



## L. KAPTARI

(BLTh, Dubna)

**SIDIS off polarized  $^3\text{He}$ : tagging the transversal nucleon structure, the EMC effect and the hadronization mechanism**

with

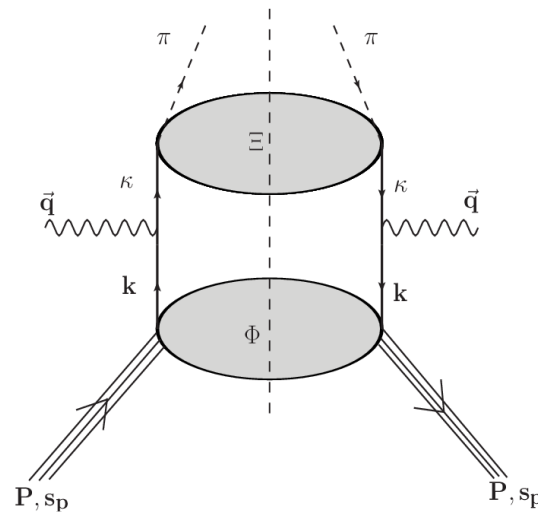
**Sergio Scopetta** – Università di Perugia and INFN, Sezione di Perugia, Italy

**Alessio Del Dotto** – Università di Roma Tre and INFN, Roma 3, Italy

**Giovanni Salmè** – INFN, Roma 1, Italy

# 1. Introduction: "Standard" SIDIS

$$\vec{l} + \vec{p} = l' + h + X$$



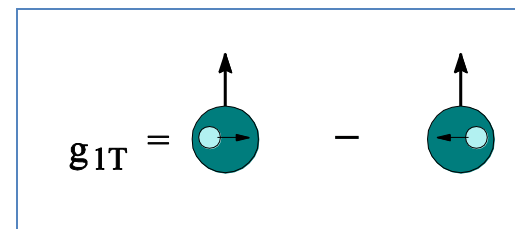
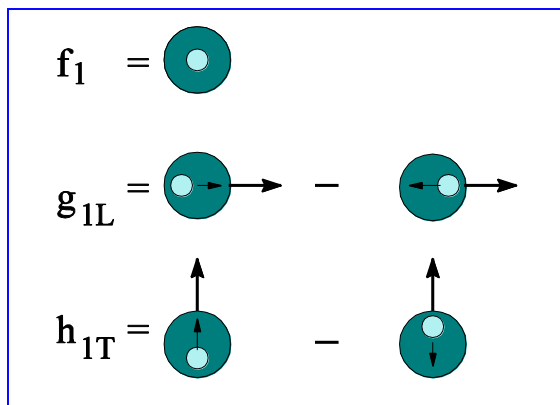
$$W^{\mu\nu(S)} = \frac{1}{2} \sum_a e_a^2 \int \frac{dk^- d^2\mathbf{k}_T}{(2\pi)^4} \int \frac{d\kappa^+ d^2\boldsymbol{\kappa}_T}{(2\pi)^4} \times \delta^2(\mathbf{k}_T + \mathbf{q}_T - \boldsymbol{\kappa}_T) \text{Tr} [\Phi \gamma^{\{\mu} \Xi \gamma^{\nu\}}]_{k^+=xP^+, \kappa^-=P_h^-/z}$$

$$\begin{aligned} \text{Tr} [\Phi \gamma^{\{\mu} \Xi \gamma^{\nu\}}] &= \frac{1}{2} \left\{ \text{Tr} [\Phi] \text{Tr} [\Xi] + \text{Tr} [\mathbf{i} \Phi \gamma_5] \text{Tr} [\mathbf{i} \Xi \gamma_5] \right. \\ &\quad - \text{Tr} [\Phi \gamma^\alpha] \text{Tr} [\Xi \gamma_\alpha] - \text{Tr} [\Phi \gamma^\alpha \gamma_5] \text{Tr} [\Xi \gamma_\alpha \gamma_5] \\ &\quad \left. + \frac{1}{2} \text{Tr} [\mathbf{i} \Phi \sigma^{\alpha\beta} \gamma_5] \text{Tr} [\mathbf{i} \Xi \sigma_{\alpha\beta} \gamma_5] \right\} g^{\mu\nu} \\ &\quad + \frac{1}{2} \text{Tr} [\Phi \gamma^{\{\mu} \Xi \gamma^{\nu\}}] + \frac{1}{2} \text{Tr} [\Phi \gamma^{\{\mu} \gamma_5 \Xi \gamma^{\nu\}} \gamma_5] \\ &\quad + \frac{1}{2} \text{Tr} [\mathbf{i} \Phi \sigma^{\alpha\{\mu} \gamma_5 \Xi \sigma_\alpha^{\nu\}} \gamma_5]. \end{aligned}$$

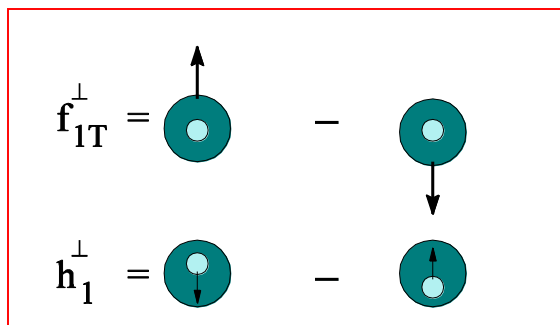
# Leading-Twist Quark Distributions

(A total of eight distributions)

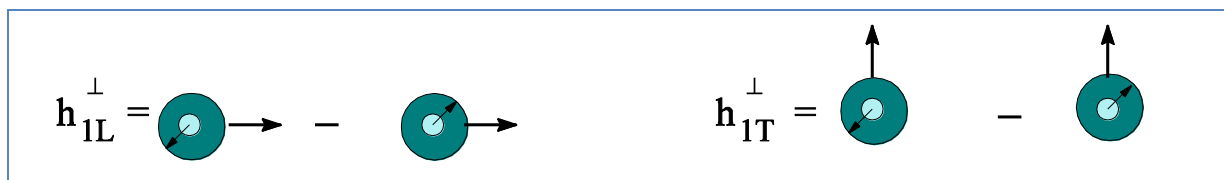
No  $K_{\perp}$   
dependence



$K_{\perp}$  - dependent, T-odd



$K_{\perp}$  - dependent, T-even



# Eight Quark Distributions Probed in SIDIS

$$d^6\sigma = \frac{4\pi\alpha^2 sx}{Q^4} \times$$

$$f_1 = \text{[Diagram: Circle with dot]} \quad \text{Unpolarized}$$

$$\{ [1 + (1-y)^2] \sum_{q,\bar{q}} e_q^2 f_1^q(x) D_1^q(z, P_{h\perp}^2) + (1-y) \frac{P_{h\perp}^2}{4z^2 M_N M_h} \cos(2\phi_h^l) \sum_{q,\bar{q}} e_q^2 h_1^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2) \}$$

$$h_1^\perp = \text{[Diagram: Circle with dot and vertical arrow]} - \text{[Diagram: Circle with dot and vertical arrow]} \quad \text{Unpolarized}$$

$$h_{1L}^\perp = \text{[Diagram: Circle with dot and horizontal arrow]} - \text{[Diagram: Circle with dot and horizontal arrow]} \quad \text{Unpolarized}$$

$$- |S_L| (1-y) \frac{P_{h\perp}^2}{4z^2 M_N M_h} \sin(2\phi_h^l) \sum_{q,\bar{q}} e_q^2 h_{1L}^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$h_{1T}^\perp = \text{[Diagram: Circle with dot and vertical arrow]} - \text{[Diagram: Circle with dot and vertical arrow]} \quad \text{Polarized target}$$

$$+ |S_T| (1-y) \frac{P_{h\perp}}{zM_h} \sin(\phi_h^l + \phi_S^l) \sum_{q,\bar{q}} e_q^2 h_1^{\perp q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$f_{1T}^\perp = \text{[Diagram: Circle with dot and vertical arrow]} - \text{[Diagram: Circle with dot and vertical arrow]} \quad \text{Polarized target}$$

$$+ |S_T| (1-y + \frac{1}{2}y^2) \frac{P_{h\perp}}{zM_N} \sin(\phi_h^l - \phi_S^l) \sum_{q,\bar{q}} e_q^2 f_{1T}^{\perp(1)q}(x) D_1^q(z, P_{h\perp}^2)$$

$$h_{1T}^\perp = \text{[Diagram: Circle with dot and vertical arrow]} - \text{[Diagram: Circle with dot and vertical arrow]} \quad \text{Polarized target}$$

$$+ |S_T| (1-y) \frac{P_{h\perp}^3}{6z^3 M_N^2 M_h} \sin(3\phi_h^l - \phi_S^l) \sum_{q,\bar{q}} e_q^2 h_{1T}^{\perp(2)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$g_{1L} = \text{[Diagram: Circle with dot and horizontal arrow]} - \text{[Diagram: Circle with dot and horizontal arrow]} \quad \text{Polarized beam and target}$$

$$+ \lambda_e |S_L| y (1 - \frac{1}{2}y) \sum_{q,\bar{q}} e_q^2 g_1^q(x) D_1^q(z, P_{h\perp}^2)$$

$$g_{1T} = \text{[Diagram: Circle with dot and vertical arrow]} - \text{[Diagram: Circle with dot and vertical arrow]} \quad \text{Polarized beam and target}$$

$$+ \lambda_e |S_T| y (1 - \frac{1}{2}y) \frac{P_{h\perp}}{zM_N} \cos(\phi_h^l - \phi_S^l) \sum_{q,\bar{q}} e_q^2 g_{1T}^{(1)q}(x) D_1^q(z, P_{h\perp}^2) \}$$

$S_L$  and  $S_T$ : Target Polarizations;  $\lambda_e$ : Beam Polarization

## Single Spin Asymetry

$$A_{UT}(\phi_h, \phi_S) \equiv \frac{d\sigma(\phi_h, \phi_S) - d\sigma(\phi_h, \phi_S + \pi)}{d\sigma(\phi_h, \phi_S) + d\sigma(\phi_h, \phi_S + \pi)} \longrightarrow A_{UT}^{Coll.(Siv.)} = \frac{\int d\phi_S d\phi_h \sin(\phi_h \pm \phi_S) d\sigma_{UT}}{\int d\phi_S d\phi_h d\sigma_{UU}} ;$$

$$A_{UT}^{Collins} \sim |\mathbf{S}_T| \times \frac{\sum_q e_q^2 \int d^2\kappa_T d^2\mathbf{k}_T \delta^2(\mathbf{k}_T + \mathbf{q}_T - \kappa_T) \frac{\hat{\mathbf{h}} \cdot \kappa_T}{M_h} h_1^q(x, \mathbf{k}_T^2) H_1^{\perp q, h}(z, (z\kappa_T)^2)}{\sum_q e_q^2 \int d^2\kappa_T d^2\mathbf{k}_T \delta^2(\mathbf{k}_T + \mathbf{q}_T - \kappa_T) f_1^q(x, \mathbf{k}_T^2) D_1^{q, h}(z, (z\kappa_T)^2)}$$

$$A_{UT}^{Sivers} = |\mathbf{S}_T| \frac{\sum_q e_q^2 \int d^2\kappa_T d^2\mathbf{k}_T \delta^2(\mathbf{k}_T + \mathbf{q}_T - \kappa_T) \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} f_{1T}^{\perp q}(x, \mathbf{k}_T^2) D_1^{q, h}(z, (z\kappa_T)^2)}{\sum_q e_q^2 \int d^2\kappa_T d^2\mathbf{k}_T \delta^2(\mathbf{k}_T + \mathbf{q}_T - \kappa_T) f_1^q(x, \mathbf{k}_T^2) D_1^{q, h}(z, (z\kappa_T)^2)}$$

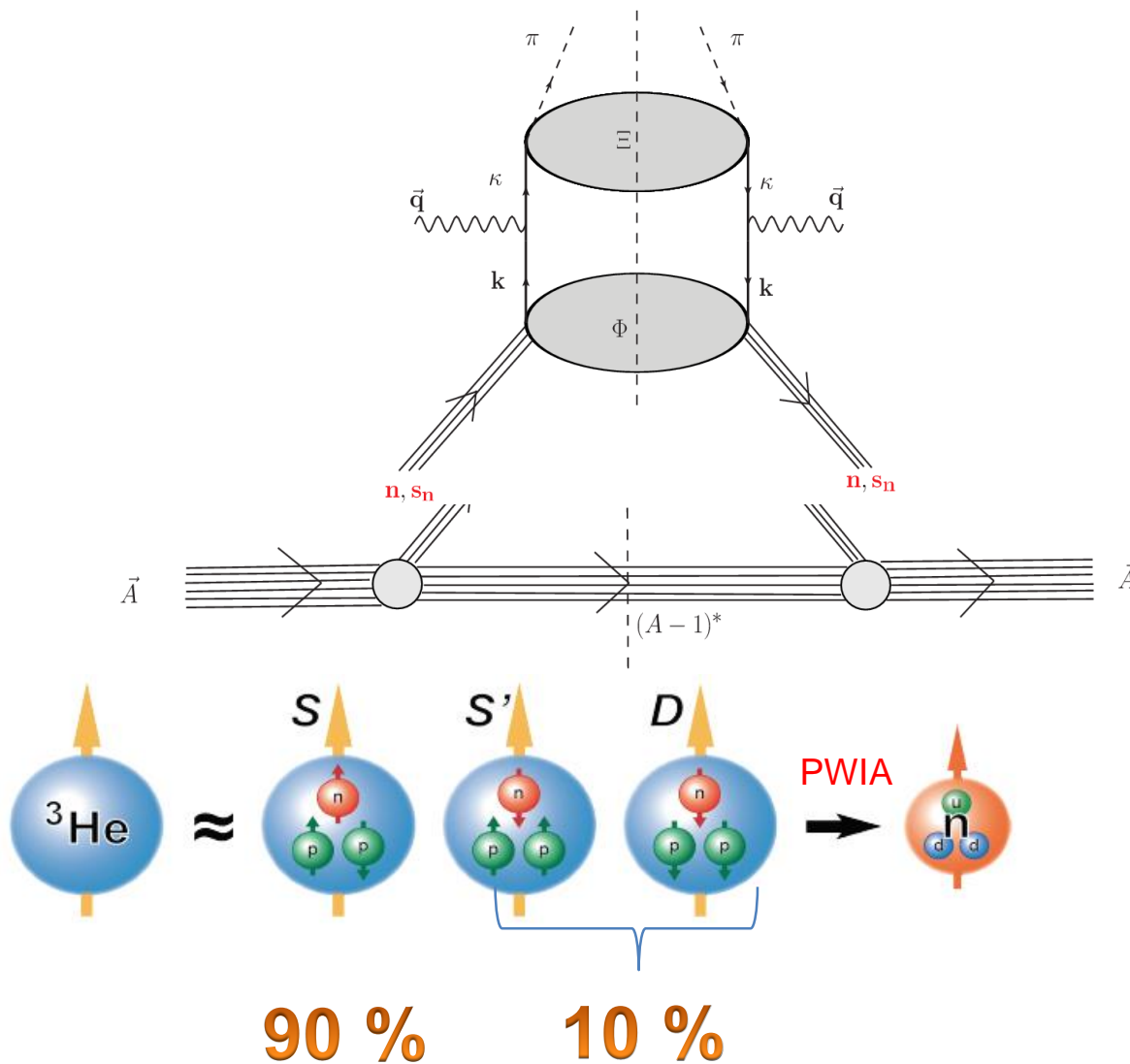
$H_1^{\perp q, h}(z, (z\kappa_T)^2)$ , the (a T-odd) Collins fragmentation function  $\equiv$  number density of scalar hadrons originating from the fragmentation of a transversely polarized quark

$f_{1T}^{\perp q}(x, \mathbf{k}_T^2)$  the Sivers distribution function (T-odd)  $\equiv$  number density of unpolarized quarks in a transversely polarized target

HERMES, COMPASS, JLAB

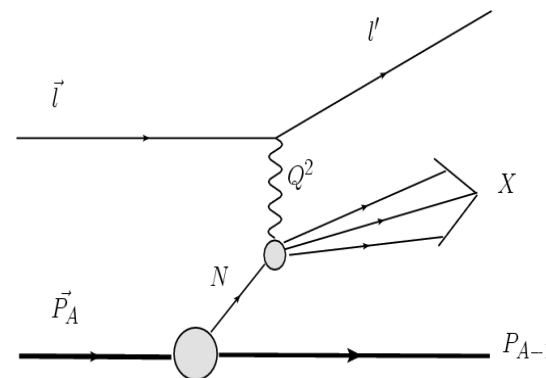
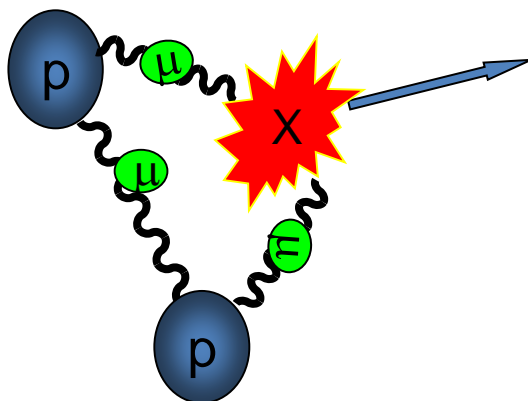
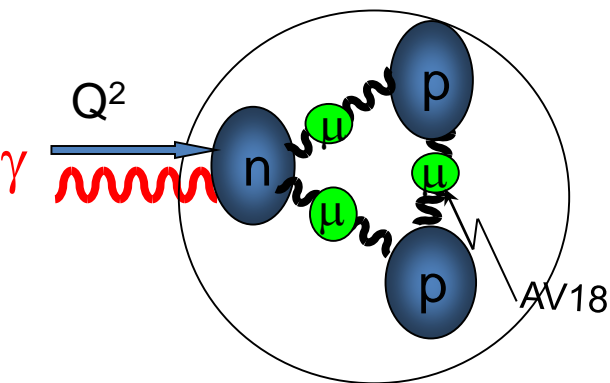
$$\vec{l} + \vec{p} = l' + h + X$$

Polarized neutron?



Single Target-Spin Asymmetry in Semi-Inclusive  $\pi$  Electroproduction on a Transversely Polarized  $^3\text{He}$  Target (JLAB, E03-004(010,011), EPJ Plus, 126 (2011) 2)

## What's PWIA?



## Exact factorization & the nuclear spectral function

CdA & LPK Phys.Rev. C66 (2002) 044004

$$d\sigma(eA) = K d\sigma(eN) P(k_1, E_{rem})$$

$$P(\mathbf{k}, E_{rem}) = \sum_{\mathbf{f}} |\langle (\mathbf{A} - 1)_{\mathbf{f}} | \mathbf{a}(\mathbf{k}) | \mathbf{A} \rangle|^2 \delta \left( E_{rem} - \sqrt{\mathbf{P}_{A-1}^2} - m_N + M_A \right)$$

many-body problem

$$\mathcal{F}^A(x_{Bj}, Q^2 \dots) = \sum_N \int_{x_{Bj}}^A \mathcal{F}^N(x_{Bj}/\alpha, Q^2 \dots) f_N^A(\alpha, Q^2 \dots) d\alpha;$$

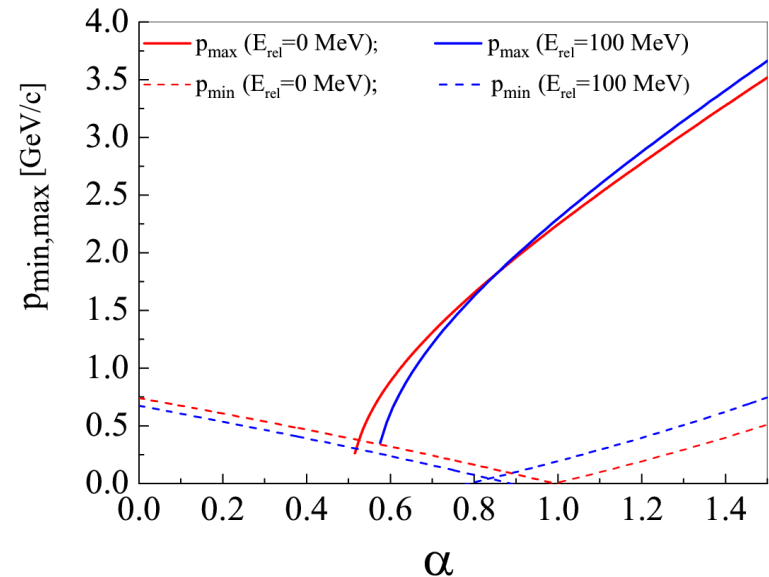
$$f_N^A(\alpha, Q^2 \dots) = \int_{p_{min}(\alpha, Q^2 \dots)}^{p_{max}(\alpha, Q^2 \dots)} dE \int P_N^A(\mathbf{p}, E) \delta\left(\alpha - \frac{pq}{m\nu}\right) \theta\left(W_x^2 - (M_N + M_\pi)^2\right) d^3\mathbf{p}$$

**Bjorken Limit:**  $|\mathbf{q}| \rightarrow \infty, \nu \rightarrow \infty,$

$p_{min;max}$  depend only on  $\alpha$  and, consequently,  $f_N^A(\alpha)$

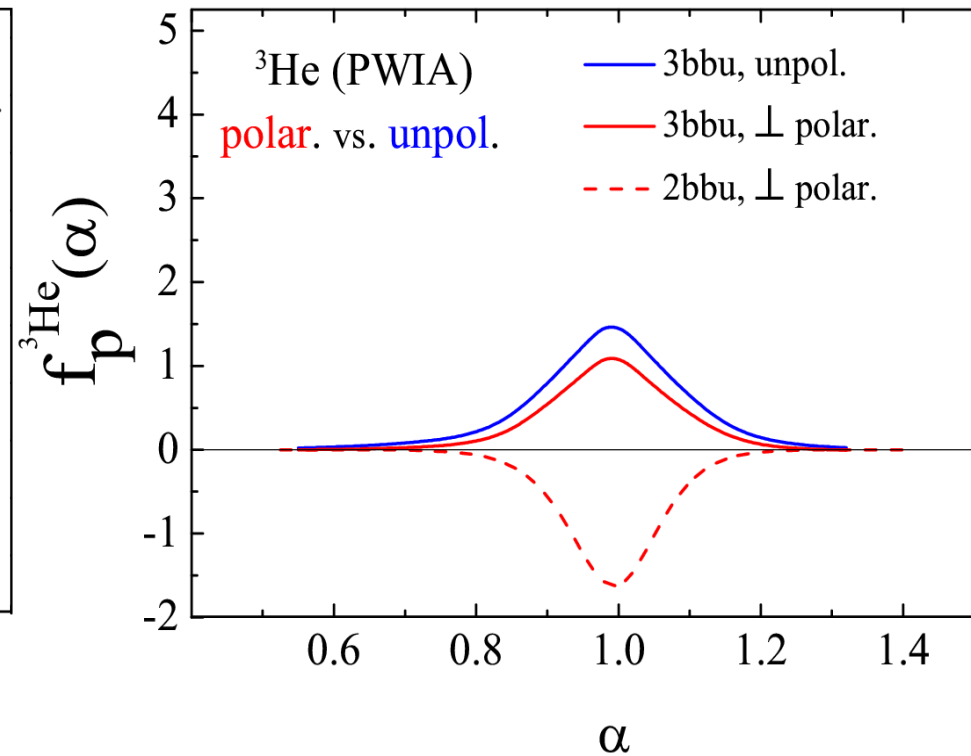
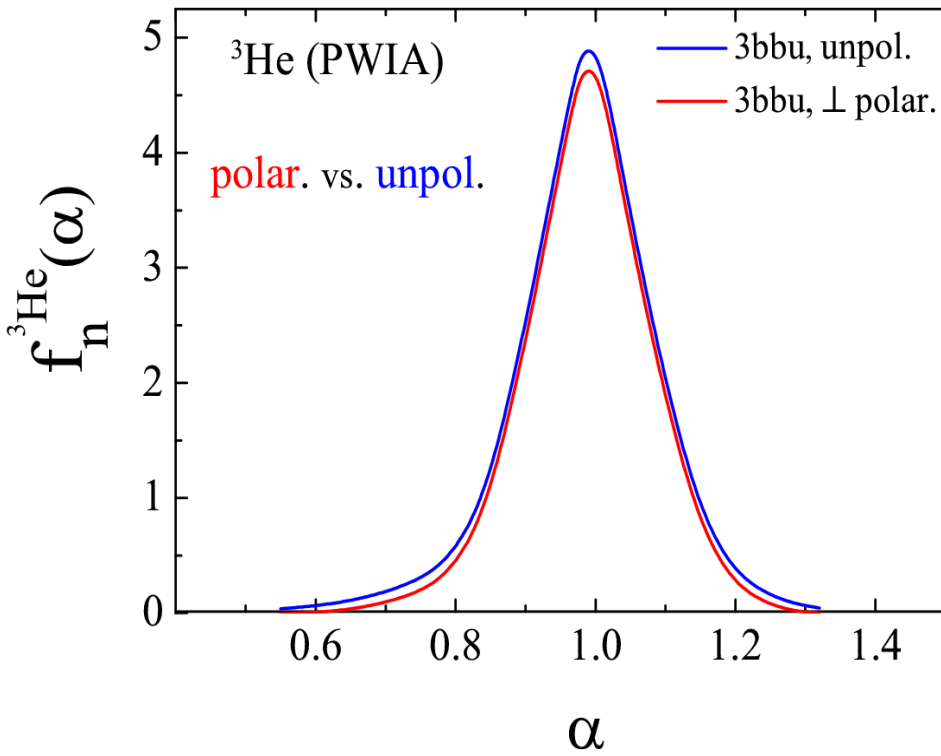
is independent on  $Q^2$  and  $x_{Bj} \equiv \frac{Q^2}{2M_N\nu^2}$  and  $0 \leq \alpha \leq A$

**JLAB kinematics,**  $|\mathbf{q}| = \nu\sqrt{1 + \frac{4M_N^2 x_{Bj}^2}{Q^2}}$   $\alpha_{min} \neq 0$   
 $E_0 = 8.80 \text{ GeV}; E' = 2.44 \text{ GeV}; \theta_{scatt.} = 30^\circ$   $\longrightarrow$



L. P.K., A. Del Dotto, E. Pace, G. Salm`e, S.Scopetta., PRC 89 (2014) 035206





Unfold the convolutoin formula by taking advantage of the fact that  $\alpha \sim 1$ , the distribution function  $f_N^A(\alpha, Q^2) \sim \delta(\alpha - 1)$ . Then the extraction procedure is based on two main conjectures:

i) The calculated cross section within the PWIA describes the experimental data, i.e.

$$d\sigma_3^{exp.} \simeq d\sigma_3^{PWIA}$$

ii) The binding effects in  ${}^3\text{He}$  are small and the intrinsic neutron can be treated as quasi-free. Then the experimentally measures asymmetry  $A_3$  (Collins or/and Sivers) can be written as

$$A_3^{exp} = \frac{\Delta\vec{\sigma}_3^{exp.}}{\sigma_{unpol.}^{exp.}} \simeq \frac{\Delta\vec{\sigma}(ntr) \cdot \int dE d^3\mathbf{p}\vec{P}_n(E, \mathbf{p}) + 2\Delta\vec{\sigma}(prt) \cdot \int dE d^3\mathbf{p}\vec{P}_p(E, \mathbf{p})}{\sigma_{unpol.}(ntr) \int dE d^3\mathbf{p}P_n^{unpol}(E, \mathbf{p}) + 2\sigma_{unpol.}(prt) \int dE d^3\mathbf{p}P_p^{unpol}(E, \mathbf{p})},$$

Introduce the so-called "dilution" functions as

$$A_3^{exp} = \underbrace{\langle p_n \rangle \frac{\Delta\vec{\sigma}(ntr)}{\sigma_{unpol.}(ntr)}}_{A_n} \underbrace{\frac{\sigma_{unpol.}(ntr)}{\langle N_n \rangle \sigma_{unpol.}(ntr) + 2\langle N_p \rangle \sigma_{unpol.}(prt)}}_{d_n} + 2\langle p_p \rangle \underbrace{\frac{\Delta\vec{\sigma}(prt)}{\sigma_{unpol.}(prt)}}_{A_p} \underbrace{\frac{\sigma_{unpol.}(prt)}{\langle N_n \rangle \sigma_{unpol.}(ntr) + 2\langle N_p \rangle \sigma_{unpol.}(prt)}}_{d_p} \equiv \langle p_n \rangle d_n A_n + 2\langle p_p \rangle d_p A_p,$$

$$A_n = \frac{1}{\langle p_n \rangle d_n} \left[ A_3^{exp.} - 2\langle p_p \rangle d_p A_p^{exp.} \right].$$

C. Ciofi degli Atti, S. Scopetta, E.Pace, G. Salme, PR.C 48 (1993) 968.

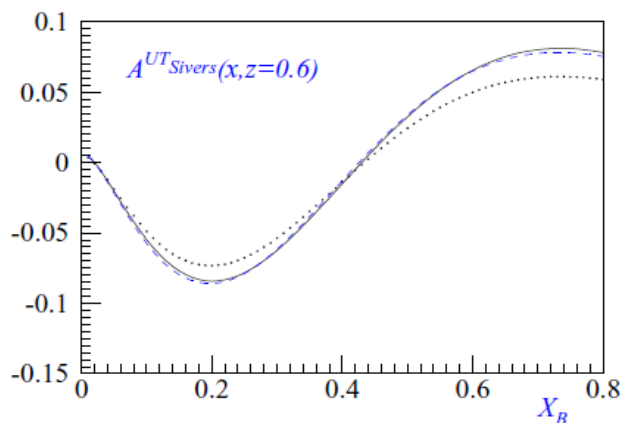
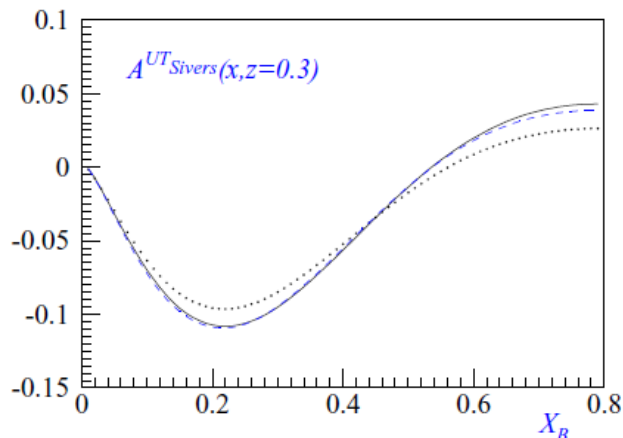
## PWIA and Sivers and Collins Asymetries

A realistic spin-dependent spectral function of  $^3\text{He}$  within the AV18 interaction and w.f. by the Pisa group (A. Kievsky et al., NPA 577, 511 (1994). )

Parameterizations of data for **pdfs** and **fragmentation** functions whenever available ( $f_1^q(x, k_\perp)$  GRV 1998,  $f_{1T}^{\perp q}(x, k_\perp)$  Anselmino et al., 2005,  $D_1^{\text{qh}}(z, z^2 \kappa_T^2)$  Kretzer, 2000)

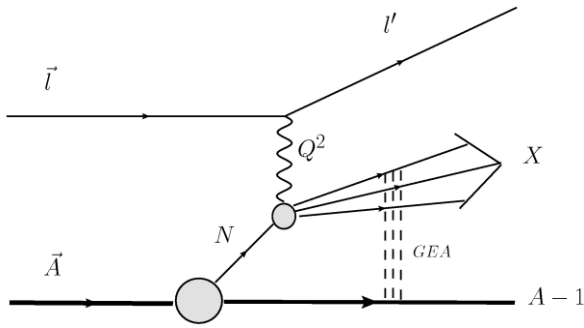
Models for the unknown **pdfs** and fragmentation functions.  
 (  $h_1^q(x, k_\perp)$  GRVW, 2001,  $H_1^{\perp \text{hq}}(z, z^2 \kappa_T^2)$  Amrath et al, 2005)

S. Scopetta, Phys.Rev. D75 (2007) 054005



full – “free” neutron (input)  
 dot - extracted without prt  
 dash – extracted with dilution factors

In **PWIA (!)** nuclear effects in the extarction of the neutron information from polarized  $^3\text{He}$  are found to be under control



PWIA + FSI (Generalized Eikonal Approximation)

$$d\sigma(eA) \sim l^{\mu\nu} \cdot W_{\mu\nu}^A(S_A)$$

1  $W_{\mu\nu}^A \sim \overline{\sum_{\alpha_A} \sum_{\alpha_{A-1}, \alpha_N}} \langle \alpha_A \mathbf{P} | \hat{\mathbf{J}}_{\mu}^A(\mathbf{0}) | \alpha_N \mathbf{p}_1, \alpha_{A-1} \mathbf{P}_{A-1} \mathbf{E}_{A-1}^f \rangle \langle \mathbf{E}_{A-1}^f \mathbf{P}_{A-1} \alpha_{A-1}, \mathbf{p}_1 \alpha_N | \hat{\mathbf{J}}_{\nu}^A(\mathbf{0}) | \alpha_A \mathbf{P}_A \rangle$ ,

2  $\Phi_{3\text{He}}(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3) = \mathcal{A} e^{i\mathbf{P}\mathbf{R}_c} \Psi_3(\boldsymbol{\rho}, \mathbf{r}); \quad \Phi_f^*(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3) = \mathcal{A} \mathbf{G}(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3) e^{-i\mathbf{p}'\mathbf{r}_1} e^{-i\mathbf{P}_{23}\mathbf{R}_{23}} \Psi_{23}^*(\mathbf{r})$

3  $\mathbf{G}(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3) = \prod_{j=2}^3 [1 - \theta(\mathbf{r}_{j\parallel} - \mathbf{r}_{1\parallel}) \Gamma(\mathbf{r}_{j\perp} - \mathbf{r}_{1\perp})]$ ,  $\Gamma(\mathbf{r}_{\perp}) = \Gamma(\mathbf{r}_{\perp}, \sigma_{\text{eff}}^{\text{NX}})$

4  $J_{\mu} = \int d\mathbf{r}_1 d\mathbf{r}_2 d\mathbf{r}_3 \Psi_{23}^{*f}(\mathbf{r}_2, \mathbf{r}_3) e^{-\mathbf{p}_X \mathbf{r}_1} \chi_{\lambda_X}^+ \phi^*(\xi_x) \cdot \mathcal{G}(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3) \hat{j}_{\mu}(\mathbf{r}_1, X) \vec{\Psi}_3^M(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3)$

5  $[\mathcal{G}(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3, \sigma_{\text{eff}}^{\text{NX}}), \hat{j}_{\mu}(\mathbf{r}_1, X)] = 0!!!(?) \longrightarrow$  **FACTORIZATION**

etc

# SIDIS AND FSI-EFFECTS

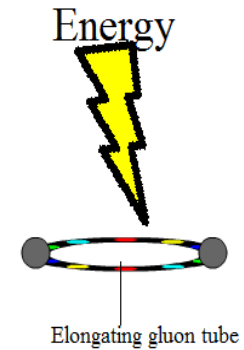
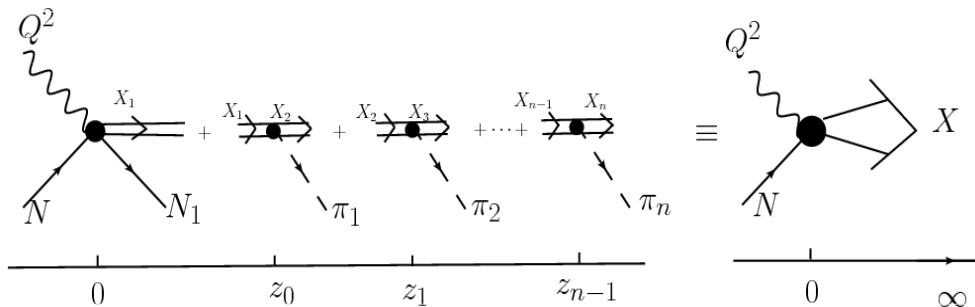
$$\mathcal{O}_{\lambda\lambda'}^{MM'(FSI)}(p_N, E) = \int \langle \mathcal{G}(1, 2, 3, \sigma_{eff}^{NX}) \{ \Psi_{23}^t, \lambda, \mathbf{p}_N \} | \Psi_{3He}^M \rangle \langle \Psi_{3He}^{M'} | \mathcal{G}(1, 2, 3, \sigma_{eff}^{NX}) \{ \Psi_{23}^t, \lambda', \mathbf{p}_N \} \rangle \delta \left( E - \frac{t^2}{M_N} \right) \frac{d^3 t}{(2\pi)^3}$$

$$\mathcal{F}^A(x_{Bj}, Q^2 \dots) = \sum_N \int_{x_{Bj}}^A \mathcal{F}^N(x_{Bj}/\alpha, Q^2 \dots) f_N^A(\alpha, Q^2 \dots) d\alpha;$$

$$f_N^A(\alpha, Q^2 \dots) = \int_{p_{min}}^{p_{max}} dE \int P_N^{FSI}(\mathbf{p}, E, \sigma_{eff}^{NX}) \delta \left( \alpha - \frac{pq}{m\nu} \right) \theta \left( W_x^2 - (M_N + M_\pi)^2 \right) d^3 \mathbf{p}$$

$$\sigma_{eff}^{NX} = ?$$

Color string model + gluon radiation



$$\sigma_{eff}(z) = \sigma_{tot}^{NN} + \sigma_{tot}^{\pi N} [n_M(z) + n_G(z)]$$

C. CdA, L.P.K. et al. PRC 80 (2009) 054610; ibid PRC C81(2010)  
C. CdA, L.P.K., C.B. Mezzetti, Fizica 20, (2012).

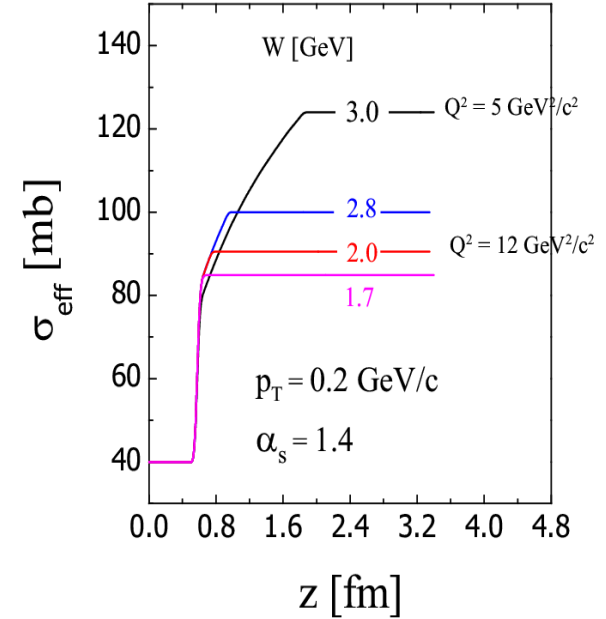
$$\mathbf{n}_M(\mathbf{t}) = \frac{\ln(1 + \mathbf{t}/\Delta\mathbf{t})}{\ln 2}$$

$t < t_0$

$$\mathbf{n}_G(\mathbf{t}) = \frac{16}{27} \left\{ \ln\left(\frac{Q}{\lambda}\right) + \ln\left(\frac{t \Lambda_{QCD}}{2}\right) \ln\left[\frac{\ln(Q/\Lambda_{QCD})}{\ln(\lambda/\Lambda_{QCD})}\right] \right\}$$

$t > t_0$

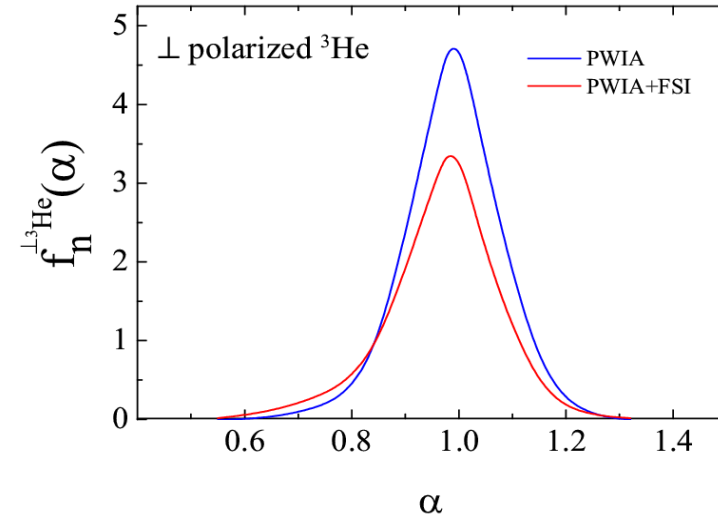
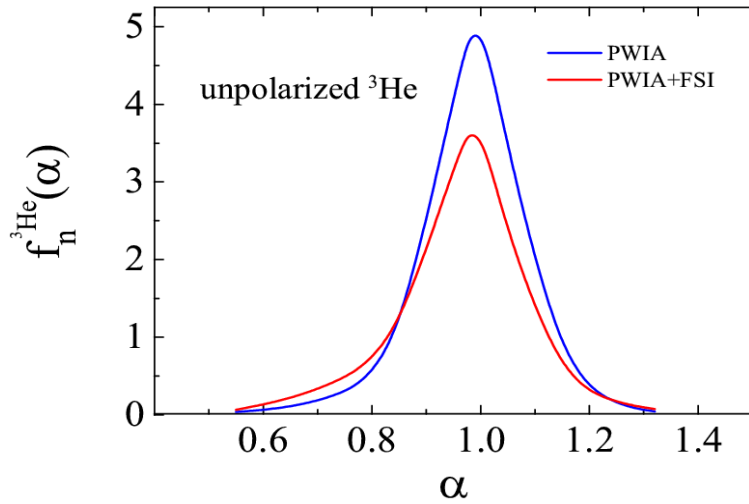
$$\mathbf{n}_G(\mathbf{t}) = \frac{16}{27} \left\{ \ln\left(\frac{Q t_0}{\lambda t}\right) + \ln\left(\frac{t \Lambda_{QCD}}{2}\right) \ln\left[\frac{\ln(Q/\Lambda_{QCD} \sqrt{t_0/t})}{\ln(\lambda/\Lambda_{QCD})}\right] \right. \\ \left. + \ln\left(\frac{Q^2 t_0}{2 \Lambda_{QCD}}\right) \ln\left[\frac{\ln(Q/\Lambda_{QCD})}{\ln(Q/\Lambda_{QCD} \sqrt{t_0/t})}\right] \right\}$$



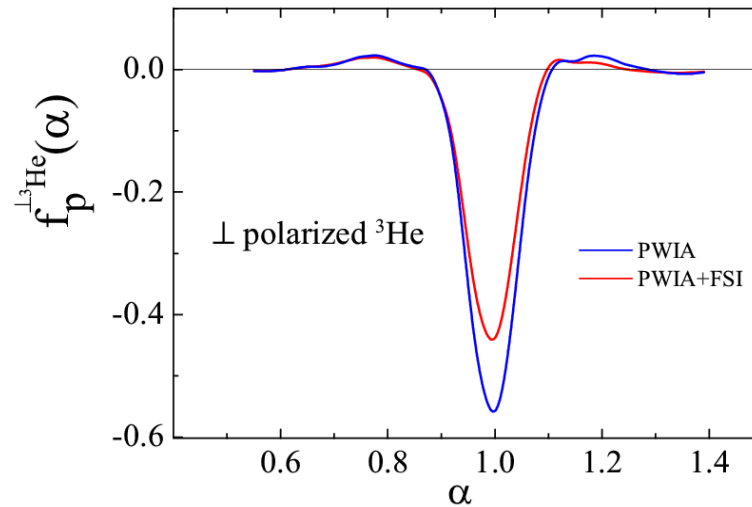
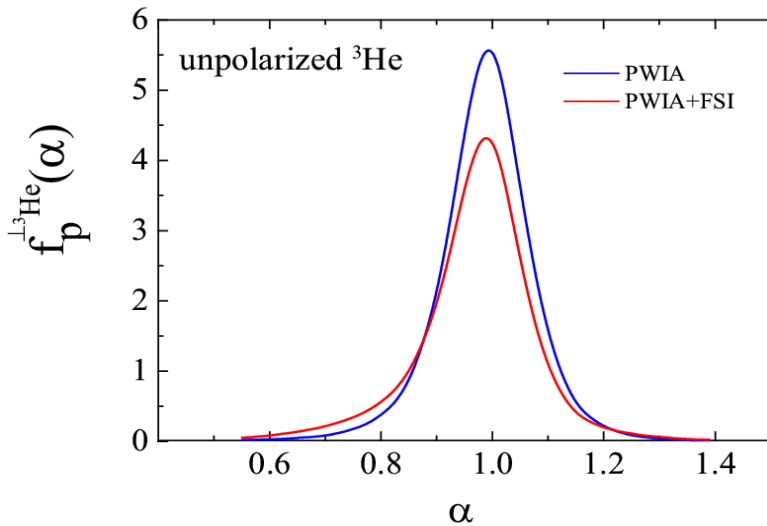
C. CdA, L.P.K, B.Z. Kopeliovich, *E.P.J. A19* (2004) 133; *ibid* p. 145

V. Palli, C. CdA, L.P.K, C.B. Mezzetti, M. Alvioli, *PRC 80* (2009) 054610; *ibid* *PRC C81* (2010)

## NEUTRON



## PROTON



# DILUTION FACTORS

$$A_3^{exp} \simeq \frac{\Delta \vec{\sigma}_3^{exp.}}{\sigma_{unpol.}^{exp.}} \Rightarrow \frac{\langle \vec{s}_n \rangle \Delta \vec{\sigma}(\mathbf{n}) + 2 \langle \vec{s}_p \rangle \Delta \vec{\sigma}(\mathbf{p})}{\langle \mathbf{N}_n \rangle \sigma_{unpol.}(\mathbf{n}) + 2 \langle \mathbf{N}_p \rangle \sigma_{unpol.}(\mathbf{p})} = \langle \vec{s}_n \rangle \mathbf{d}_n \mathbf{A}_n + 2 \langle \vec{s}_p \rangle \mathbf{d}_p \mathbf{A}_p$$

PWIA:

$$\langle \vec{s}_{n(p)} \rangle = \int dE \int d^3p P_{||}(E, \mathbf{p}) = \mathbf{p}_{n(p)};$$

$$\langle N \rangle = \int dE \int d^3p P_{unpol.}(E, \mathbf{p}) = 1.$$

$$\mathbf{d}_{n,(p)}(\mathbf{x}, \mathbf{z}) = \frac{\sum_q e_q^2 f_1^{q,n(p)}(\mathbf{x}) D_1^{q,h}(\mathbf{z})}{\sum_N \sum_q e_q^2 f_1^{q,N}(\mathbf{x}) D_1^{q,h}(\mathbf{z})}$$

FSI:

$$\langle \vec{s}_{n(p)} \rangle = \int dE \int d^3p P_{||}^{FSI}(E, \mathbf{p}) = \mathbf{p}_{n(p)}^{FSI};$$

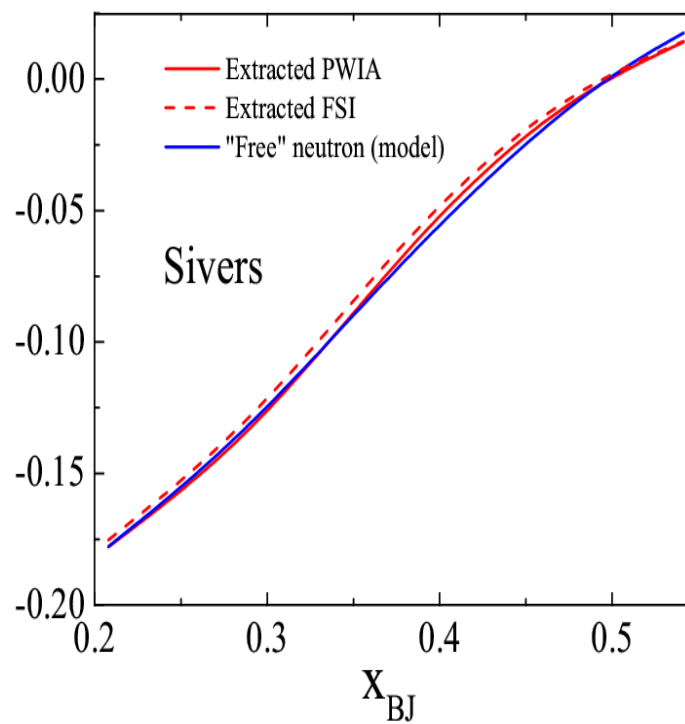
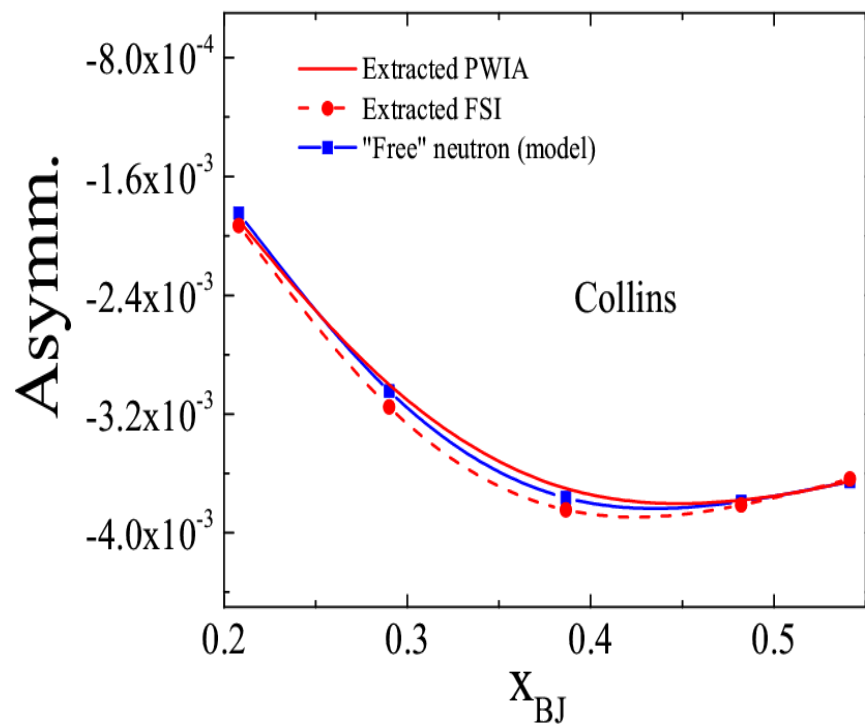
$$\langle N \rangle = \int dE \int d^3p P_{unpol.}^{FSI}(E, \mathbf{p}) < 1.$$

$$\mathbf{d}_{n,(p)}^{FSI}(\mathbf{x}, \mathbf{z}) = \frac{\sum_q e_q^2 f_1^{q,n(p)}(\mathbf{x}) D_1^{q,h}(\mathbf{z})}{\sum_N \langle \mathbf{N} \rangle \sum_q e_q^2 f_1^{q,N}(\mathbf{x}) D_1^{q,h}(\mathbf{z})}$$

$$\mathbf{A}_n \simeq \frac{1}{\mathbf{p}_n^{FSI} \mathbf{d}_n^{FSI}} \left( \mathbf{A}_3^{exp} - 2 \mathbf{p}_p^{FSI} \mathbf{d}_p^{FSI} \mathbf{A}_p^{exp} \right) \simeq \frac{1}{\mathbf{p}_n \mathbf{d}_n} \left( \mathbf{A}_3^{exp} - 2 \mathbf{p}_p \mathbf{d}_p \mathbf{A}_p^{exp} \right)$$



## Extracted Asymmetries



## **INTERMEDIATE** conclusions

- PWIA describes data fairly well at low and moderate intrinsic momenta (up to 250-300 MeV/c)
- PWIA + GEA describes data in the whole kinematical region in q.e. ( $\sigma = \sigma_{NN}$ ) high energy e.m. processes off  $^3\text{He}$
- PWIA + GEA with factorization adequately describes unpolarized spectator SIDIS ( $\sigma = \sigma_{\text{eff}}(t, Q^2, x_{Bj})$ ) at intrinsic momenta up to 400-500 MeV/c
- Since in the “standard” SIDIS processes one integrates over undetected removal energy and momenta (from 0 to infinity) the PWIA + GEA ( $\sigma = \sigma_{\text{eff}}(t, Q^2, x_{Bj})$ ) with factorization can be applied to extract free Information information also from polarized SIDIS processes

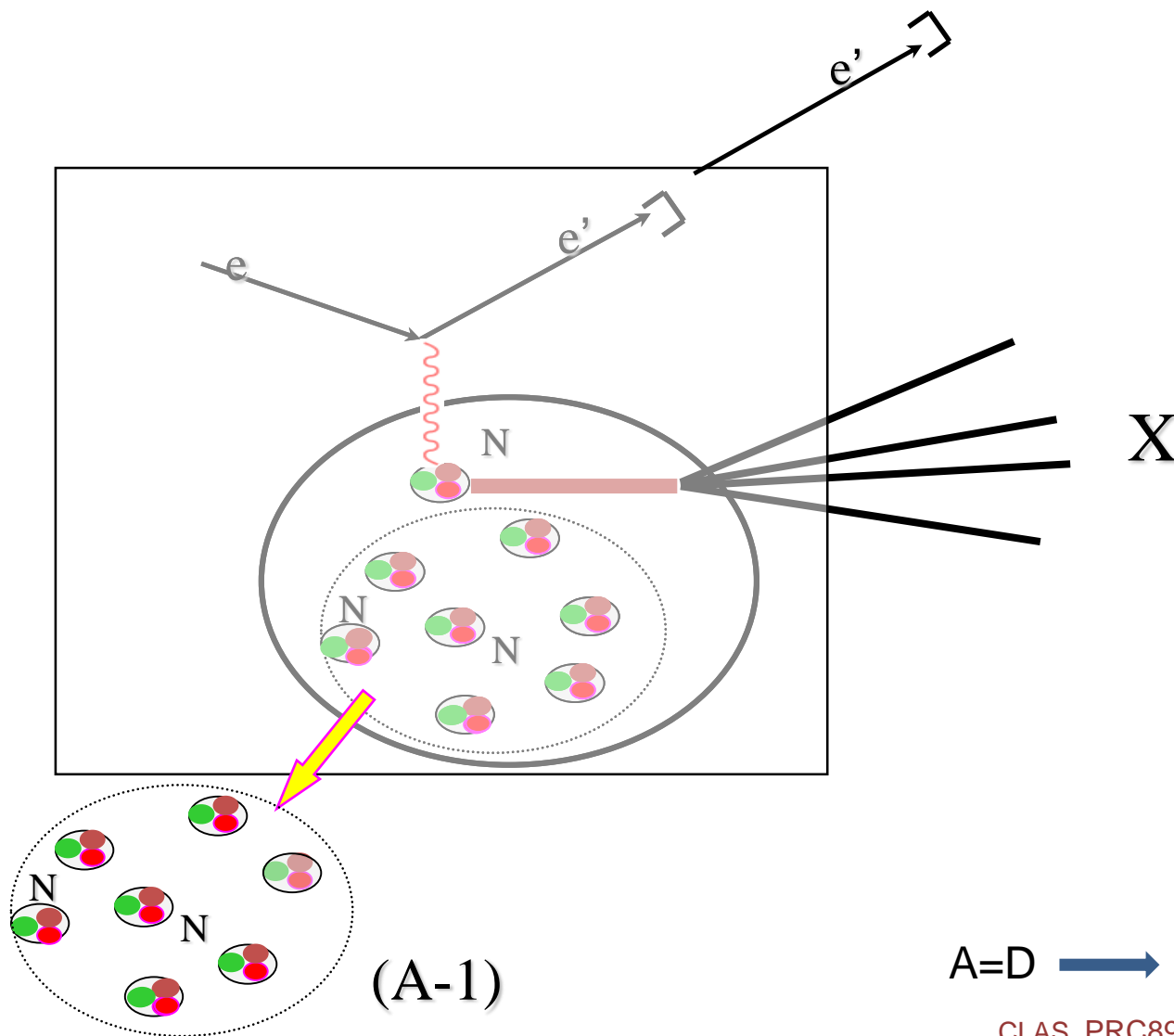
# Tagging the Nucleon Structure in the “Spectator” SIDIS

In spite of many experimental and theoretical efforts, the origin of the nuclear EMC effect exhibited by **INCLUSIVE DIS** of leptons off nuclei, has not yet been fully clarified, and the problem as to whether and to what extent the quark distributions of nucleons undergo deformations due to the nuclear medium remains open. We argue that in **SPECTATOR SIDIS** off a complex nucleus  $A$ , the detection, in coincidence with the scattered electron, of a nucleus  $(A - 1)$  in the ground or excited state may provide unique information on:

- i)* **the medium induced modifications of the nucleon structure function and the origin of the *EMC* effect**, and
- ii)* **the mechanism of quark hadronization in the nuclear medium.**

C. Ciofi degli Atti, L. P.K., S. Scopetta, EPJA 5 (1999) 191; PRC 83 (2011) 044602,;  
C. Ciofi degli Atti, L.P.K. , B. Kopeliovich, EPJ A19, (2004), 133 C. Ciofi degli Atti, L. P.K., and  
C. Mezzeti Fizika B20 (2011) 161  
CLAS, Phys.Rev. C89 (2014) 4, 045206, Phys.Rev. C90 (2014) 5, 059901  
L. P.K., A. Del Dotto, E. Pace, G. Salm`e, S.Scopetta., PRC 89 (2014) 035206

# Tagging the Nucleon Structure in the "Spectator" SIDIS



$A=D \rightarrow$  Deeps(BONUS)

CLAS, PRC89 (2014) 4, 045206,  
PRC90 (2014) 5, 059901

# Tagging the Nucleon Structure in the “Spectator” SIDIS

$$\frac{d\vec{\sigma}^{A,FSI}}{dx_{Bj}dQ^2dEd\mathbf{P}_{A-1}} = K^A(x_{Bj}, Q^2, y_A, z_1^{(A)}) \left(\frac{y}{y_A}\right)^2 z_1^{(A)} \mathcal{F}^{N/A}(x_A, Q^2, k_1^2) \vec{P}^A(E, \mathbf{P}_{A-1}),$$

$$K^A(x_{Bj}, Q^2, y_A, z_1^{(A)}) = \frac{4\alpha_{em}^2}{Q^4} \frac{\pi}{x_{Bj}} \cdot \left[ \frac{y_A^2}{2} + (1 - y_A) - \frac{k_1^2 x_{Bj}^2 y_A^2}{z_1^{(A)2} Q^2} \right].$$

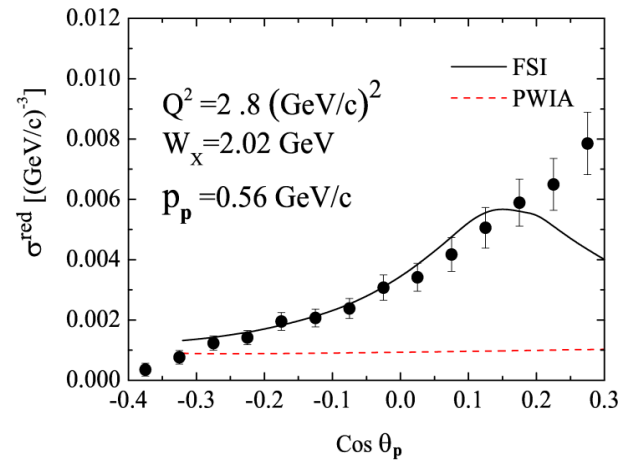
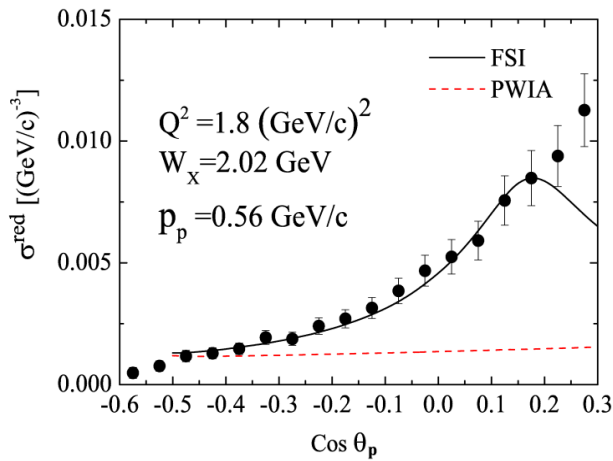
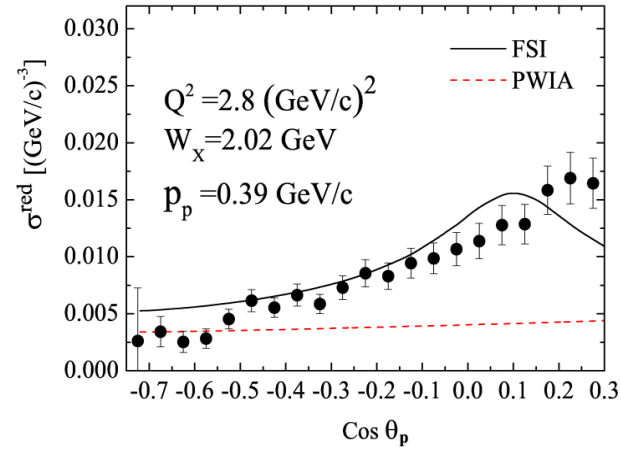
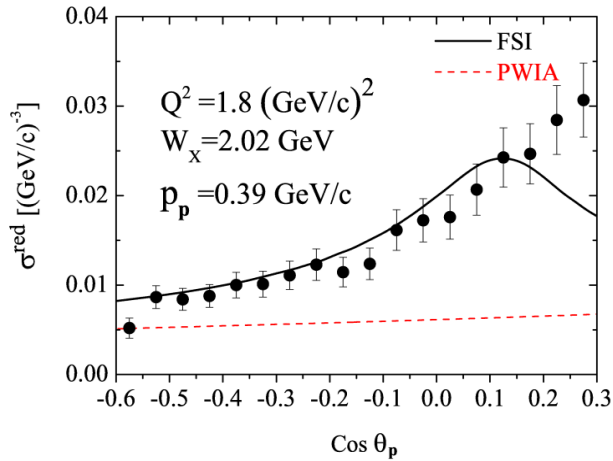
$$y_A = \frac{k_1 \cdot q}{k_1 \cdot k_e}, \quad x_A = \frac{x_{Bj}}{z_1^{(A)}}, \quad z_1^{(A)} = \frac{k_1 \cdot q}{m_N \nu}, \quad , \quad k_1 = P_A - P_{A-1}.$$

$$\vec{\sigma}^{red}(x_{Bj}, Q^2, \mathbf{p}_p) = \frac{1}{K^A(x_{Bj}, y_A, Q^2)} \left(\frac{y_A}{y}\right)^2 \frac{1}{z_1^{(A)}} \frac{d\vec{\sigma}^{A,exp}}{dx_{Bj}dQ^2dEd\mathbf{p}_{A-1}}$$

$$\vec{\sigma}^{red}(x_{Bj}, Q^2, \mathbf{p}_p) = \mathcal{F}^{N/D}(x_A, Q^2, k_1^2) \vec{P}^A(E, \mathbf{p}_p)$$

# Tagging the Hadronization Mechanism

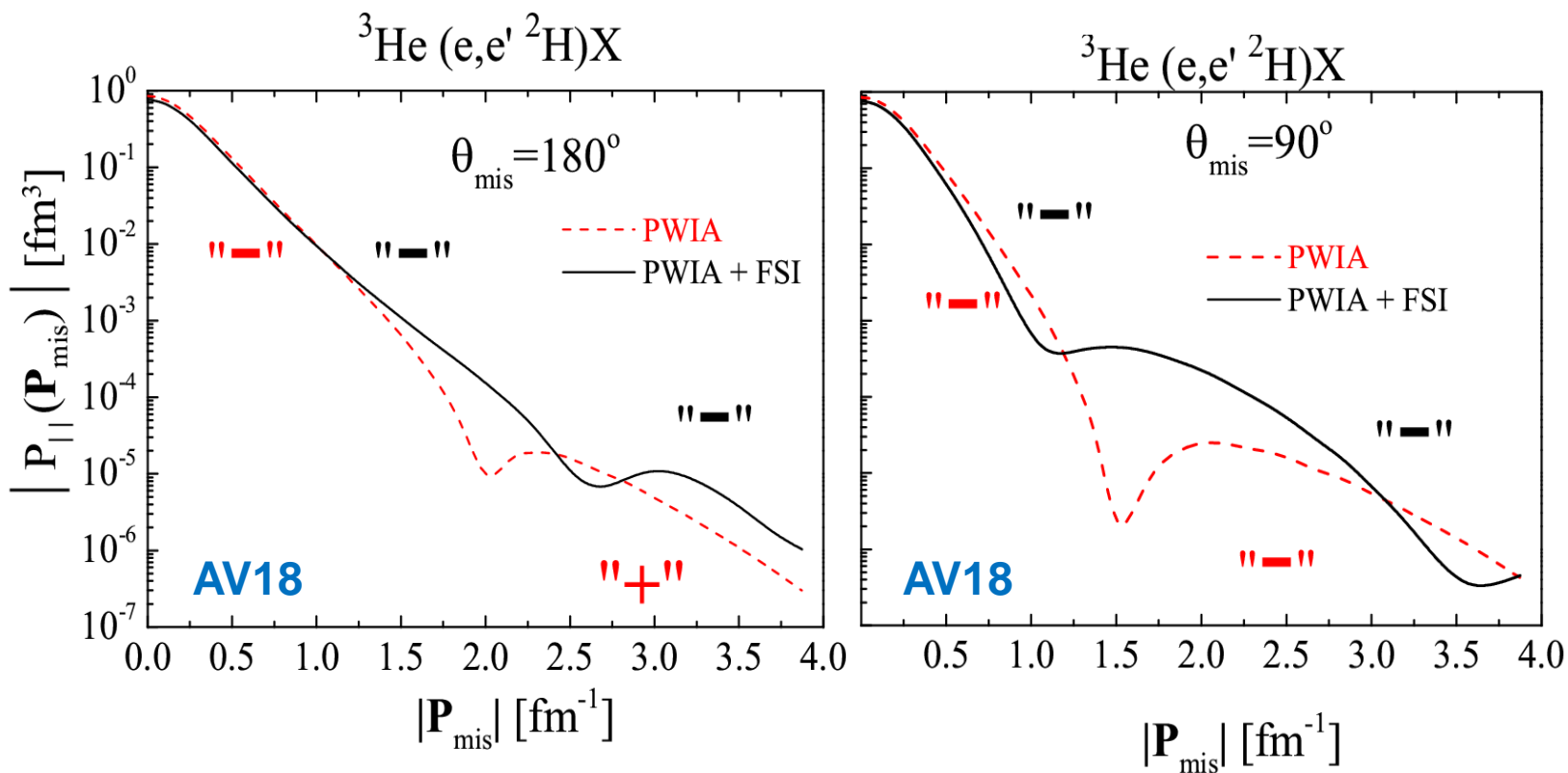
## $D(e, e'p)X$ (Recent Jlab experiment)



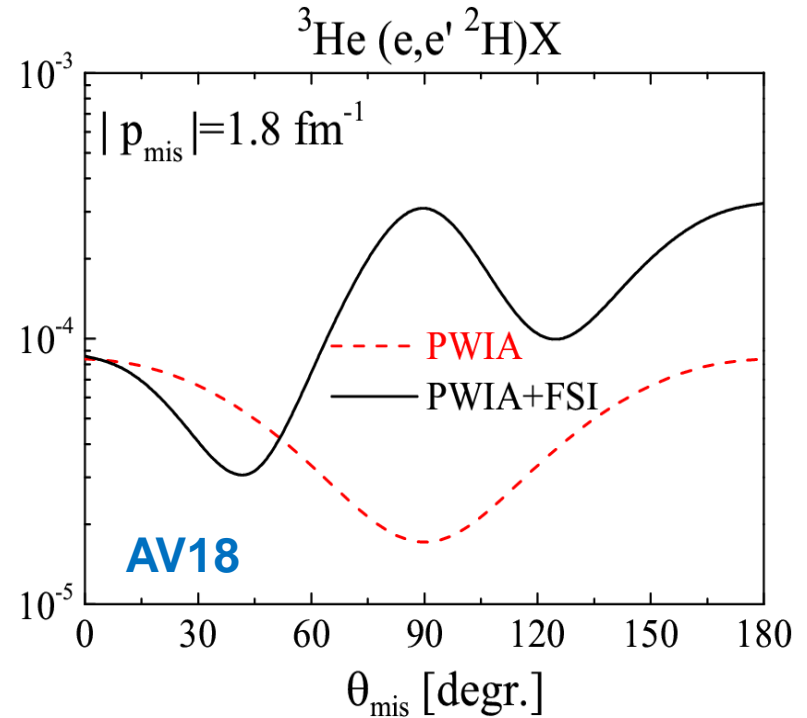
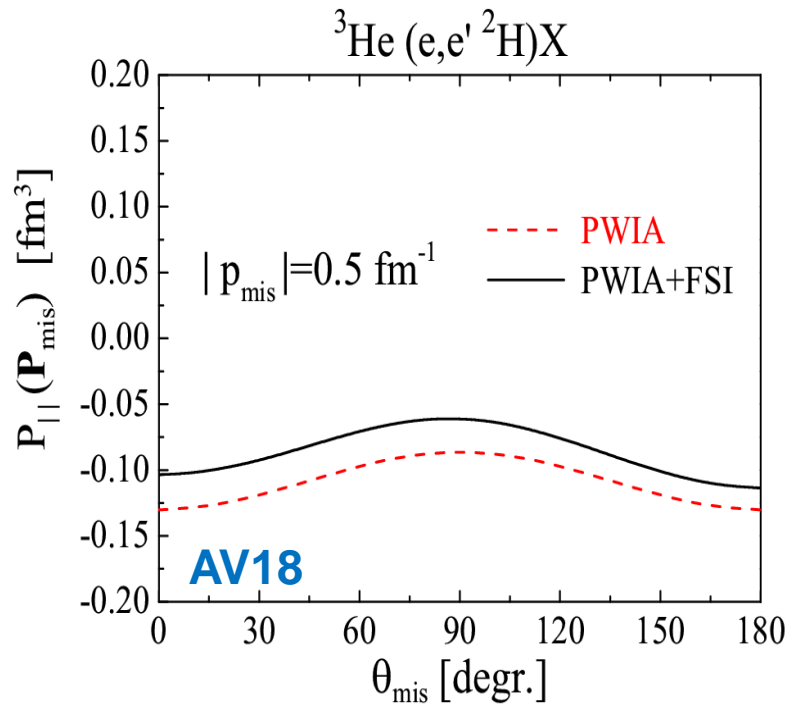
C. CdA, L.P.K, B.Z. Kopeliovich, *E.P.J. A19* (2004) 133; *ibid p. 145*  
 V. Palli, C. CdA, L.P.K, C.B. Mezzetti, M. Alvioli, *PRC 80* (2009) 054610; *ibid PRC C81*(2010)  
 C. CdA, L.P.K, C.B. Mezzetti, *Fizica 20*, (2012); W. Cosyn, M. Sargsian *PRC 84* (2011) 014601

# Tagging the Spin Dependent Spectral Function

L. P.K., A. Del Dotto, E. Pace, G. Salm`e, S.Scopetta., PRC 89 (2014) 035206



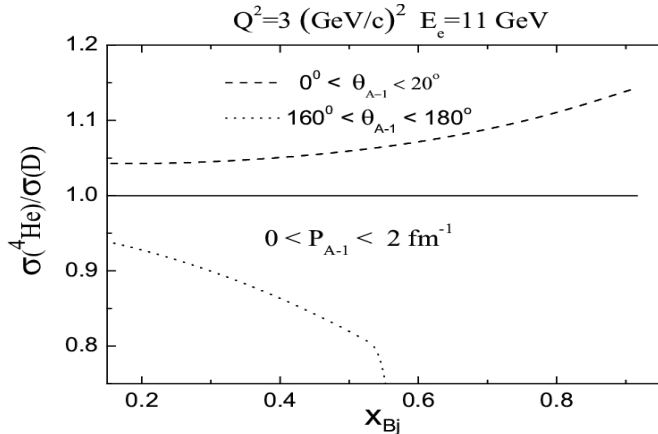
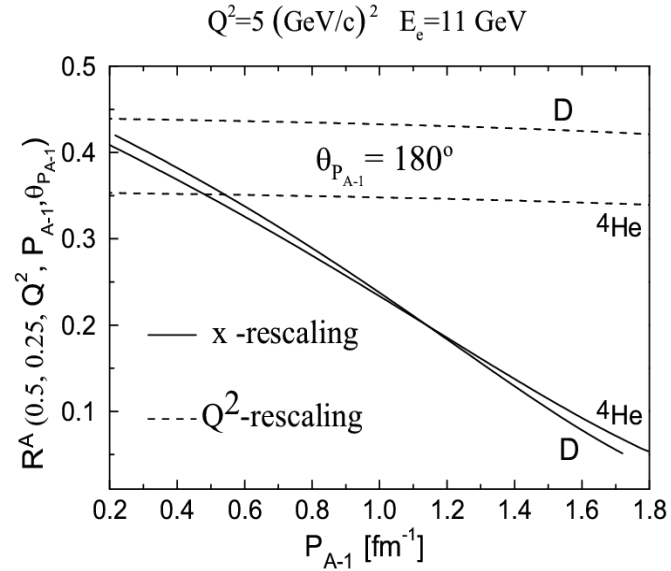
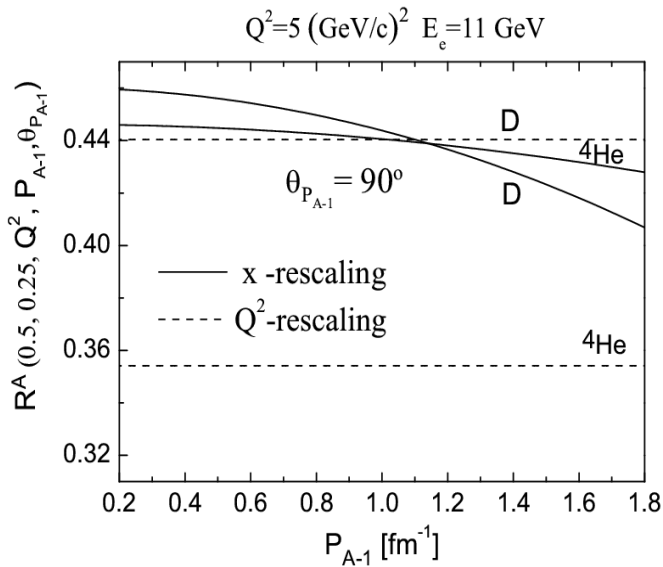
## The Parallel (along the target polarization) Spin Dependent Spectral Function $P_{||}(\mathbf{p}_{\text{mis}}, \theta_{\text{mis}})$





# Tagging the EMC-effect

$$R(x_{Bj}, x'_{Bj}, Q^2, |\mathbf{P}_{A-1}|, z_1^{(A)}, y_A) = \frac{\sigma^{A,exp}(x_{Bj}, Q^2, |\mathbf{P}_{A-1}|, z_1^{(A)}, y_A)}{\sigma^{A,exp}(x'_{Bj}, Q^2, |\mathbf{P}_{A-1}|, z_1^{(A)}, y_A)} \rightarrow \frac{F_2^{N/A}(x_A, Q^2, k_1^2)}{F_2^{N/A}(x'_A, Q^2, k_1^2)}$$



C. Ciofi degli Atti, L. P.K., S. Scopetta, EPJA 5 (1999) 191; CdA, LPK, PRC 83 (2011) 044602,;

# SUMMARY

✂ **Plane Wave Impulse Approximation (PWIA)** seems to describe rather well the Semi-Inclusive Processes  ${}^3\text{He}(e, e'p(pn)X)$ ,  ${}^3\text{He}(e, e'h)X$ ,  ${}^2\text{H}(e, e'p)X$ , etc. This, **at first glance**, justifies the use of the simple formula  $A_n \simeq \frac{1}{p_n f_n} (A_3^{\text{exp}} - 2p_p f_p A_p^{\text{exp}})$  to extract the Sivers and Collins asymmetries from data on polarized  ${}^3\text{He}$ .

✂ PWIA holds only in a restricted kinematical range of intrinsic momenta and removal energies. Beyond this region the **Final State Interaction (FSI)** plays an important role. It leads to a partial depolarization of nucleons and hinders the use of the simple extraction procedure. However, by a proper redefinition of polarizations  $p_{n(p)}$  and dfunctions  $f_{n(p)}$  one can derive a similar formula for the asymmetries which takes properly into account **FSI** effects.

✂ The extraction procedures within the PWIA and with FSI taken into account provide (with most deviation  $< 4\%$ ) basically the same results and, consequently, the PWIA procedure can be safely applied even in the presence of FSI effects.

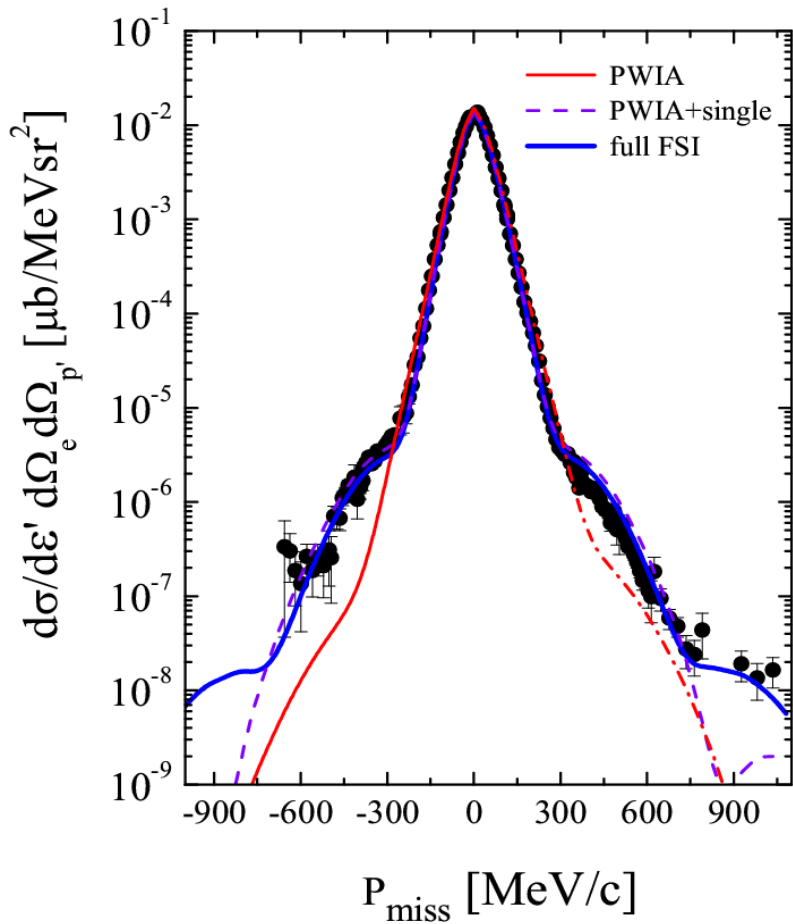
✂ An unambiguous, model independent, extraction of the T-odd asymmetries would be possible in a "double" SIDIS process, when the  $(A-1)$  nucleus is also detected.

✂ Moreover, it is argued that such a "spectator" SIDIS can serve as a powerful tool to also provide unique information on: *i)* the in-medium induced modifications of the nucleon parton distributions and the origin of the EMC effect, and *ii)* the mechanism of quark hadronization in the nuclear medium

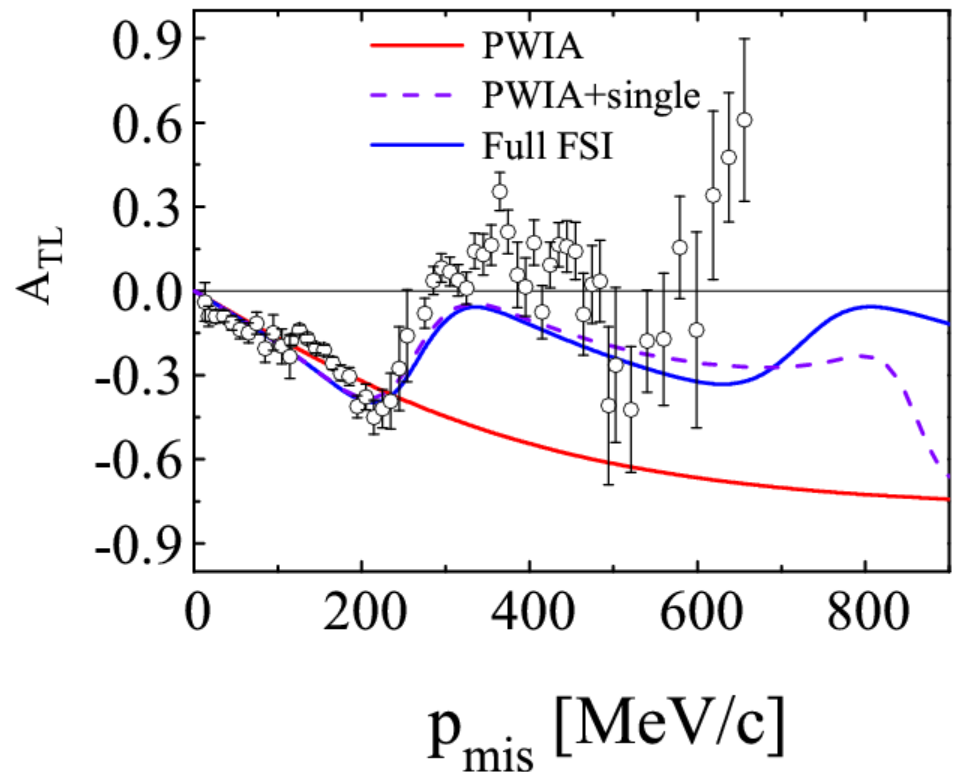


# Check of the GEA: unfactorized calcs. of $q.e \ ^3He(e, e, p)D$ .

M. Alvioli, CdA & LPK *PRC* 81 (Rapid Comm.) (2010) 02100, R. Schiavilla et al, *PRC*. 72 064003 (2005),



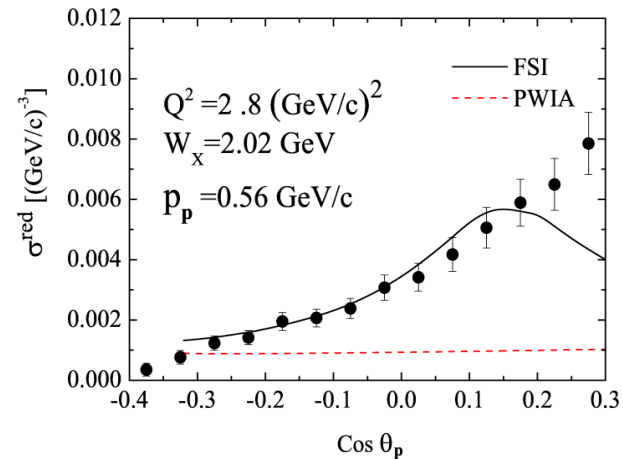
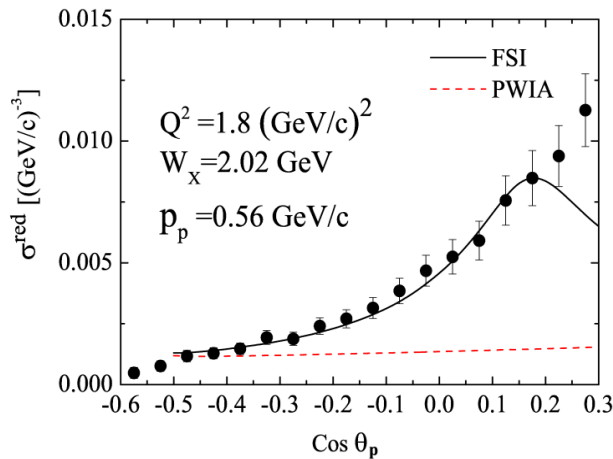
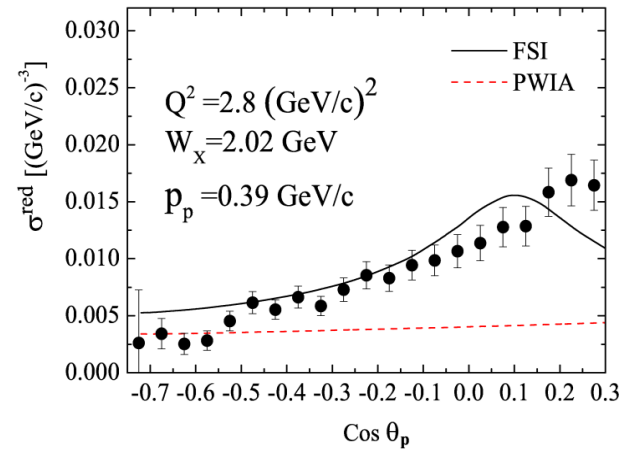
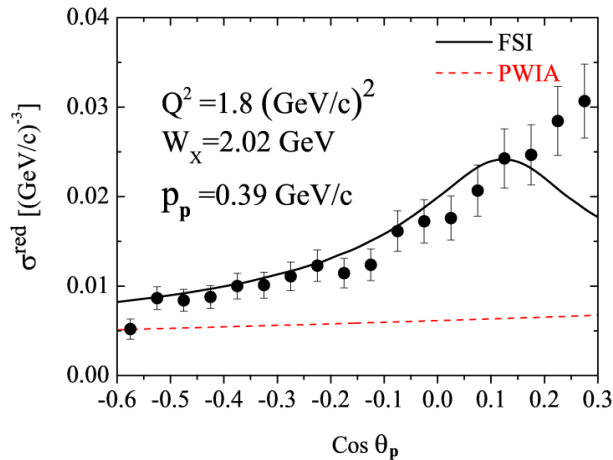
$$A_{TL} = \frac{d\sigma(\phi=0^\circ) - d\sigma(\phi=180^\circ)}{d\sigma(\phi=0^\circ) + d\sigma(\phi=180^\circ)}$$



# Check of the factorization of GEA in DIS: $D(e, e'p)X$

C. CdA, L.P.K, B.Z. Kopeliovich, *E.P.J. A***19** (2004) 133; *ibid* p. 145  
V. Palli, C. CdA, L.P.K, C.B. Mezzetti, M. Alvioli, *PRC* **80** (2009) 054610; *ibid* *PRC* **C81**(2010)  
C. CdA, L.P.K, C.B. Mezzetti, *Fizica* **20**, (2012); W. Cosyn, M. Sargsian *PRC* **84** (2011) 014601

## $D(e, e'p)X$ (Recent Jlab experiment)



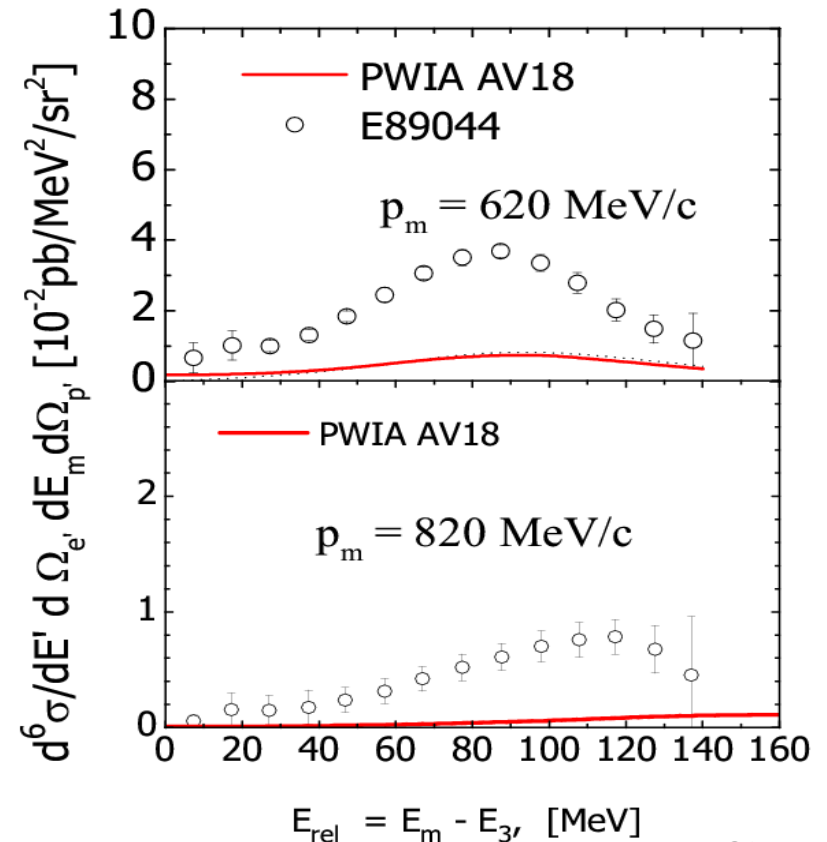
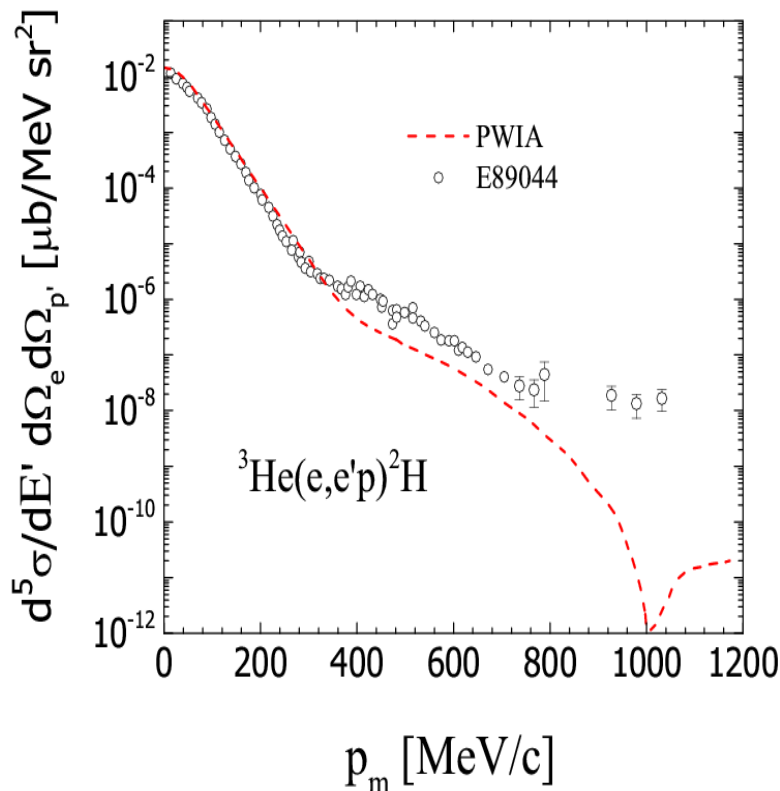


# How “good” is the PWIA approximation?

Results from q.e.  ${}^3\text{He}(e,e')pD$ ,  ${}^3\text{He}(e,e')ppn$

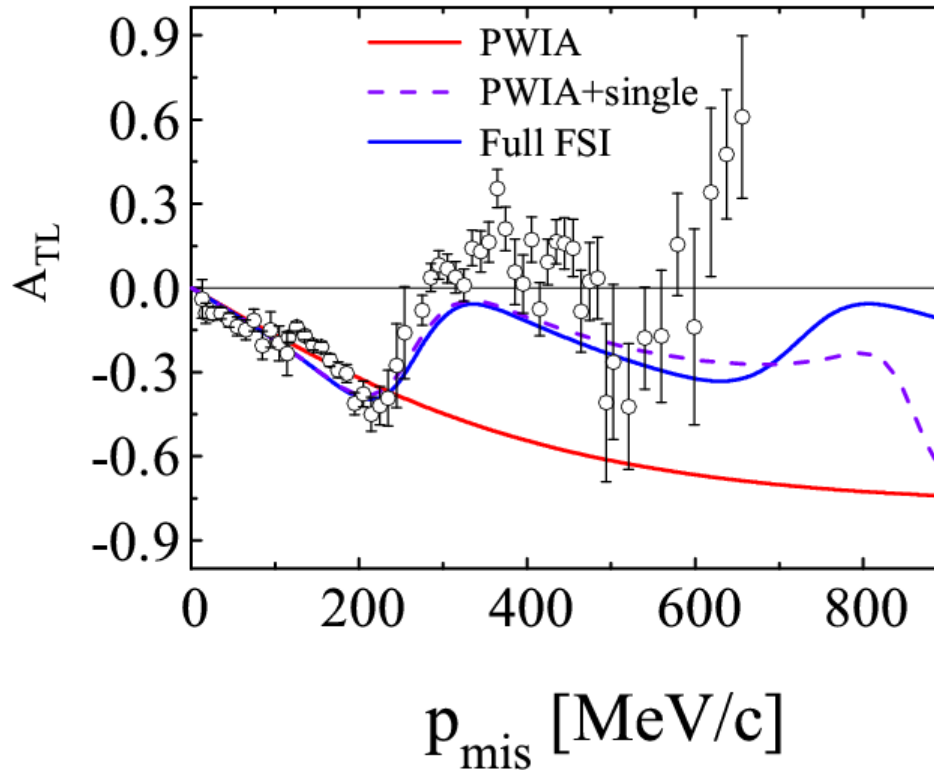
CdA & LPK, *PRL* **95**, 052502 (2005), R. Schiavilla et al, *PRC*. **72** 064003 (2005), L. Frankfurt, M. Sargsian, M. Strikman  
*Int. J.Mod. Phys.* **A23** (2008) 2291

M.M. Rvachev et al., *PRL* **94**(2005) 192302



$$A_{TL} = \frac{d\sigma(\phi=0^\circ) - d\sigma(\phi=180^\circ)}{d\sigma(\phi=0^\circ) + d\sigma(\phi=180^\circ)}$$

q.e.  ${}^3\text{He}(e,e')pD$

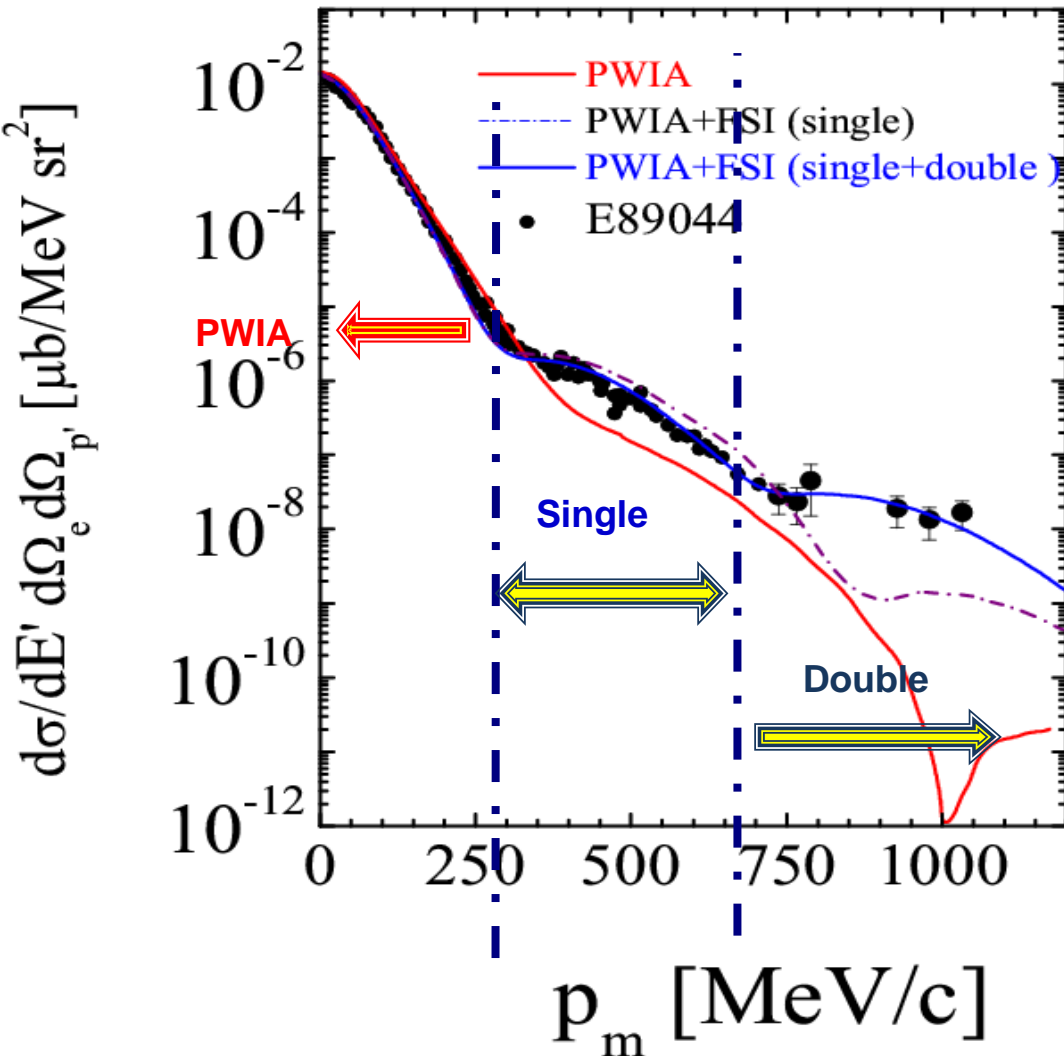


PWIA works for nucleon momenta  $0 < p < 250 \div 300 \text{ meV/c}$

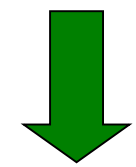


# Multiple Scattering Contributions

CdA & LPK, *PRL* **95**, 052502 (2005), R. Schiavilla et al, *PRC*. **72** 064003 (2005)



$d\sigma(p_m)$  has  
different (three)  
slopes



different Multiple  
Scattering  
Components

1) PWIA:  $\langle p_n \rangle = 0.876$ ,  $\langle p_p \rangle = -0.0237$ ,  $\theta_e = 30^\circ$ ,  $\theta_\pi = 14^\circ$

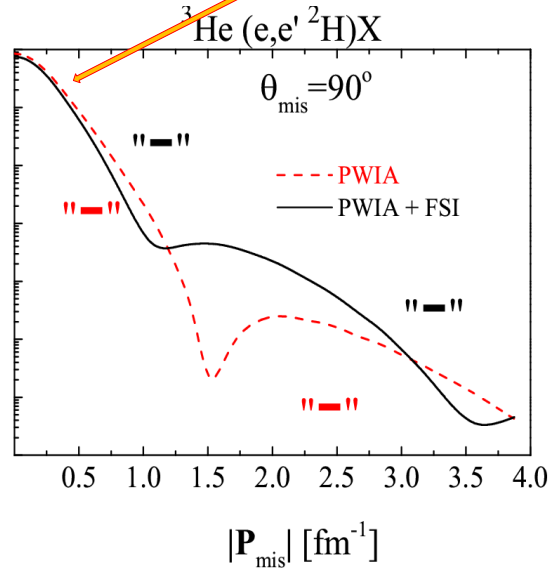
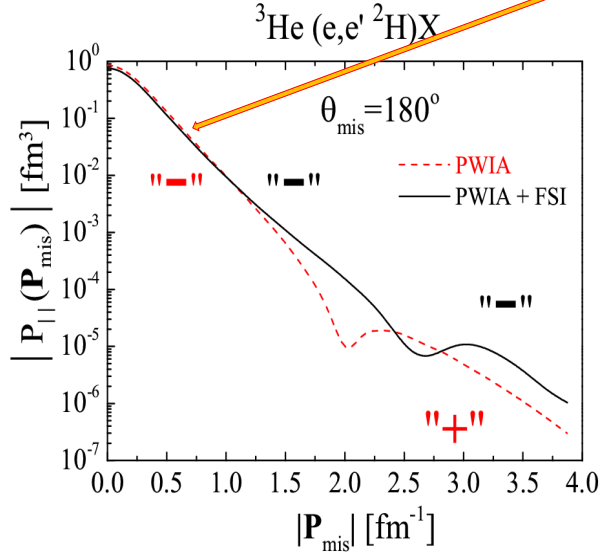
| $E_{beam}$ ,<br>GeV | $x_{Bj}$ | $\nu$<br>GeV | $p_\pi$<br>GeV/c | $f_n(x, z)$ | $\langle p_n \rangle f_n$ | $f_p(x, z)$ | $\langle p_p \rangle f_p$ |
|---------------------|----------|--------------|------------------|-------------|---------------------------|-------------|---------------------------|
| 8.8                 | 0.21     | 7.55         | 3.40             | 0.304       | <b>0.266</b>              | 0.348       | $-8.410^{-3}$             |
| 8.8                 | 0.29     | 7.15         | 3.19             | 0.286       | <b>0.251</b>              | 0.357       | $-8.510^{-3}$             |
| 8.8                 | 0.48     | 6.36         | 2.77             | 0.257       | <b>0.225</b>              | 0.372       | $-8.910^{-3}$             |
| 11                  | 0.21     | 9.68         | 4.29             | 0.302       | <b>0.265</b>              | 0.349       | $-8.310^{-3}$             |
| 11                  | 0.29     | 9.28         | 4.11             | 0.285       | <b>0.25</b>               | 0.357       | $-8.510^{-3}$             |

1) FSI:  $\langle p_n \rangle = 0.756$ ,  $\langle p_p \rangle = -0.0265$ ,  $\langle N_n \rangle = 0.85$ ,  $\langle N_p \rangle = 0.87$ ,  $\langle \sigma_{eff.} \rangle = 71 \text{ mb}$

| $E_{beam}$ ,<br>GeV | $x_{Bj}$ | $\nu$<br>GeV | $p_\pi$<br>GeV/c | $f_n(x, z)$ | $\langle p_n \rangle f_n$ | $f_p(x, z)$ | $\langle p_p \rangle f_p$ |
|---------------------|----------|--------------|------------------|-------------|---------------------------|-------------|---------------------------|
| 8.8                 | 0.21     | 7.55         | 3.40             | 0.353       | <b>0.267</b>              | 0.405       | $-1.110^{-2}$             |
| 8.8                 | 0.29     | 7.15         | 3.19             | 0.332       | <b>0.251</b>              | 0.415       | $-1.110^{-2}$             |
| 8.8                 | 0.48     | 6.36         | 2.77             | 0.298       | <b>0.225</b>              | 0.432       | $-1.210^{-2}$             |
| 11                  | 0.21     | 9.68         | 4.29             | 0.351       | <b>0.266</b>              | 0.405       | $-1.10^{-2}$              |
| 11                  | 0.29     | 9.28         | 4.11             | 0.331       | <b>0.250</b>              | 0.415       | $-1.110^{-2}$             |

$$\mathcal{F}^A(x, \{\alpha\}) \simeq \int_x^A \mathcal{F}^N(\xi/x, \{\alpha\}) f^A(\xi) d\xi; \quad f^A(\xi) = \int dE \int_{\mathbf{p}_{\min}}^{p_{\max}} P^A(\mathbf{p}, E) \delta\left(\xi - \frac{pq}{m\nu}\right) d^3\mathbf{p}$$

$\mathbf{p} = \mathbf{p}_{\min} \rightarrow |\cos \theta_{\mathbf{p}}| = 1$  (FSI minimized, Spectral Function maximized !!!)



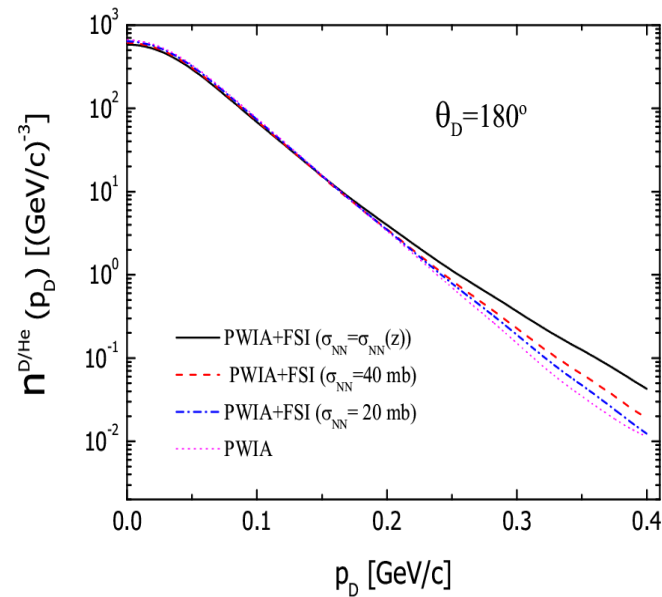
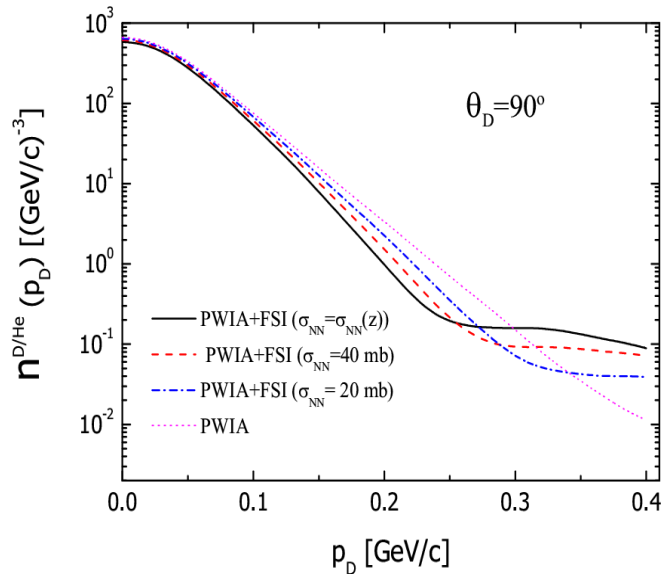
$$\mathbf{A}_{\mathbf{n}} \simeq \frac{1}{\mathbf{p}_{\mathbf{n}}^{\text{FSI}} \mathbf{f}_{\mathbf{n}}} \left( \mathbf{A}_{\mathbf{3}}^{\text{exp}} - 2\mathbf{p}_{\mathbf{p}}^{\text{FSI}} \mathbf{f}_{\mathbf{p}} \mathbf{A}_{\mathbf{p}}^{\text{exp}} \right)$$

$$\mathbf{p}_{\mathbf{N}}^{\text{FSI}} = \int \mathbf{P}_{\parallel}^{\text{N}}(\vec{p}_{\text{mis}}, E) dE d^3 p_{\text{mis}} = \mathbf{p}_{\mathbf{N}}^{\text{PWIA}} - \delta \mathbf{p}_{\mathbf{N}}^{\text{FSI}}(Q^2, \mathbf{x}_{\text{Bj}})$$

Preliminary  $\delta \mathbf{p}_{\mathbf{N}}^{\text{FSI}}(Q^2, \mathbf{x}_{\text{Bj}}) \sim 10 - 15 \%$

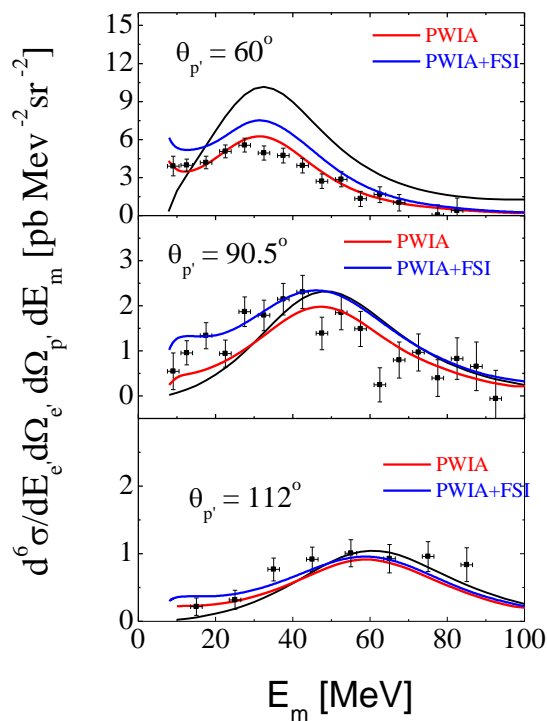
# ${}^3\text{He}(e, e'D)X$

C. CdA, L.P.K, B.Z. Kopeliovich, *EIC white book*, arXiv:1108.1713,INT-PUB-11-034,BNL-96164-2011,JLAB-THY-11-1373. Aug 2011. 547 pp., e-Print: arXiv:1108.1713 [nucl-th]

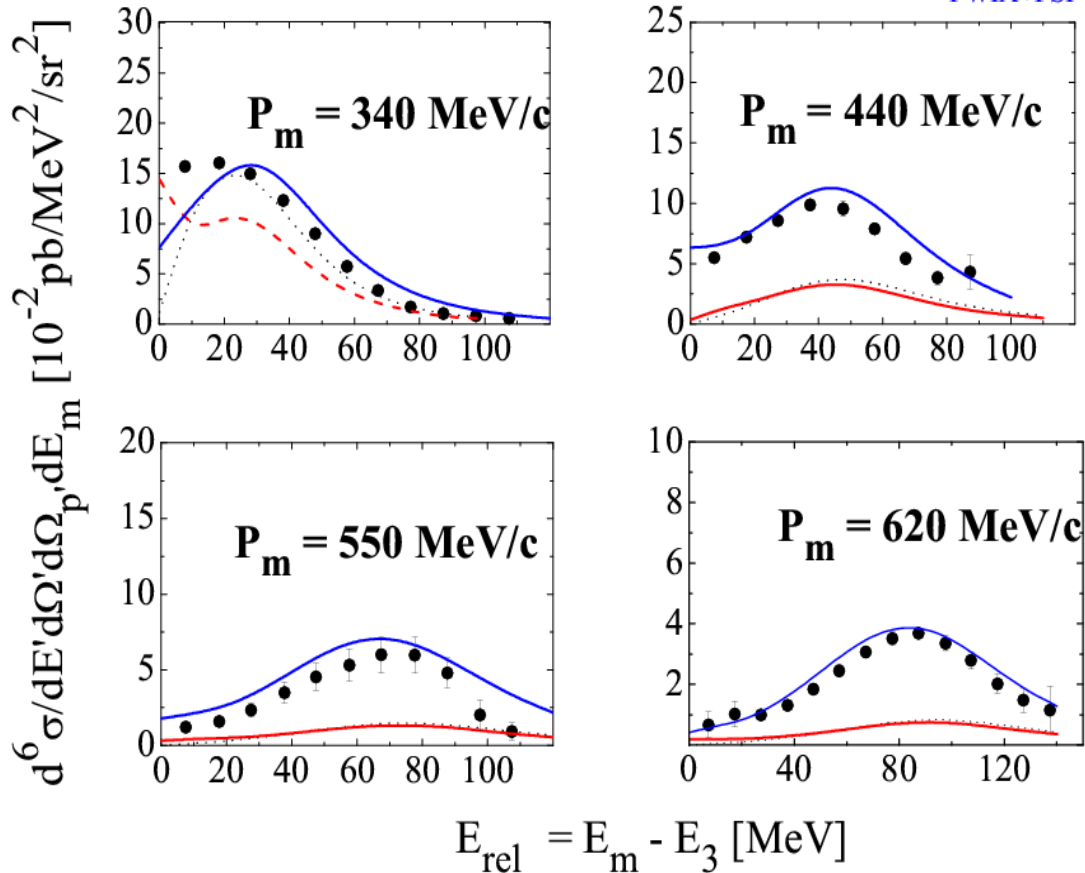


3bbu

$^3\text{He}(e,e'p)pn$  (SACLAY kinem.)



JLAB 89084



CdA & LPK, *PRL* **95**, 052502 (2005), L. Frankfurt, M. Sargsian, M. Strikman *Int. J.Mod. Phys. A* **23** (2008) 2291

$$d\sigma(eA) \sim l^{\mu\nu} \cdot W_{\mu\nu}^A(S_A)$$

where

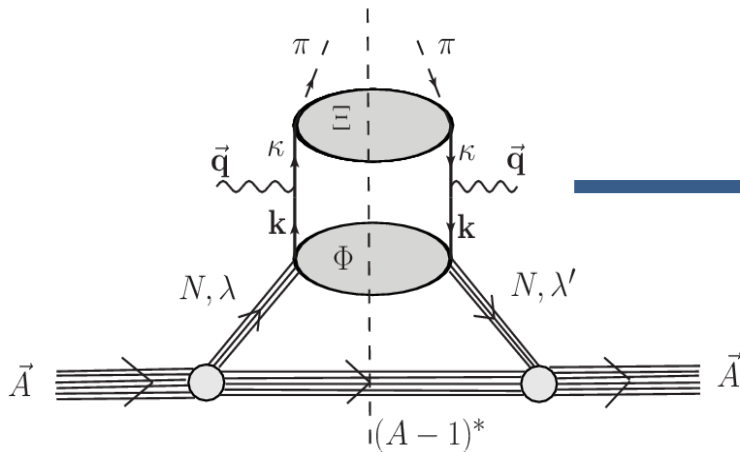
$$W_{\mu\nu}^A = \sum_f \langle \mathbf{P}_A, S_A | \hat{J}_\nu | \mathbf{P}_f \rangle \langle \mathbf{P}_f | \hat{J}_\mu | \mathbf{P}_A, S_A \rangle \delta^{(4)}(q + P_A - P_f) d\tau_X$$

$$W_{\mu\nu}^{MM'} = \sum_{\lambda, \lambda'} \langle \lambda' | \hat{w}_{\mu\nu}^N | \lambda \rangle \mathcal{O}_{\lambda\lambda'}^{MM'}(\mathbf{t}_f, \mathbf{P}_{mis})$$

$$\mathcal{O}_{\lambda\lambda'}^{MM'}(\mathbf{t}_f, \mathbf{P}_{mis}) = \langle \lambda, \phi^{*\mathbf{t}_f}(\mathbf{r}) e^{i\mathbf{P}_{mis}\boldsymbol{\rho}} | \vec{\Psi}_3^M(\mathbf{r}, \boldsymbol{\rho}) \rangle \langle \vec{\Psi}_3^{M'}(\mathbf{r}', \boldsymbol{\rho}') | \lambda', \phi^{\mathbf{t}_f}(\mathbf{r}') e^{-i\mathbf{P}_{mis}\boldsymbol{\rho}} \rangle$$

$$P_{\lambda\lambda'}^{MM'}(E, \mathbf{P}_{mis}) = \int \frac{d\mathbf{t}_f}{(2\pi)^3} \delta\left(E - \frac{t_f^2}{m_N}\right) \mathcal{O}_{\lambda\lambda'}^{MM'}(\mathbf{t}_f, \mathbf{P}_{mis})$$

# The Spin Dependent Spectral Function



$$W_{\mu\nu}^{s.i.}(S^A, Q^2) \sim \sum_{\lambda\lambda'} \langle \lambda' | \hat{w}_{\mu\nu}^N(Q^2, p_N) | \lambda \rangle \mathcal{O}_{\lambda\lambda'}^{S_A}(p_N)$$

$$\mathcal{O}_{\lambda\lambda'}^{MM'(FSI)}(p_N, E) = \int \langle \mathcal{G}(1, 2, 3, \sigma_{eff}^{NX}) \{ \Psi_{23}^t, \lambda, \mathbf{p}_N \} | \Psi_{3He}^M \rangle \langle \Psi_{3He}^{M'} | \mathcal{G}(1, 2, 3, \sigma_{eff}^{NX}) \{ \Psi_{23}^t, \lambda', \mathbf{p}_N \} \rangle \delta \left( E - \frac{t^2}{M_N} \right) \frac{d^3\mathbf{t}}{(2\pi)^3}$$

$$\vec{P}^{S_A}(E, \mathbf{p}_N) = P_{||}^{S_A} \mathbf{e}_0 + P_{1\perp}^{S_A} \mathbf{e}_+ + P_{2\perp}^{S_A} \mathbf{e}_-$$

$$P_{||}^{S_A} = \mathcal{O}_{\frac{1}{2}\frac{1}{2}}^{S_A} - \mathcal{O}_{-\frac{1}{2}-\frac{1}{2}}^{S_A}; \quad P_+^{S_A} = -\sqrt{2}\mathcal{O}_{\frac{1}{2}-\frac{1}{2}}^{S_A}; \quad P_-^{S_A} = \sqrt{2}\mathcal{O}_{-\frac{1}{2}\frac{1}{2}}^{S_A}$$

“||” means along  $S_A$