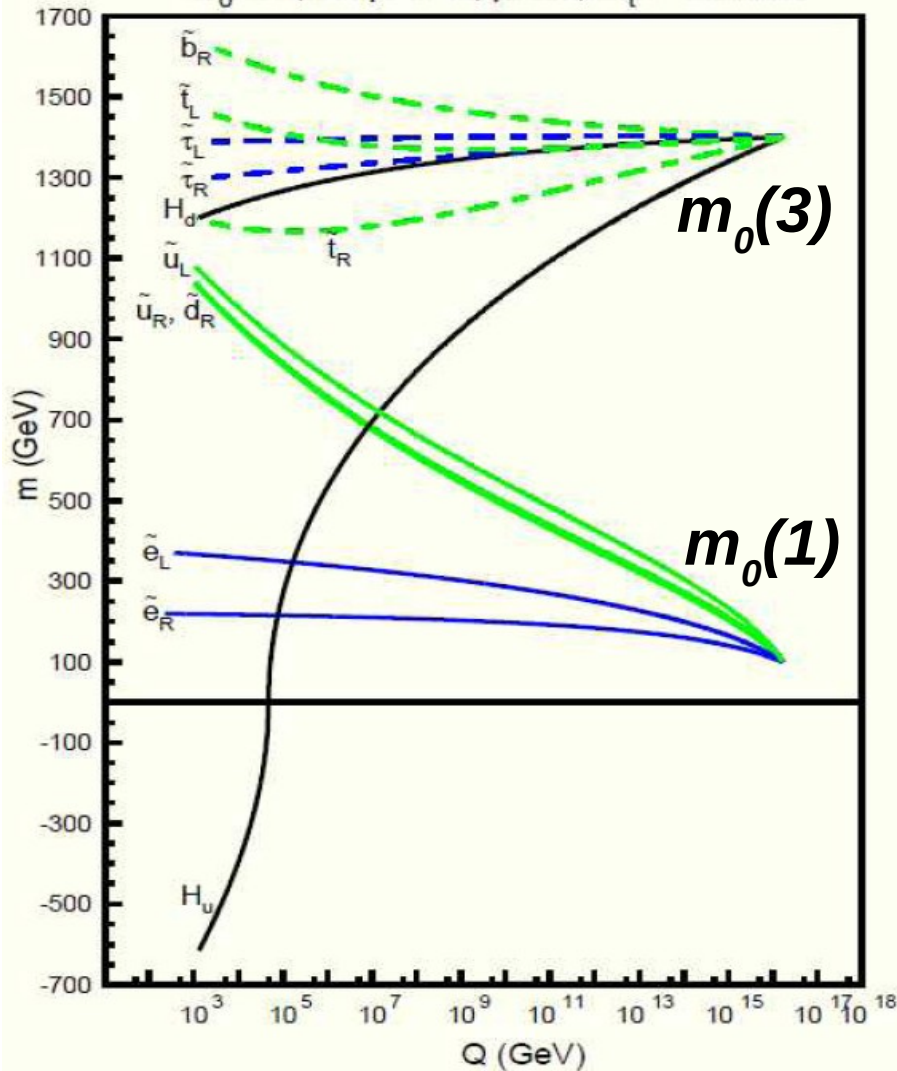
◆ one step beyond universality solves the problem! [Baer, AB, Krupovnikas, Mustafayev]
 $[m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)] \rightarrow [m_0(1), m_0(3), m_H, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)]$



◆ $B_H^0 - B_L^0 = \Delta m_B$ mass splitting bound is safe

NMH: SUSY spectra and LHC signatures

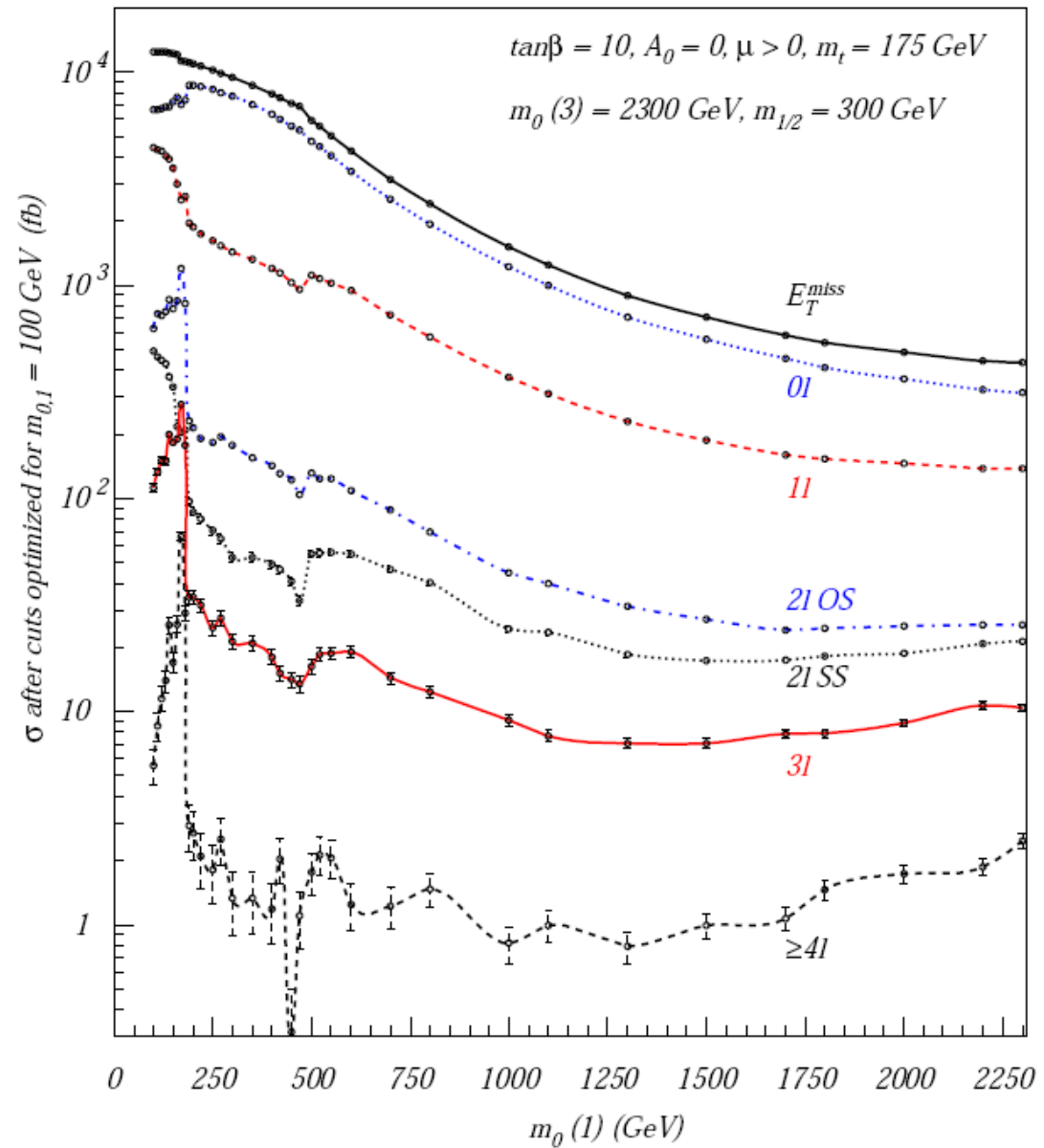
$m_0(1) = 0.1\text{TeV}$, $m_0(3) = 1.4\text{TeV}$, $m_{1/2} = 550\text{GeV}$
 $A_0 = 0$, $\tan\beta = 30$, $\mu > 0$, $m_t = 175\text{GeV}$



$$m_{\tilde{q}}^2 \simeq m_0^2 + (5 - 6)m_{1/2}^2$$

$$m_{\tilde{\ell}}^2 \simeq m_0^2 + (0.15 - 0.5)m_{1/2}^2$$

LHC



Scenario with non-universal Higgs masses (NUHM)

- ▶ *universality of m_0 is motivated by the need to suppress unwanted flavor changing processes (generation blind mech for matter scalars in SUSY GUTs)*
- ▶ *this does not apply to soft breaking Higgs masses. In $SO(10)$ SUSY GUTs: $(10 + \bar{5} + \bar{\nu}) \in \hat{\psi}(16)$, $(5_H, \bar{5}_H) \in \hat{\phi}(10)$, different repres \Rightarrow SUSY breaking scalar mass terms for $\hat{\psi}(16)$ and $\hat{\phi}(10)$ are not expected to be the same*

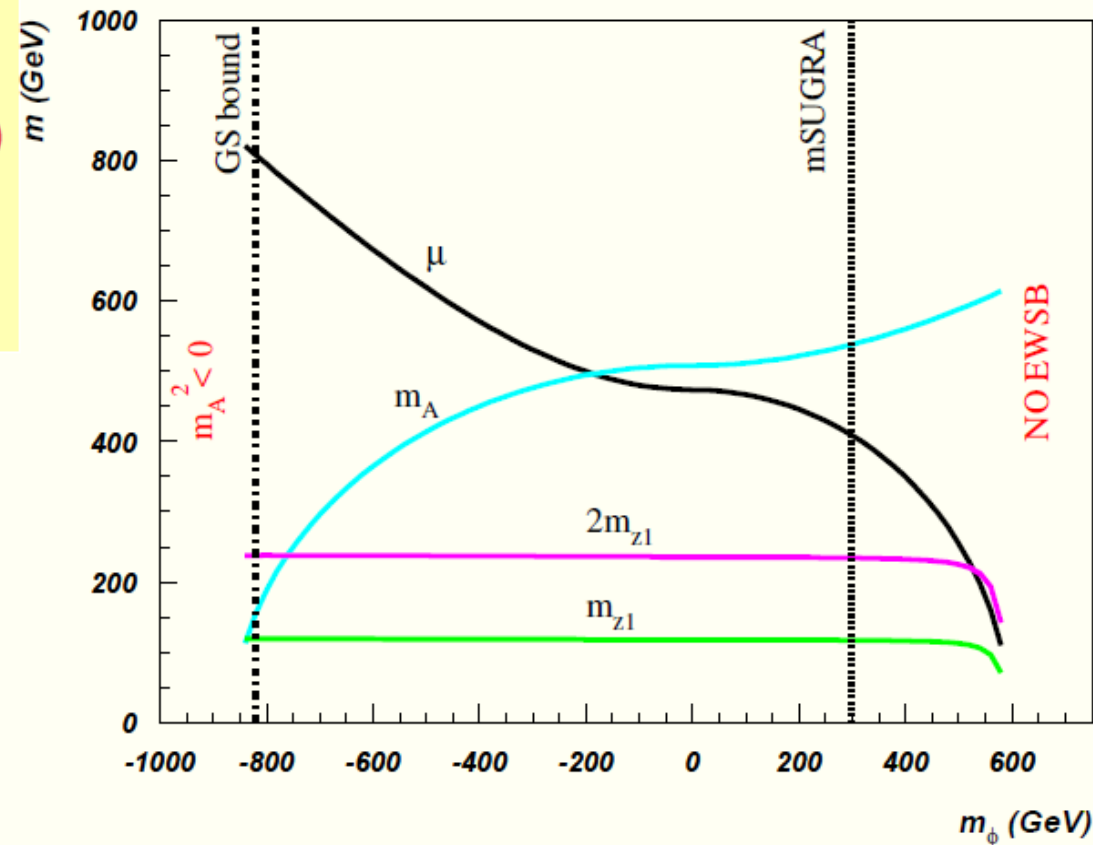
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the minimal non-universal Higgs extension of mSUGRA \Rightarrow NUHM1:
 $m_0, m_\phi, m_{1/2}, A_0, \tan\beta$ and $sign(\mu)$
 $m_\phi = sign(m_{H_{u,d}}^2) \cdot \sqrt{|m_{H_{u,d}}^2|}$
 $m_{H_{u,d}}^2$ are allowed to be negative

- ▶ μ becomes small for $m_\phi > m_0 \Rightarrow$ FP! can be reached even for low m_0 and $m_{1/2}$!
- ▶ M_A decrease down to $2m_{\tilde{Z}_1}$ for m_ϕ going down \Rightarrow Funnel! Even for low $\tan\beta$! Requires $m_\phi^2 < 0$.

$m_0 = 300\text{GeV}, m_{1/2} = 300\text{GeV}, \tan\beta = 10, A_0 = 0, \mu > 0, m_t = 178\text{GeV}$



Baer, Belyaev, Mustafayev, Profumo, Tata

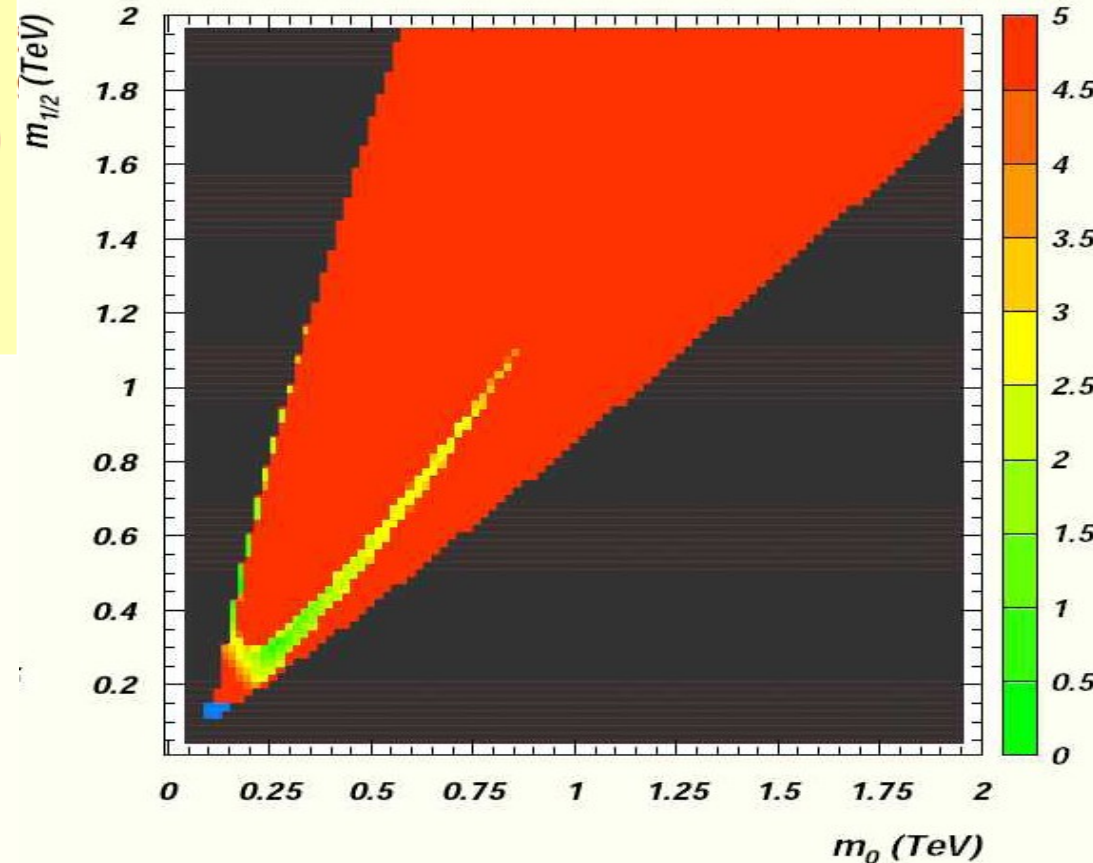
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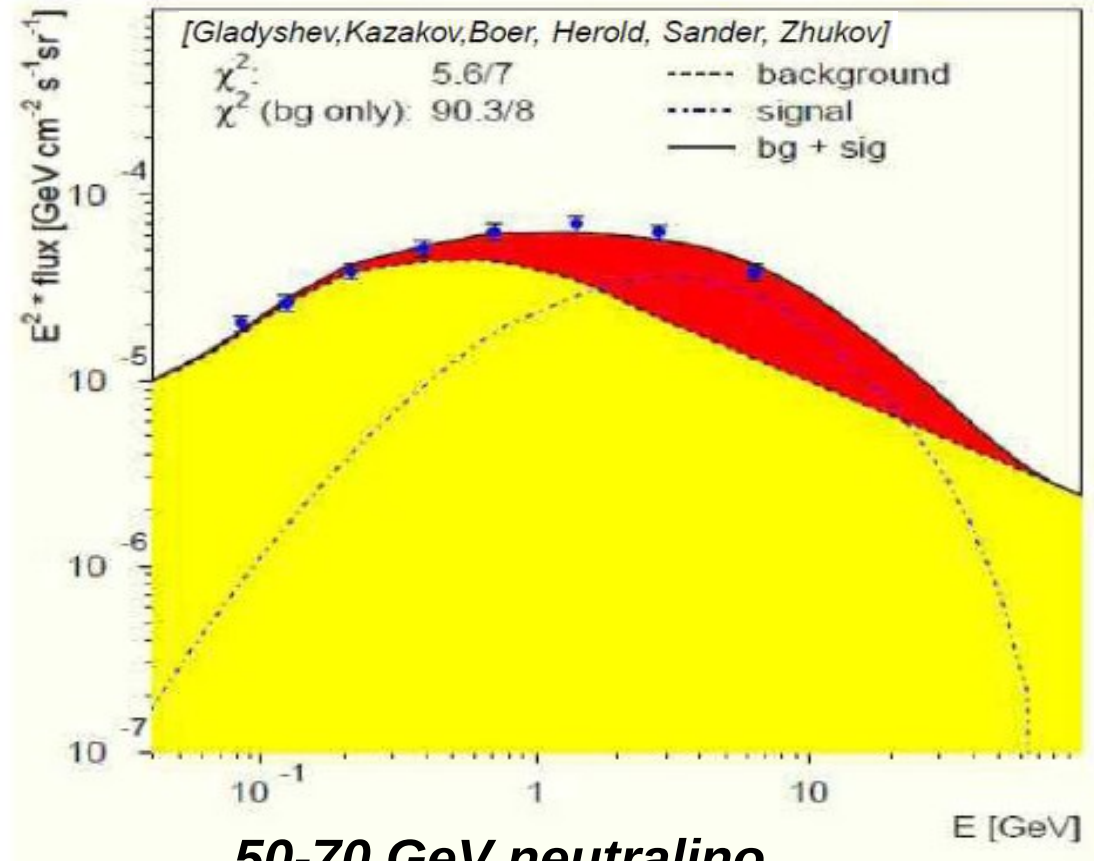
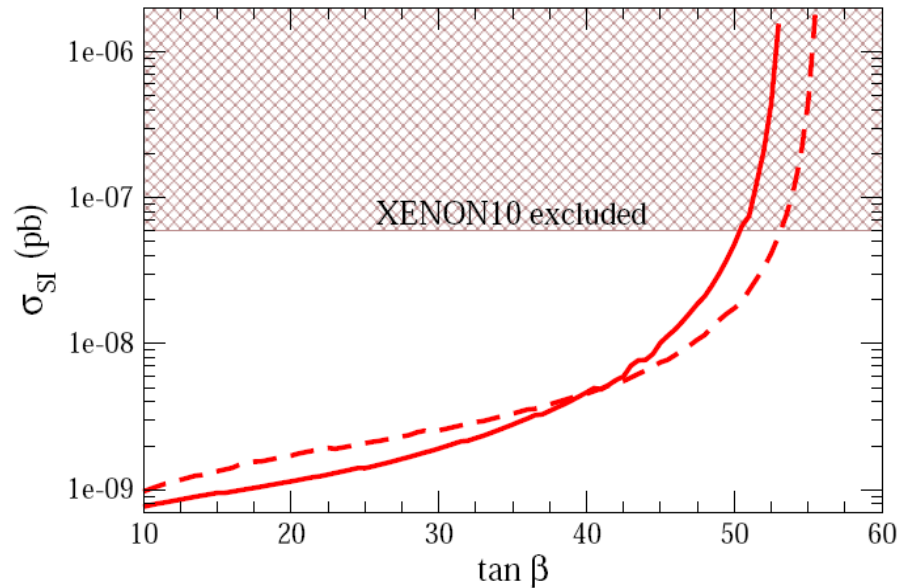
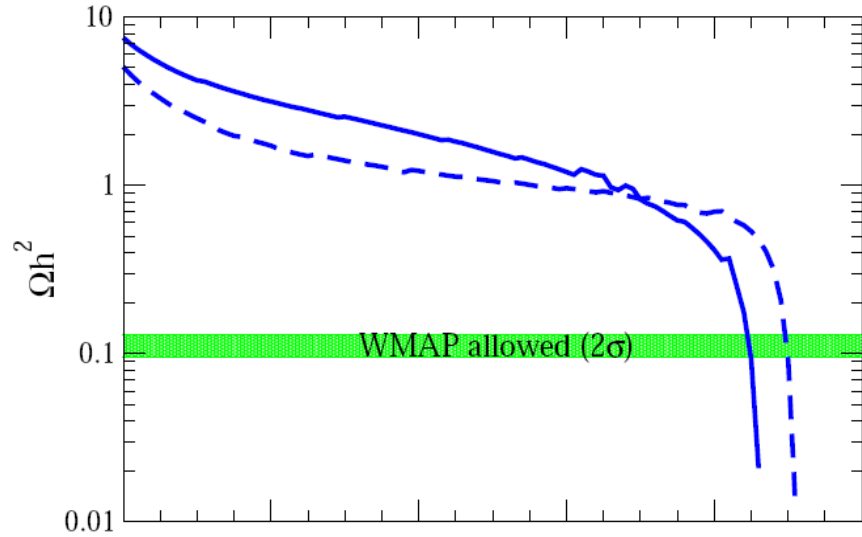
NUHM1: $\tan \beta = 35, m_\phi = -2.5m_\sigma, \mu > 0, A_0 = 0, m_t = 178 \text{ GeV}$



Baer, Belyaev, Mustafayev, Profumo, Tata

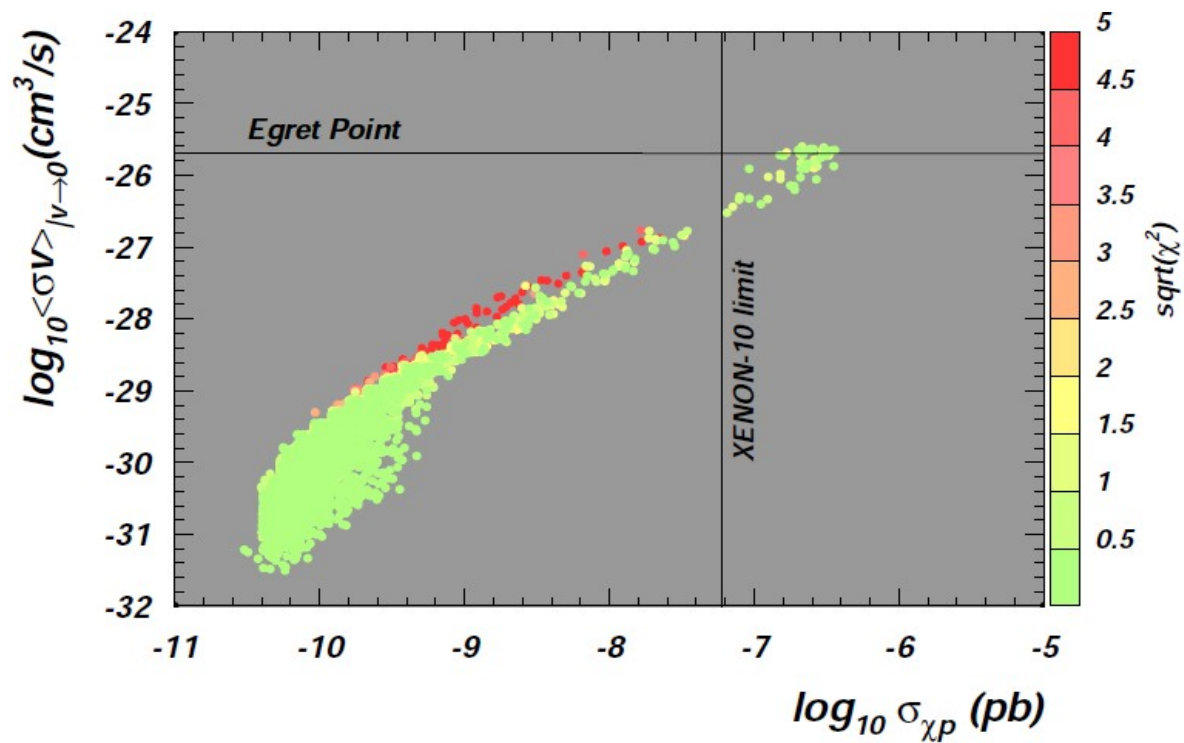
Complementarity of DD DM search: Xenon-10 constraints and “Egret” mSUGRA point

Solid Lines: $m_t=171.0, A_0=-900$ Dashed Lines: $m_t=175.0, A_0=0$
 $m_0=1500, m_{1/2}=160, \text{sgn}(\mu)=+1, \text{incr}(\tan\beta)=0.5$

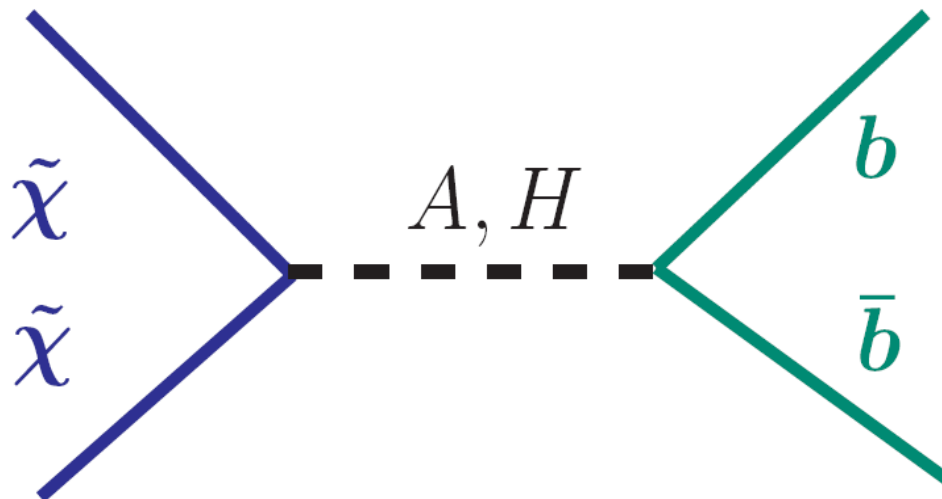


**50-70 GeV neutralino
 provides a good fit
 $m_0 = 1400$ GeV
 $m_{1/2} = 180$ GeV
 $\tan\beta = 0.5 m_0$
 are suggested**

mSUGRA and NUHM2 scenarios for Egret data

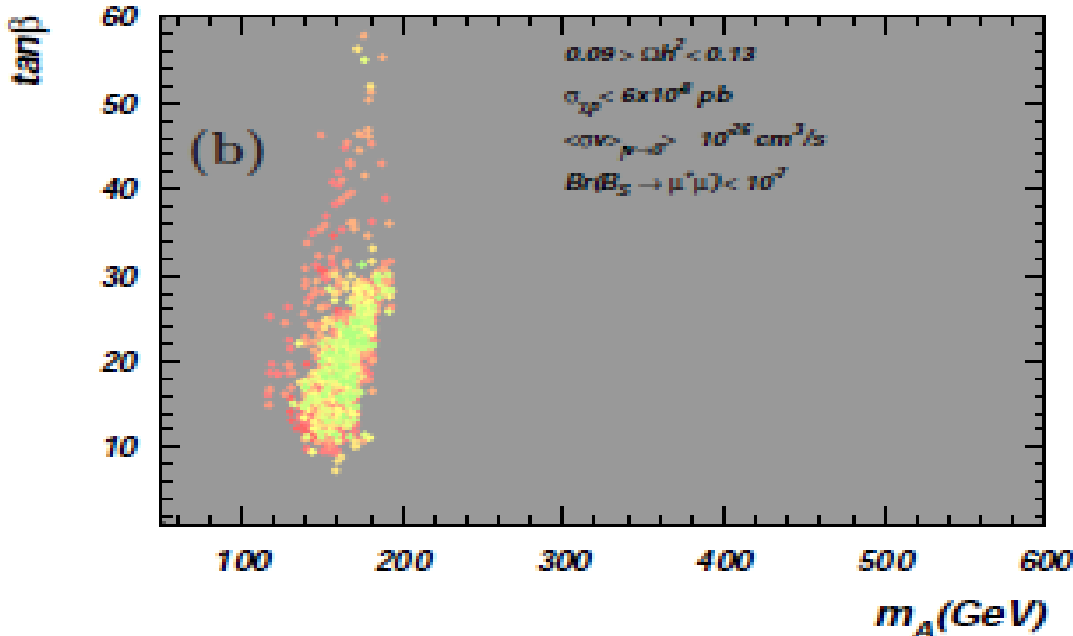
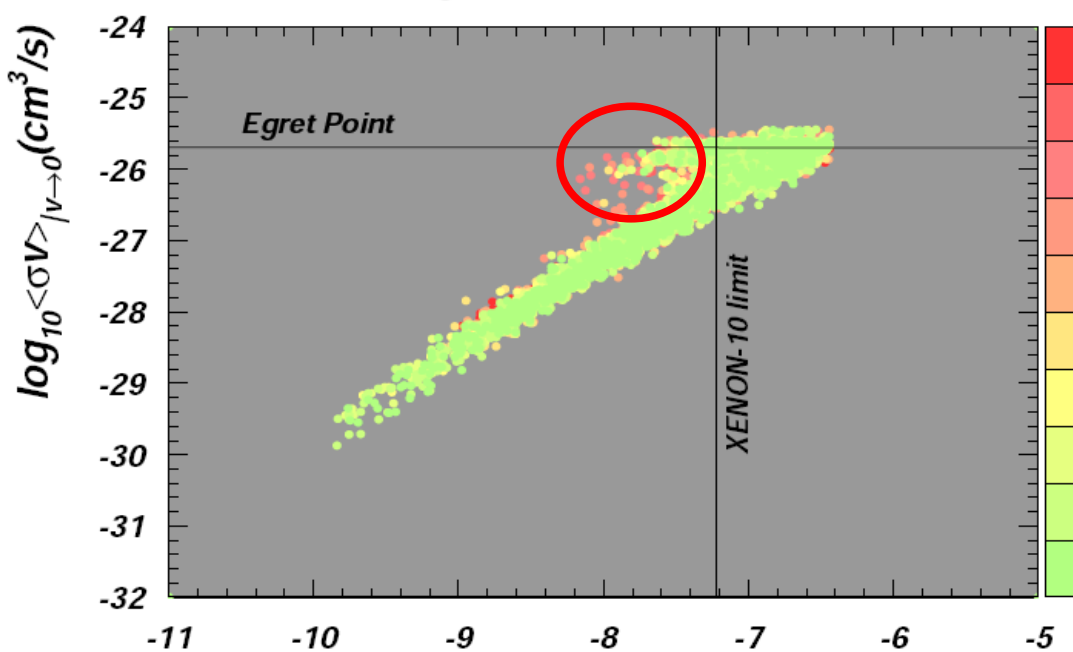


parameter	mSUGRA(171)	NUHM
m_0	1500	831.8
$m_{1/2}$	160	161.2
A_0	-900	-1597.1
$\tan\beta$	52.1	17.6
m_t	170.9	170.9
μ	177.5	644.0
$m_{\tilde{g}}$	476.9	450.8
$m_{\tilde{u}_L}$	1522.8	891.1
$m_{\tilde{u}_R}$	1526.5	914.4
$m_{\tilde{t}_1}$	890.7	248.3
$m_{\tilde{b}_1}$	1025.0	632.2
$m_{\tilde{e}_L}$	1501.6	853.6
$m_{\tilde{e}_R}$	1499.8	802.4
$m_{\tilde{W}_1}$	106.3	131.7
$m_{\tilde{Z}_2}$	106.7	131.0
$m_{\tilde{Z}_1}$	61.8	66.6
m_A	347.0	157.0
m_h	112.8	116.6
$\Omega_{\tilde{Z}_1} h^2$	0.11	0.10
$BF(b \rightarrow s\gamma)$	2.4×10^{-4}	3.1×10^{-4}
Δa_μ	10.0×10^{-10}	5.4×10^{-10}
$BF(B_s \rightarrow \mu^+\mu^-)$	9.3×10^{-9}	3.7×10^{-8}
$\sigma_{sc}(\tilde{Z}_1 p)$ [pb]	3.1×10^{-7}	2.6×10^{-8}
$\langle\sigma v\rangle _{v\to 0}$ (cm ³ /sec)	2.3×10^{-26}	1.6×10^{-26}



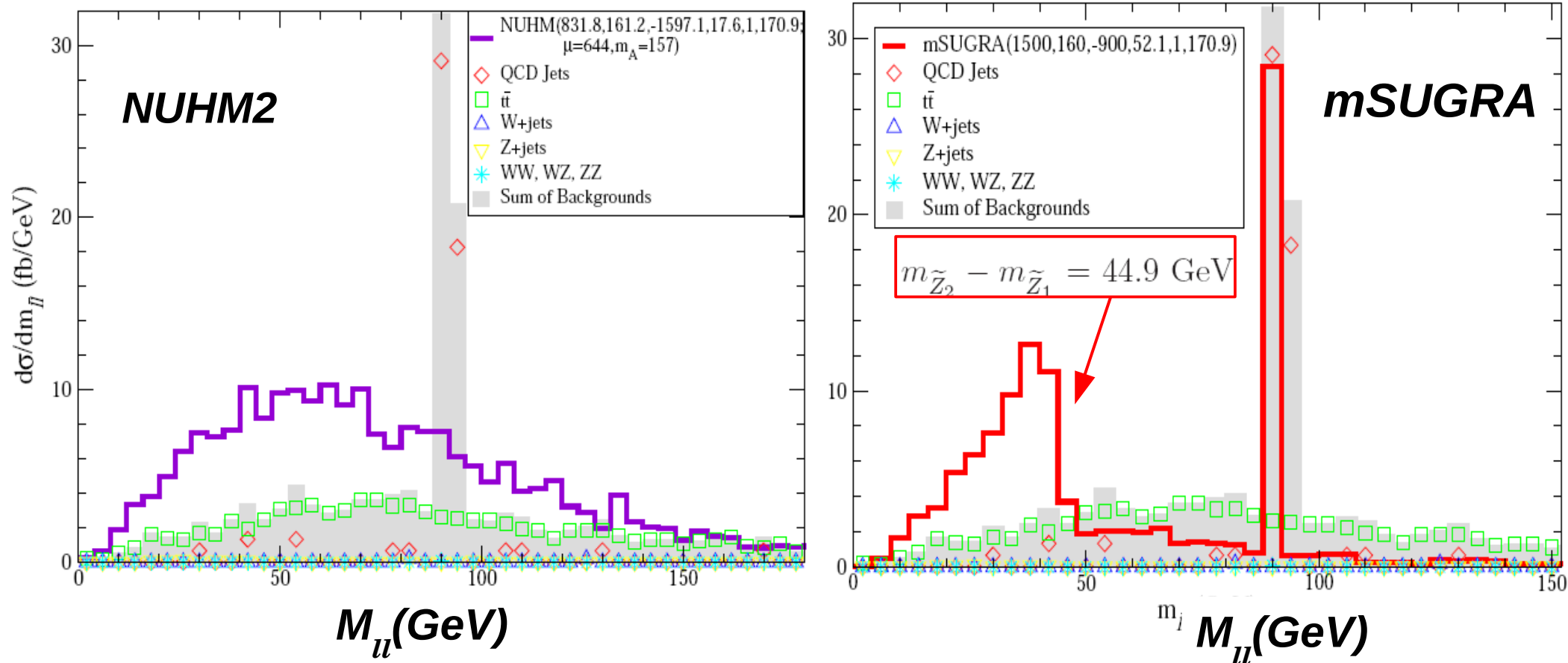
mSUGRA and NUHM2 scenarios for Egret data

$0.09 > \Omega h^2 < 0.13, Br(B_s \rightarrow \mu^+ \mu^-) < 10^{-7}$



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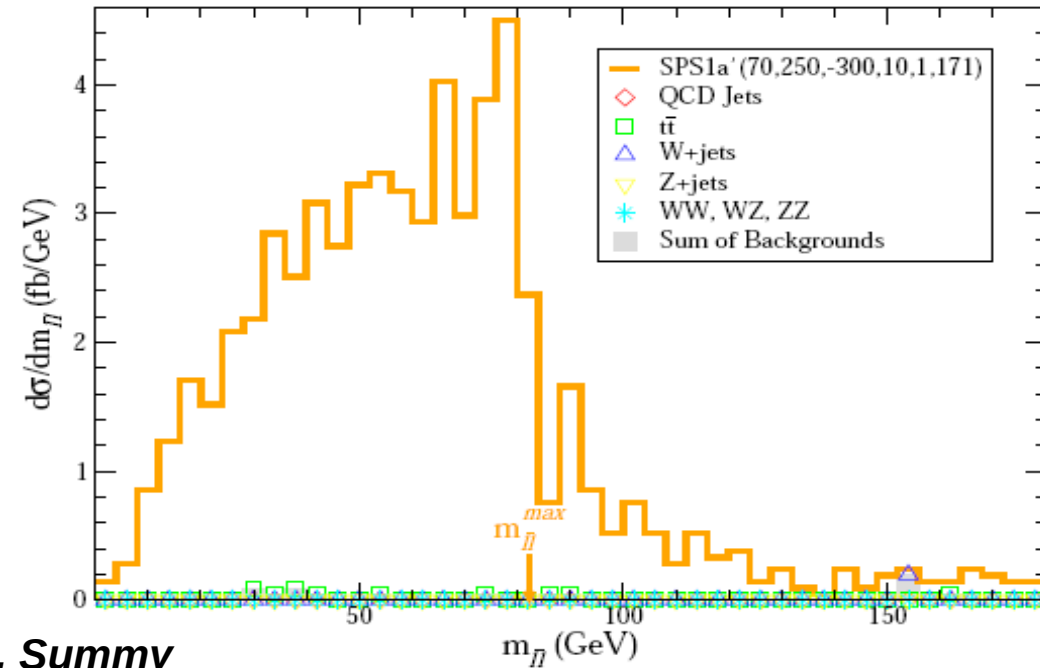
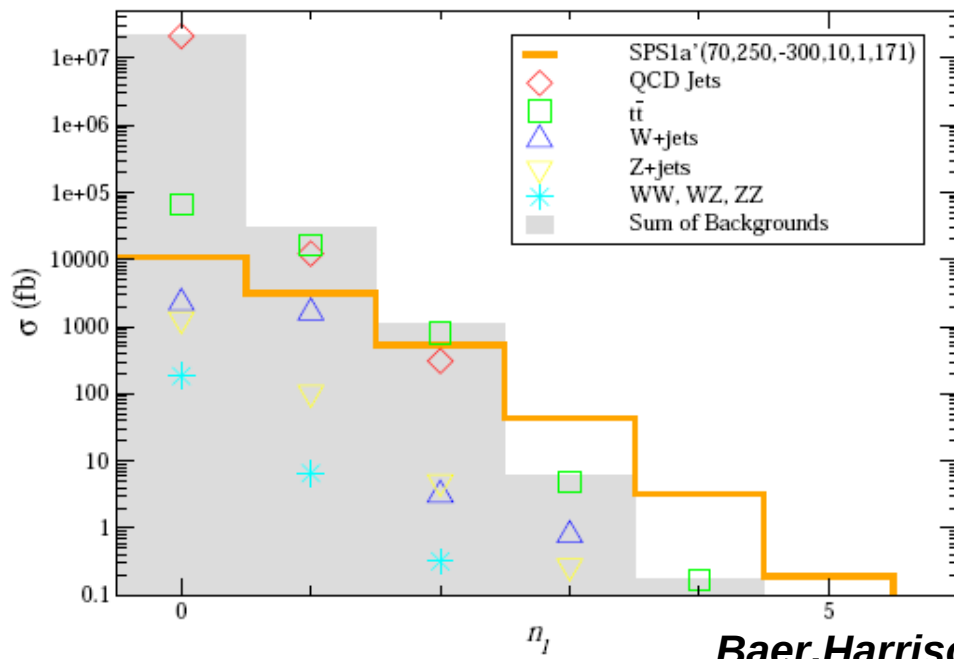
Collider signatures: distinguishing NUHM2 and mSUGRA within light neutralino (50-70 GeV) scenario



In the case of the NUHM2 model the \tilde{t}_1 is light and that $\tilde{g} \rightarrow t\tilde{t}_1$ dominant while \tilde{Z}_2 production via cascade decays is suppressed.

The $Br(\tilde{Z}_2 \rightarrow \tilde{Z}_1 e^+ e^-)$ is suppressed to 0.8% level due to the presence of light A and H Higgs bosons enhancing $Br(\tilde{Z}_2 \rightarrow \tilde{Z}_1 b\bar{b})$ to the 45% level, at the expense of first/second generation decay modes.

Early SUSY discovery without missing E_T

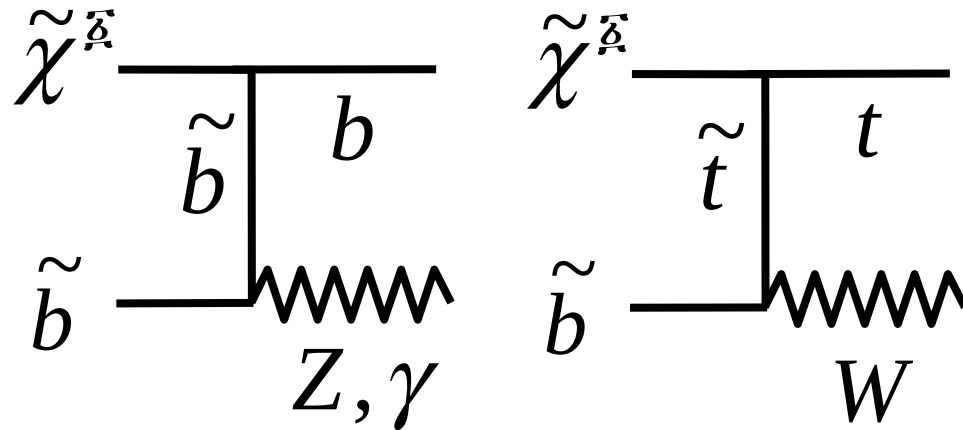


Baer, Harrison, Summy

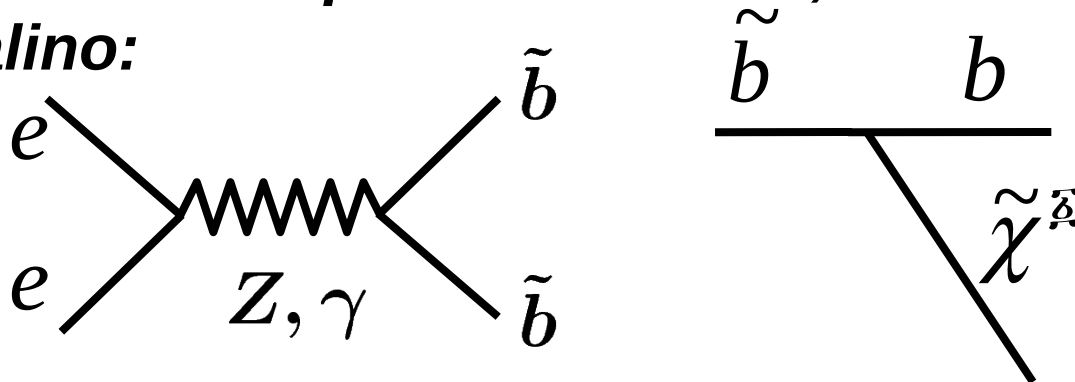
$$\begin{aligned}
 n(\text{jets}) &\geq 4, \\
 E_T(j_1, j_2, j_3, j_4) &\geq 100, 50, 50, 50 \text{ GeV} \\
 S_T &\geq 0.2.
 \end{aligned}
 \quad \text{plus } \geq 3\ell.$$

Sbottom-neutralino co-annihilation as a possible problematic scenario for LHC

- If sbottom and neutralino have a small mass split they can account for co-annihilation in early Universe through this type of diagrams:

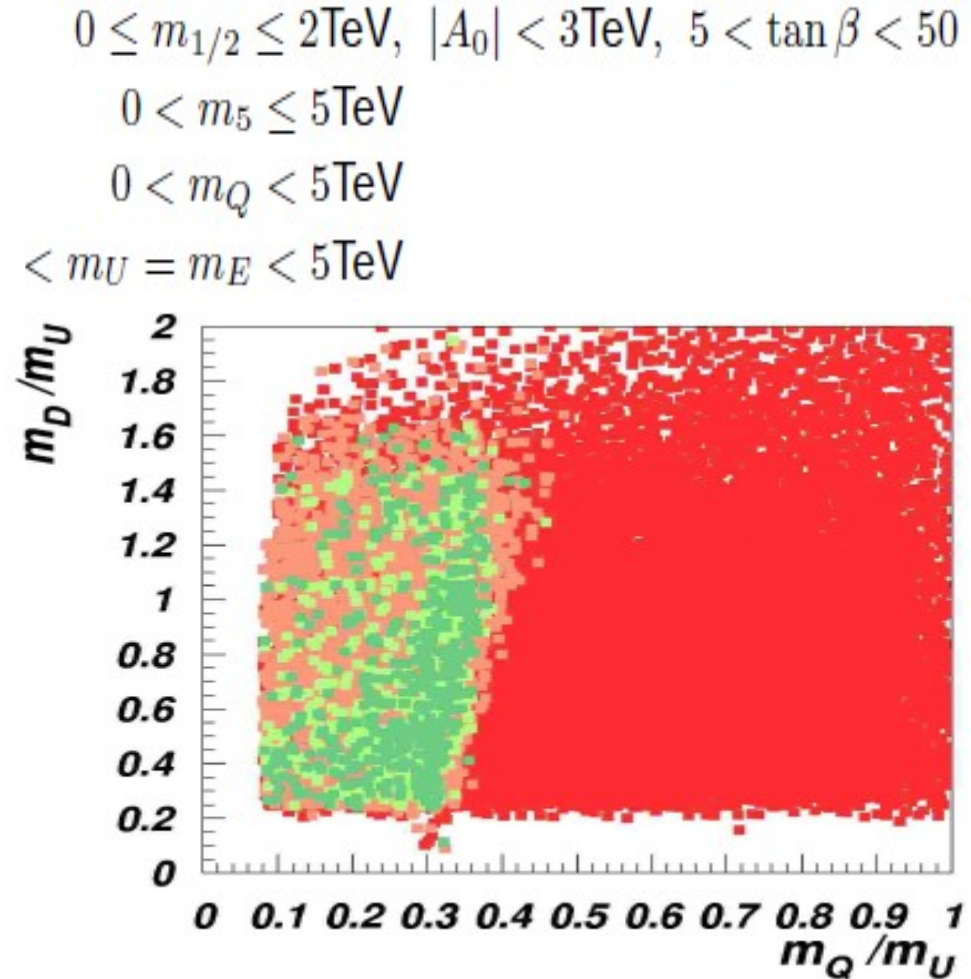
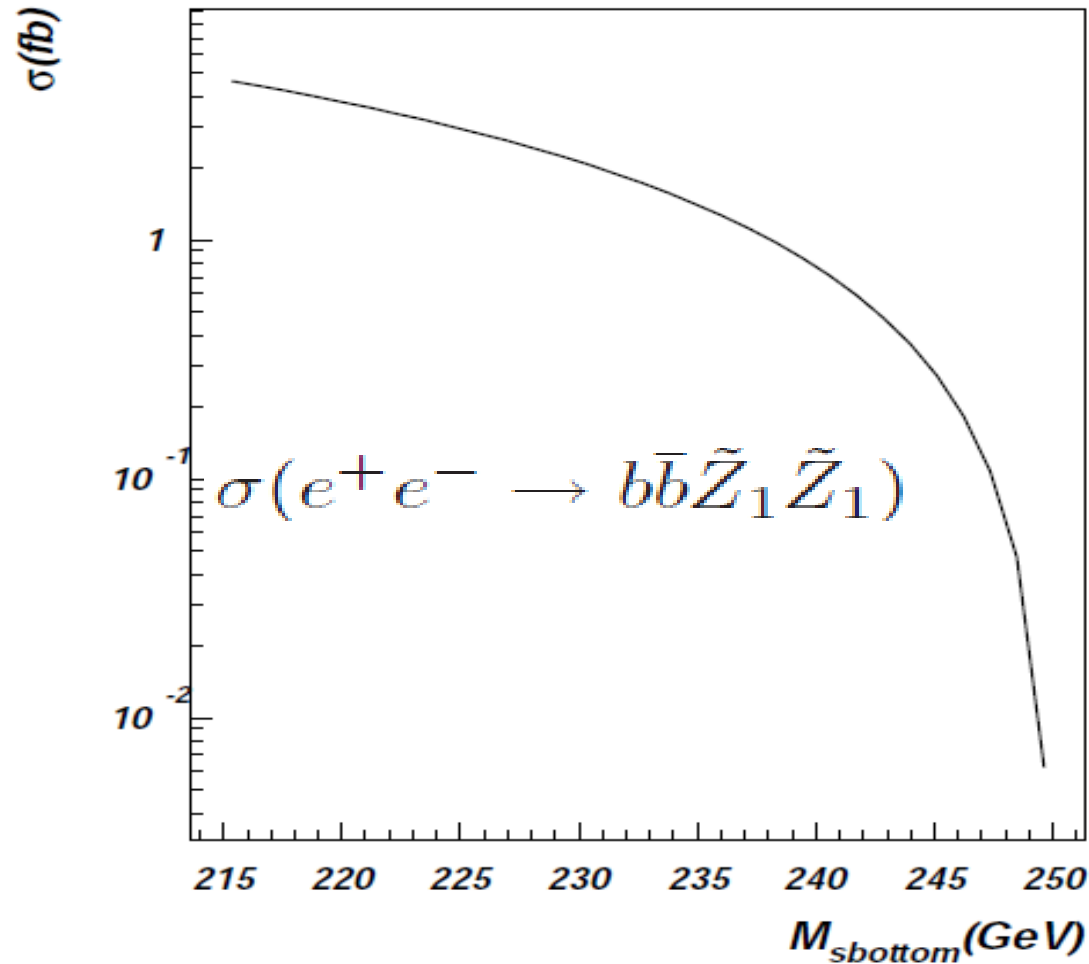


- Sbottom can be produced at ILC, then it decays to b and neutralino:

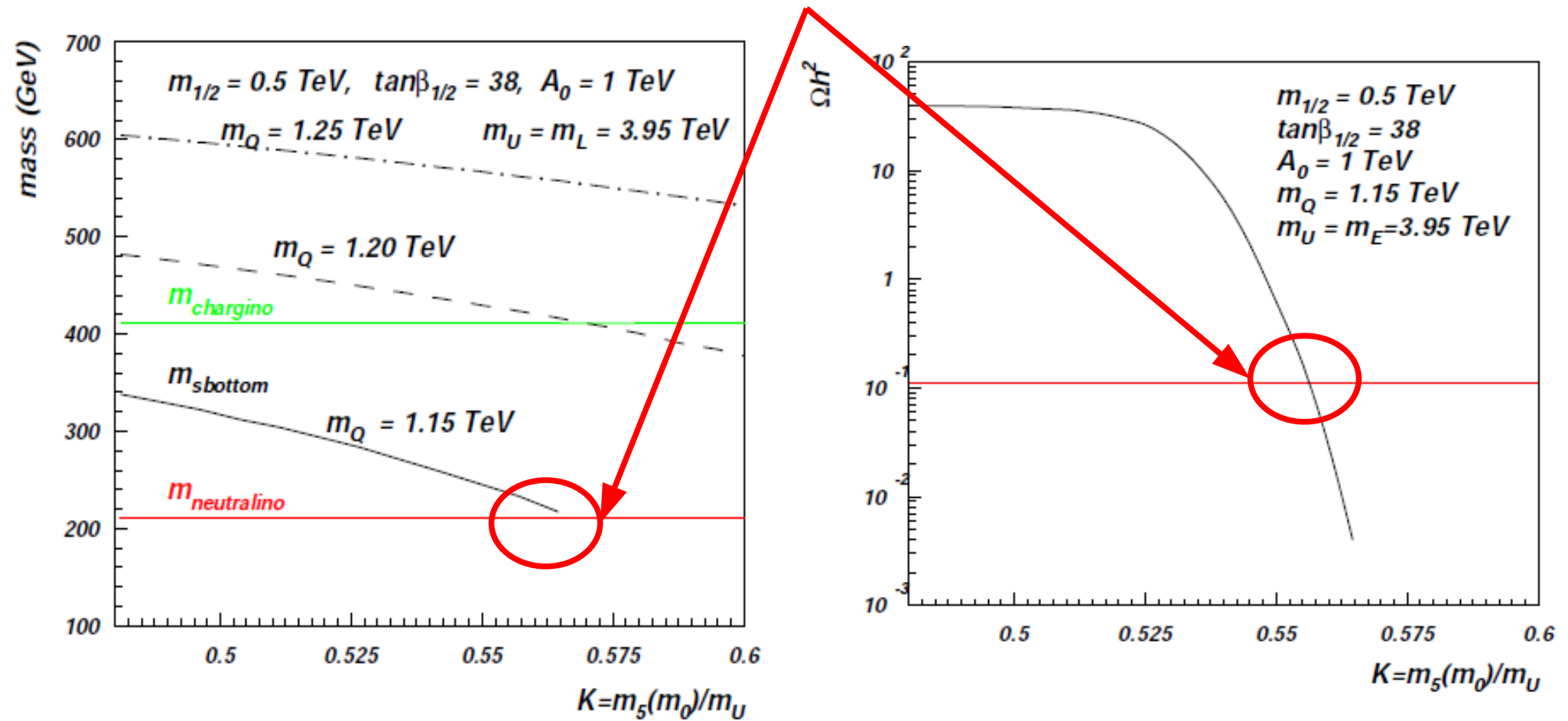


the small mass split leads to **very soft b-jets and missing p_T**

Sbottom-neutralino co-annihilation scenario: CS and parameter space

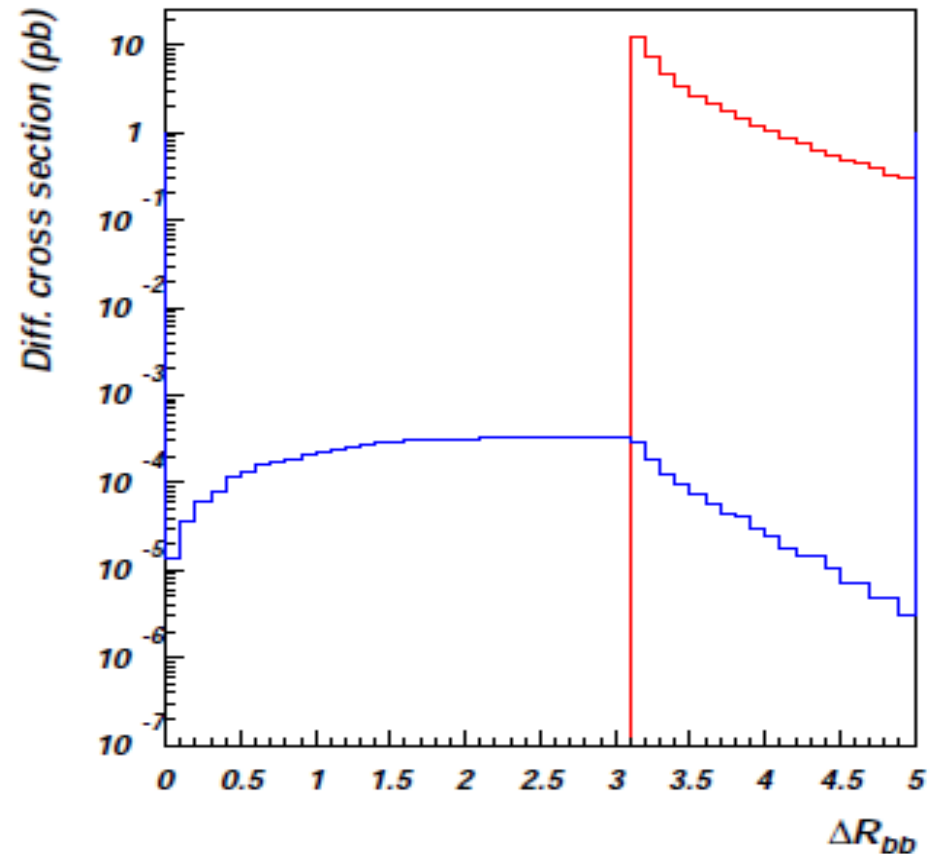
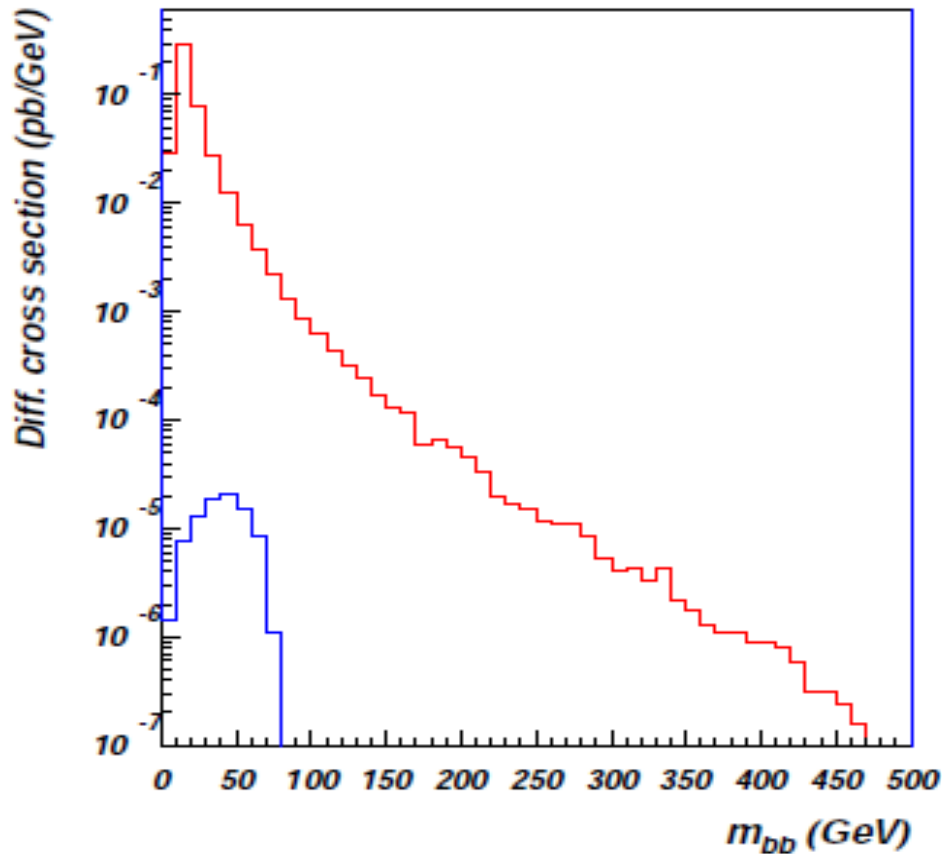


Sbottom-neutralino co-annihilation scenario: sbottom-neutralino mass $\sim 10\%$ degeneracy defines the “right” CDM relic density



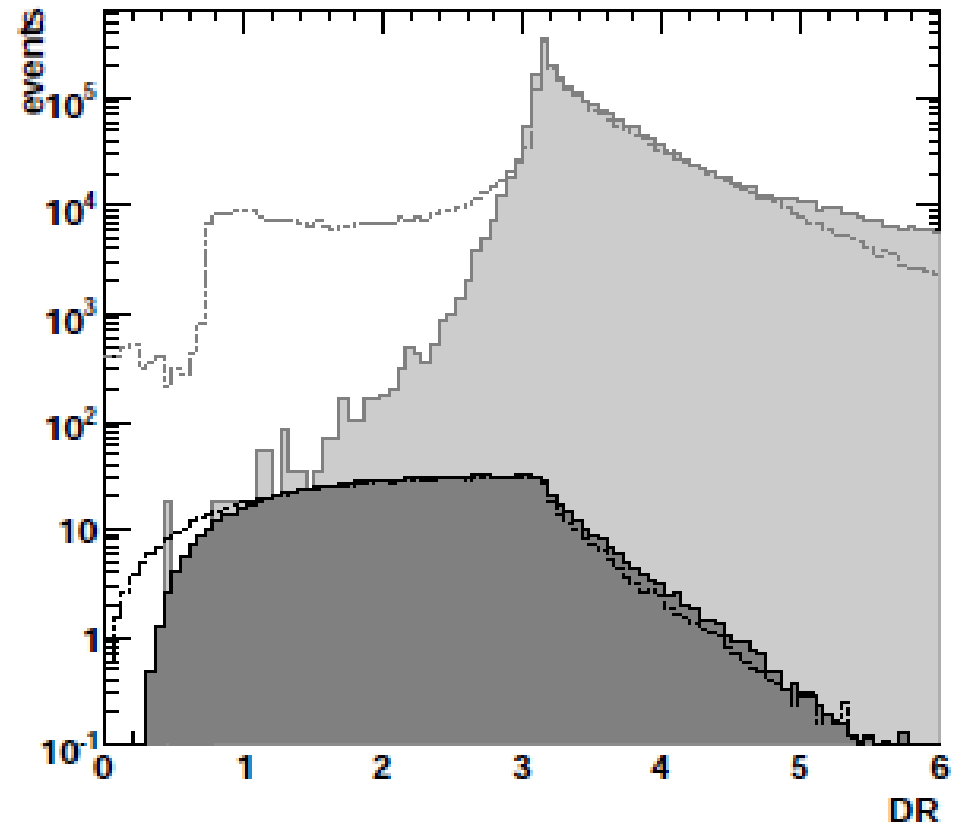
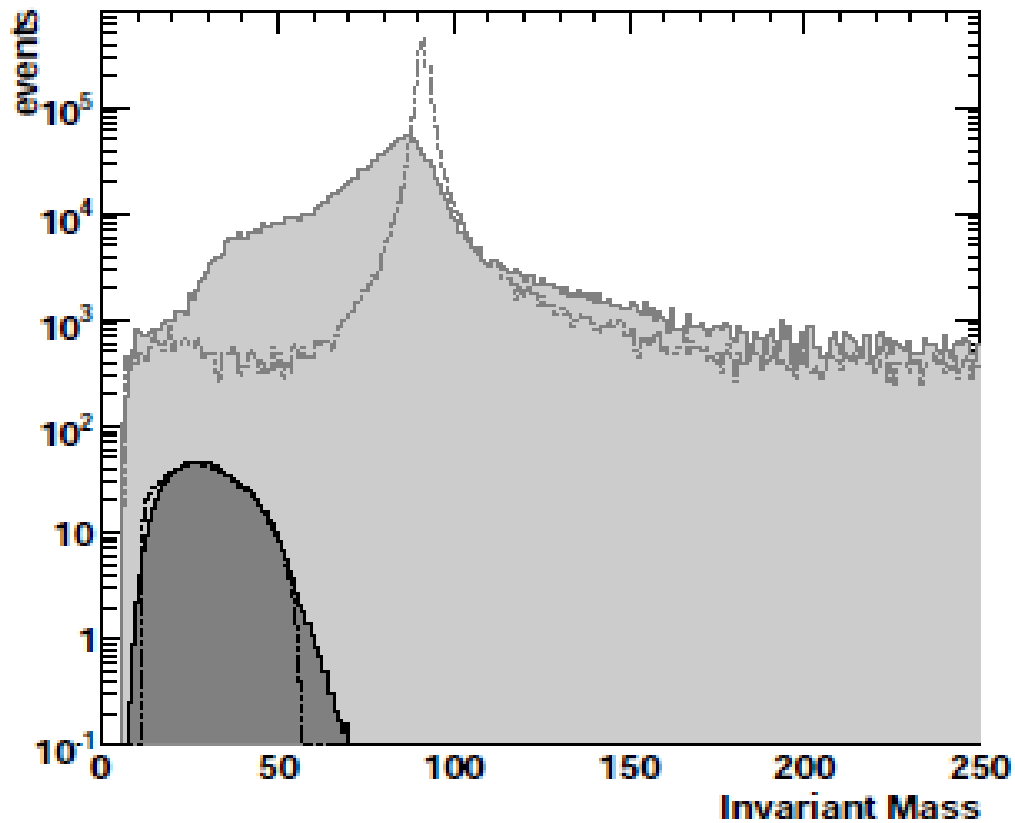
Sbottom-neutralino co-annihilation scenario: Signal versus background (parton level)

$$m_{\tilde{Z}_1} = 210\text{GeV}, m_{\tilde{b}_1} = 240\text{GeV}$$

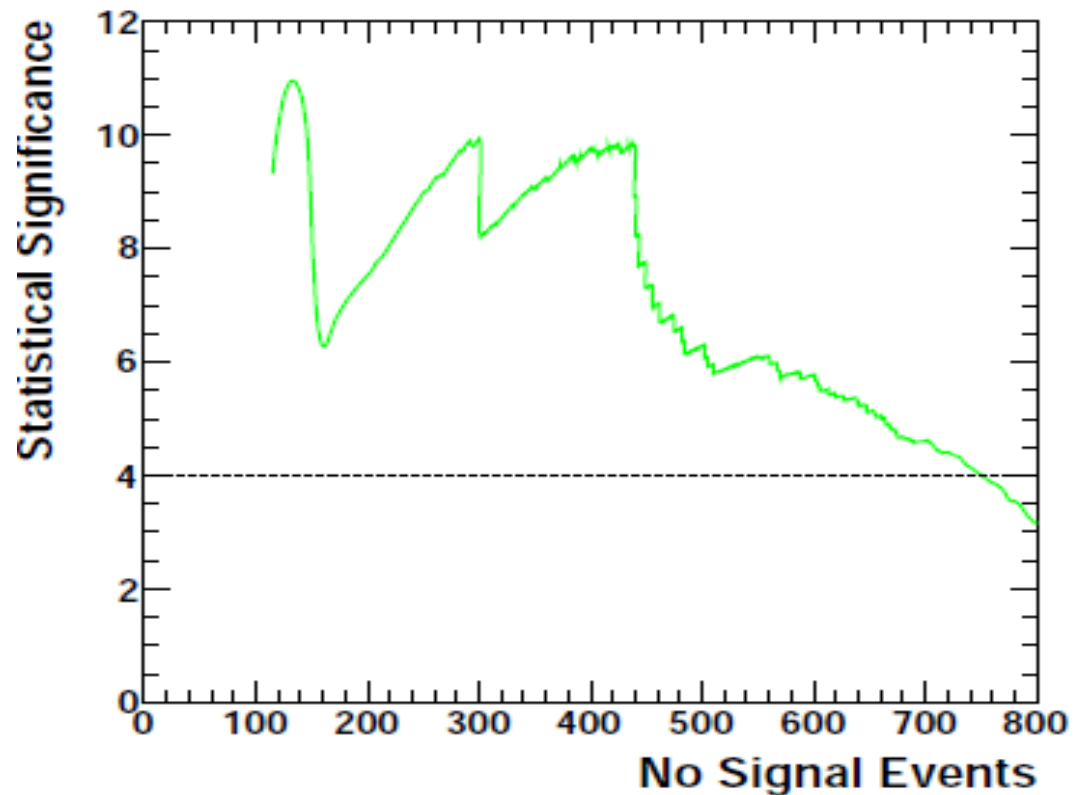
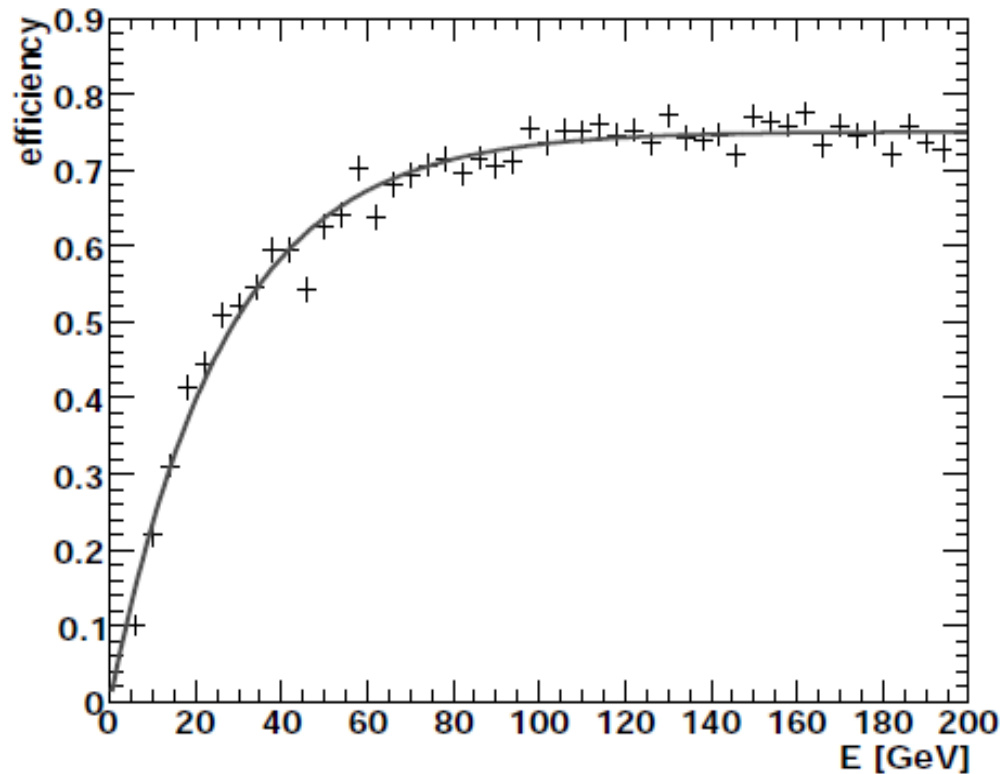


0.77 fb ($m_{\tilde{b}} = 240$ GeV) versus 4.6×10^3 fb rate for dominant $\gamma\gamma \rightarrow b\bar{b}$

Sbottom-neutralino co-annihilation scenario: Signal versus background (detector level)



Sbottom-neutralino co-annihilation scenario: Signal significance from Neural Net



$$m_{\tilde{b}} = 230 \text{ GeV}, \quad m_{\tilde{\chi}_1^0} = 210 \text{ GeV}$$

Conclusions

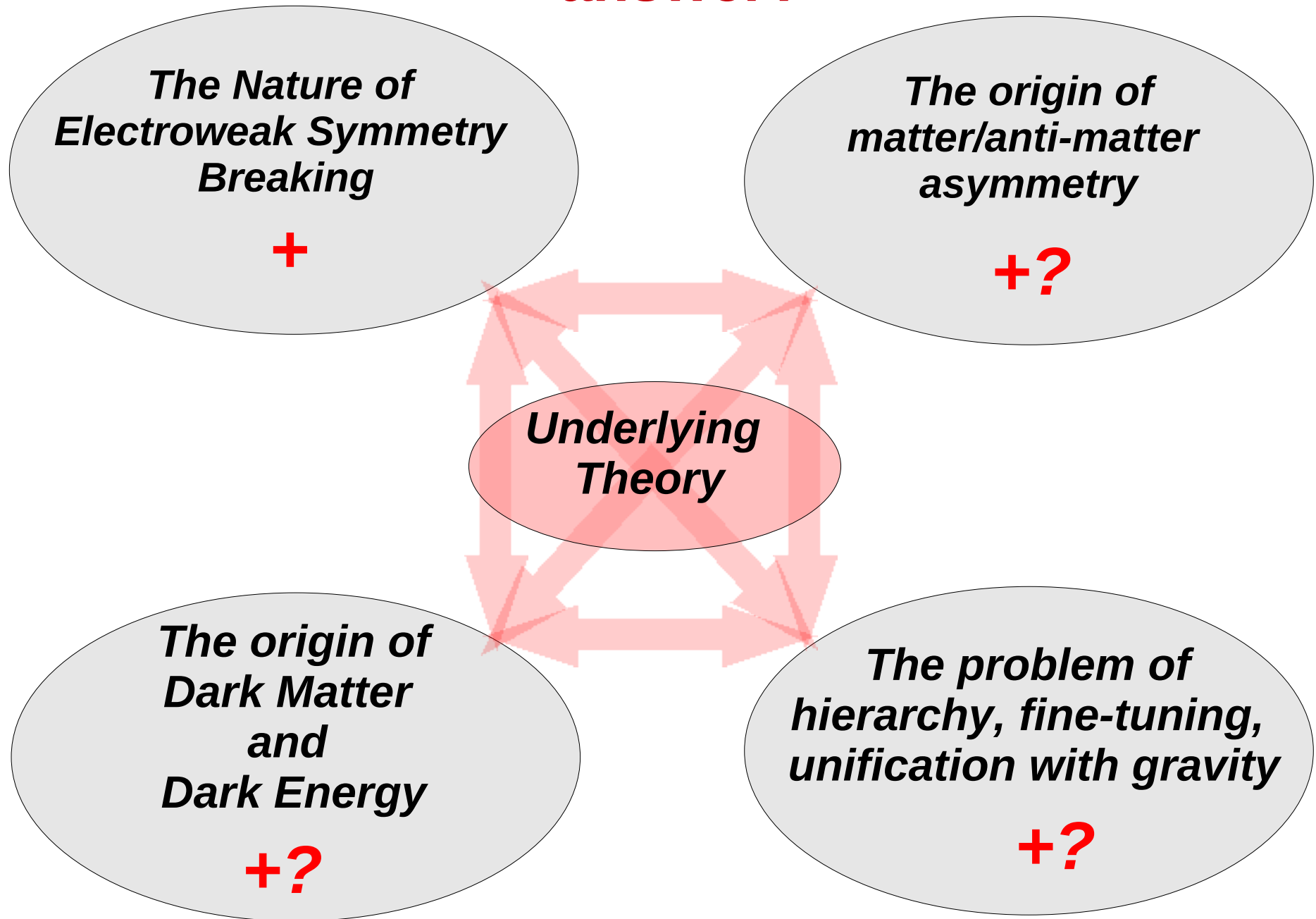
- *SUSY is very compelling theory*
- *The role of CDM and other constraints is crucial*
- *LHC: covers funnel region and stau-coannihilation region, but only low part of FP/HB is covered*
- *ILC: greatly extends LHC reach in FP/HB*
- *ILC can deal with very problematic for LHC scenarios*
- *direct/indirect DM search experiments are highly complementary to LHC/ILC*
- *combined constraints: mSUGRA is practically excluded!*
- *one step beyond the universality opens parameter space and new signatures: NMH, NUMH, non-universal gauginos motivated by SUSY GUTS*

Present constraints/data, especially CDM, give a good idea how SUSY should look like at the LHC and DM search experiments.

ILC will precisely identify SUSY parameter space.

Road is open to hunt down EW scale SUSY which could be just near the corner!

What do we expect from the LHC/ILC to answer?



PhD positions are opened at Southampton

- *Physics beyond the SM: SUSY and alternatives*
- *Delineating Underlying scenarios from LHC signatures*
- *Cosmological connections*

