

# SUSY-QCD corrections in the decay of neutral Higgs bosons into two photons

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*in collaboration with*

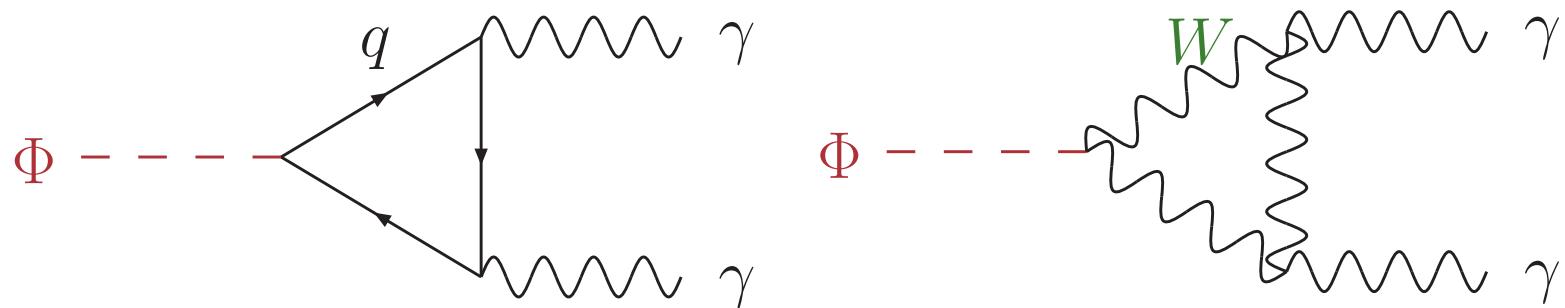
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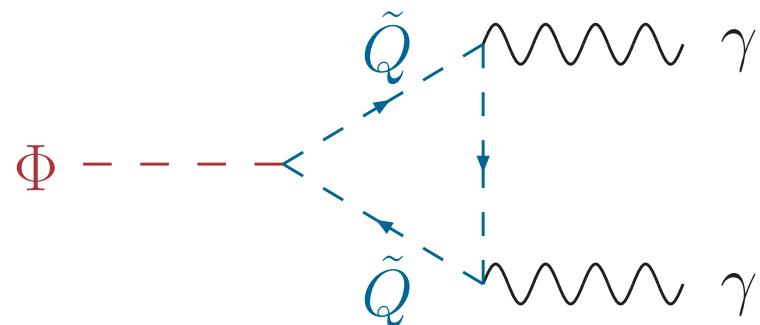
Dubna, July 17th 2006

# Higgs decay into two photons

- Leading order:



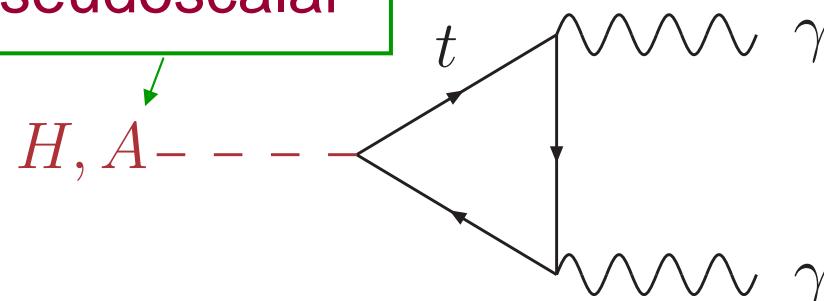
- Contribution of **supersymmetric** particles:



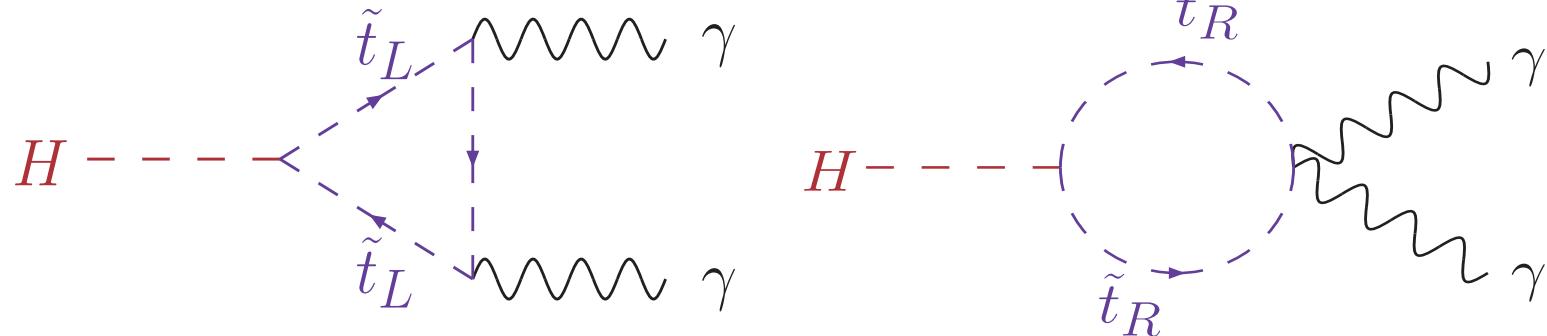
# Neutral Higgs decay into two photons

- SM contribution in LO:

scalar      pseudoscalar



- Superpartner of the top-quarks: stops  $\tilde{t}_{L,R}$



# Content

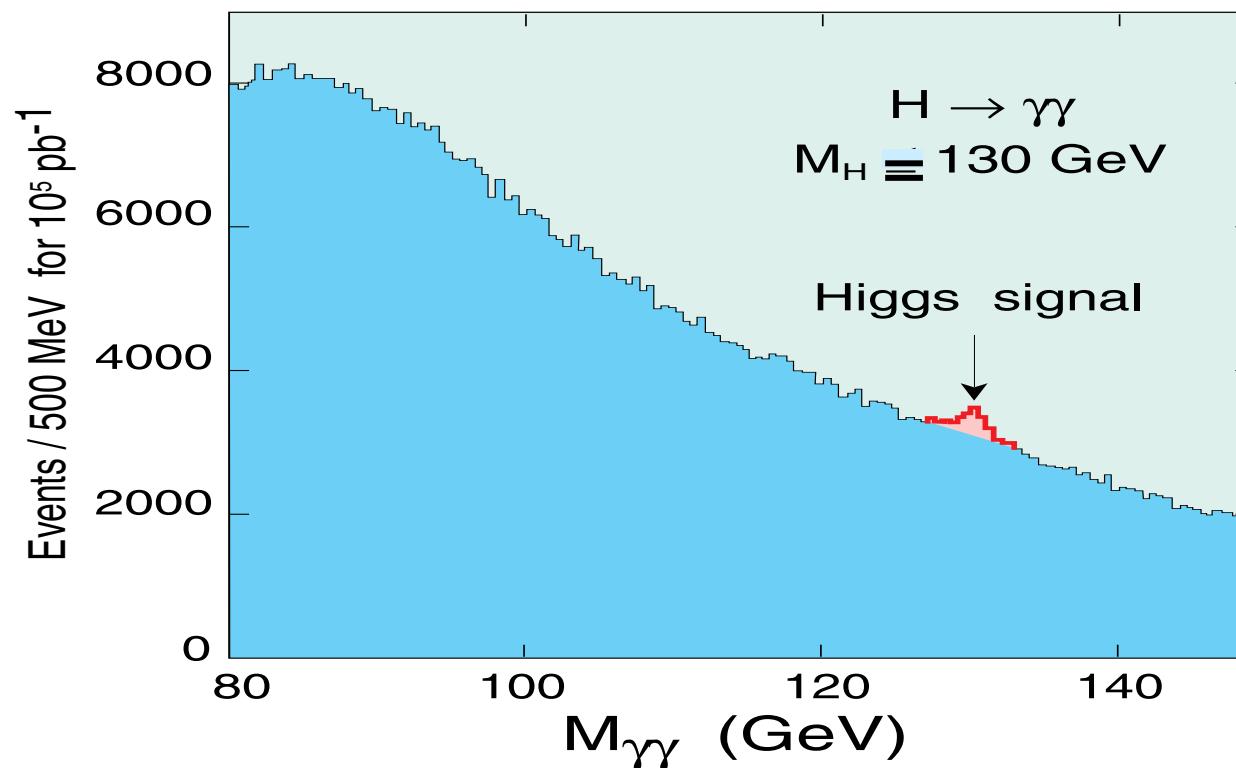
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- Decay of Higgs bosons into photons
- Corrections in higher orders
- Methods
- Results

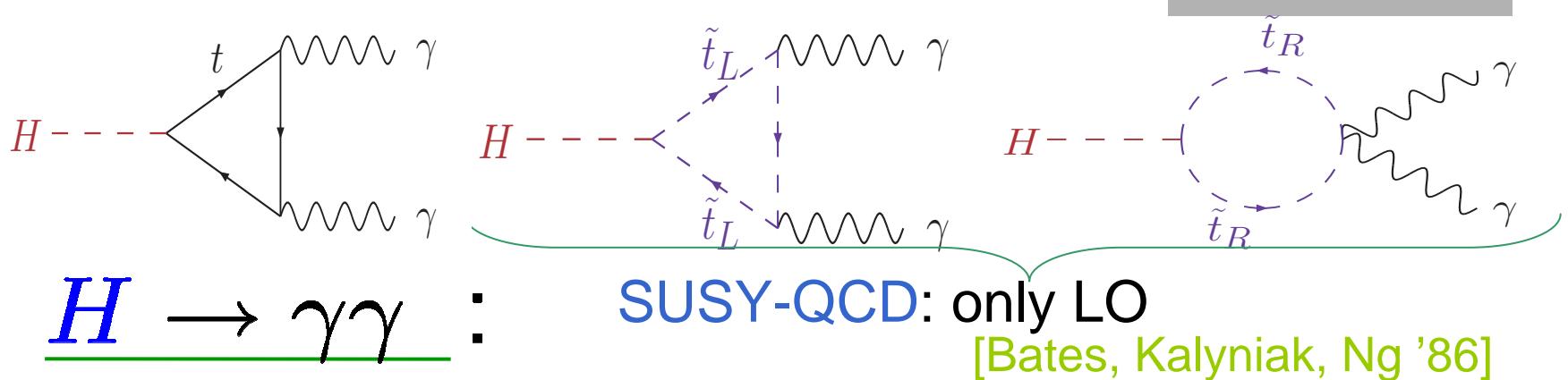
# $H \rightarrow \gamma\gamma$ at the LHC

- Important for Higgs masses

$$m_H \leq 140 \text{ GeV}$$

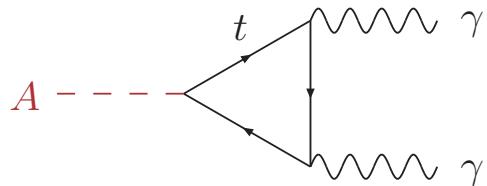


# Corrections in higher orders I



- **NLO-QCD:** [Djouadi et al., '91 ] [Spira et al.,'95]  
[Fleischer, Tarasov, Tarasov, '04 ]  
[Harlander, Kant '05]
- **NNLO-QCD: large top masses** [Steinhauser '97]
- **NLO: electroweak** [Aglietti et al., '04]  
[Fugel, Kniehl, Steinhauser, '04]  
[Degrassi, Maltoni '05]

# Corrections in higher orders II



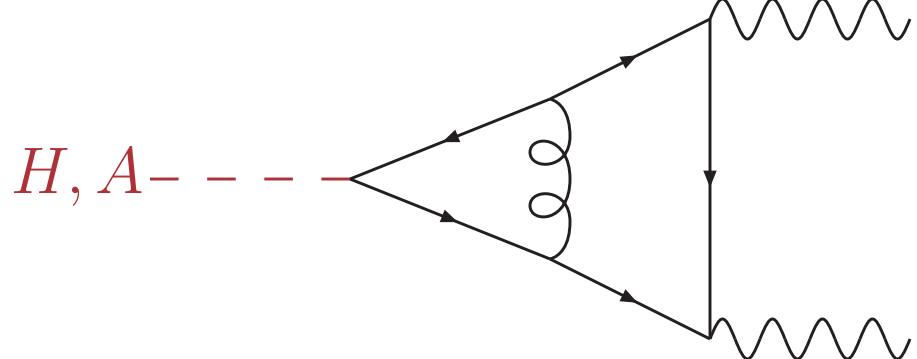
$A \rightarrow \gamma\gamma$ :

- NLO-QCD: [Spira et al., '95]  
[Harlander, Kant '05]

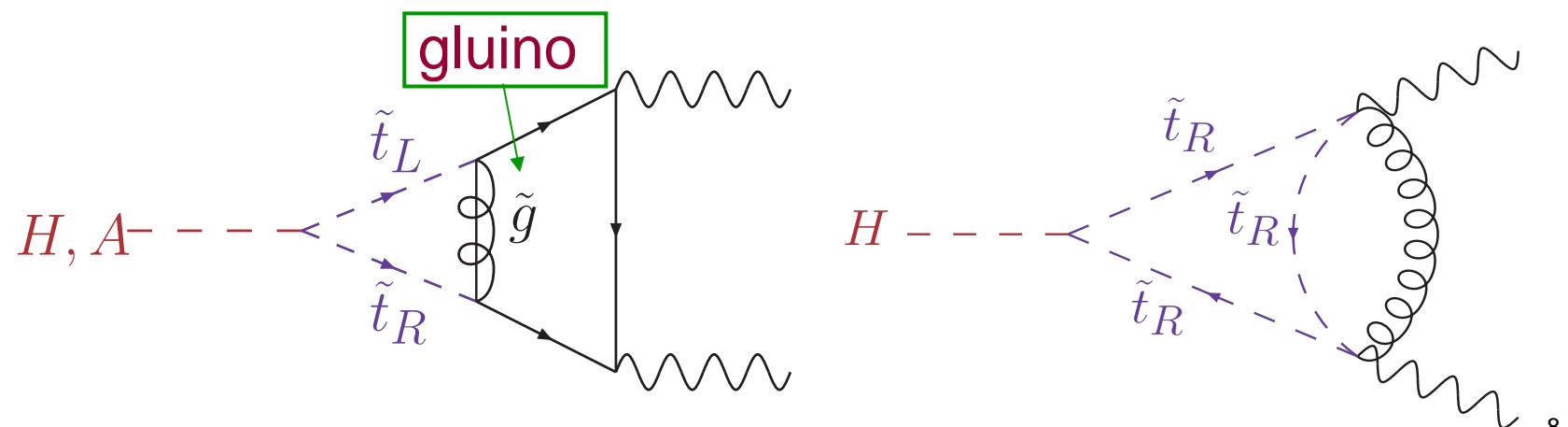
→ SUSY-QCD: NLO ?

# Diagrams in NLO SUSY-QCD

- QCD contributions:



- SUSY-QCD contributions:



# Tensor structure of the amplitude

$$\mathcal{A} = \mathcal{A}_1 + \frac{\alpha_s}{\pi} \mathcal{A}_2 + \dots$$

- Scalar part of the amplitude:

$H \rightarrow \gamma\gamma$  :

$$\mathcal{A}_2^{\mu\nu,H} = (q_1 q_2 g^{\mu\nu} - q_1^\nu q_2^\mu - q_1^\mu q_2^\nu) \mathcal{A}_2^H$$

$q_1, q_2$  : photon 4-momenta

$A \rightarrow \gamma\gamma$  :

$$\mathcal{A}_2^{\mu\nu,A} = (\epsilon^{\mu\nu\alpha\beta} q_{1\alpha} q_{2\beta}) \mathcal{A}_2^A$$

# Projectors

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$$\mathcal{A}_2 = \sum_{l,m,n=0}^{\infty} c_{lmn} (q_1^2)^l (q_2^2)^m (q_1 q_2)^n$$

- on-shell photons:  $q_1^2 = 0, q_2^2 = 0$
- Coefficients  $c_{00n} \sim c_n$  through application of  
→ d'Alembert operators:

$$D_{ij} = \frac{\partial^2}{\partial q_i^\mu \partial q_j^\mu}, \quad i, j = 1, 2$$

# Amplitude in NLO: $H, A \rightarrow \gamma\gamma$

Expansion for  $m_H < \sqrt{2}m_t$

$$\mathcal{A}_2(q_1, q_2) = c_0 + c_1 \left( \frac{q_1 q_2}{m_t^2} \right) + c_2 \left( \frac{q_1 q_2}{m_t^2} \right)^2 + \dots$$

→  $q_1, q_2$  : Photon 4-momenta

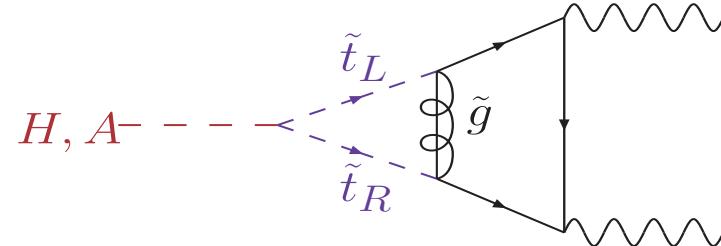
$$q_1 q_2 = \frac{m_H^2}{2}$$

goal:

$$c_n = c_n(m_t, m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{g}})$$

# Methods

- Difficulty:  
up to 4 mass scales



→ Diagrams in asymptotic expansion

e.g.

$$m_t \ll m_{\tilde{t}_1} \ll m_{\tilde{t}_2} \ll m_{\tilde{g}}$$

- Exact calculation:

→ Algorithm by [Davydychev, Tausk '92]

# Tools

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- Diagrams generated with  
QGRAF [Nogueira '93]  $A \rightarrow \gamma\gamma$  : 126 diagrams  
 $H \rightarrow \gamma\gamma$  : 288 diagrams
- translation of symbolic QGRAF-notation with  
Q2E [Seidensticker '99]  
as input for EXP [Harlander, Seidensticker, Steinhauser '98]  
[Seidensticker '99]
- EXP - asymptotic expansions
  - preparation for a FORM based program  
e.g. MATAD [Vermaseren '00]  
[Steinhauser '01]

# Regularization

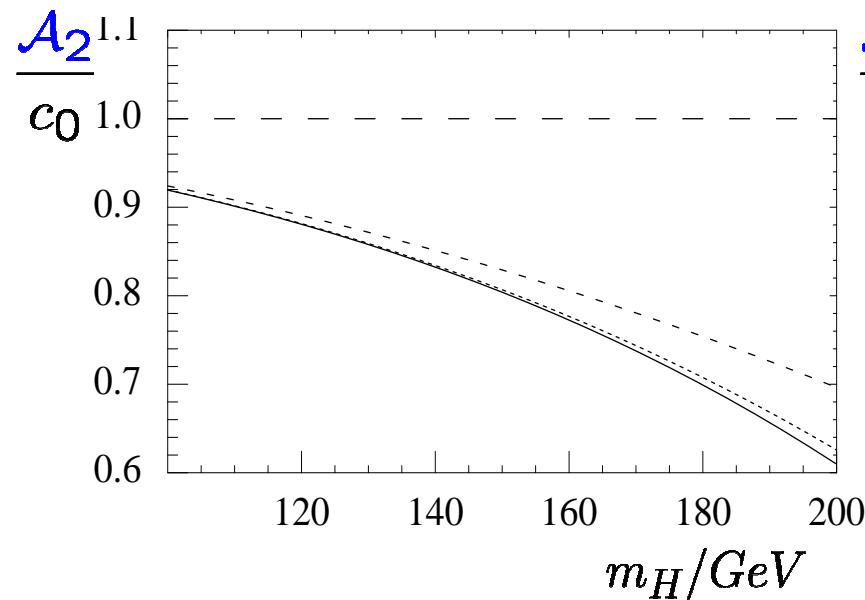
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- Dimensional Regularization (DREG)
  - violates SUSY
  - $A$  pseudoscalar  $\Rightarrow \gamma_5$
  - problems with  $\gamma_5$  in  $d$  dimensions
- Dimensional Reduction (DRED) [Siegel, '79 ]
  - respects SUSY at low orders
  - Lorentz Indices in 4 dimensions

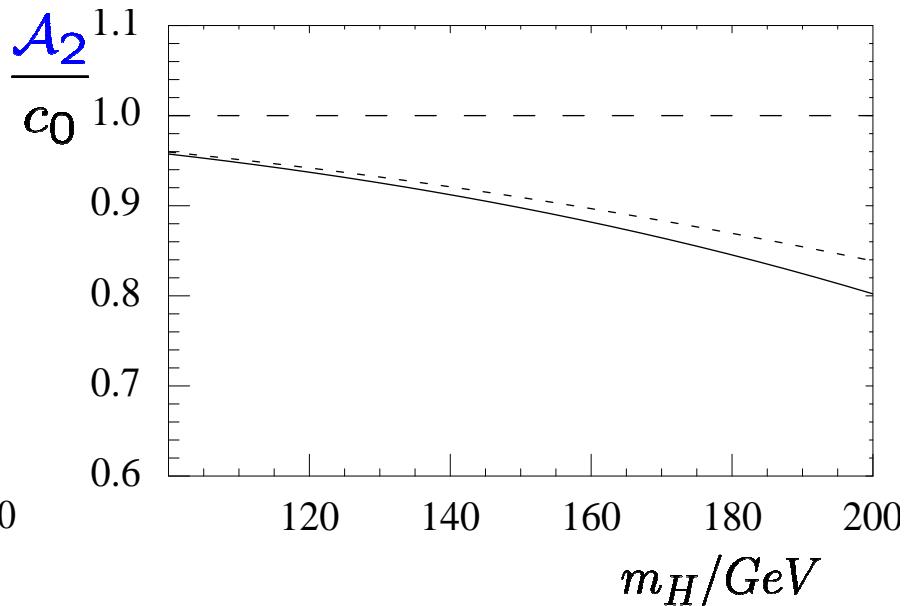
$$\gamma_5 = \frac{i}{4!} \epsilon_{\mu\nu\rho\sigma} \gamma^\mu \gamma^\nu \gamma^\rho \gamma^\sigma$$

# Amplitude in NLO: $H \rightarrow \gamma\gamma$

QCD:



SUSY-QCD:



masses/GeV:

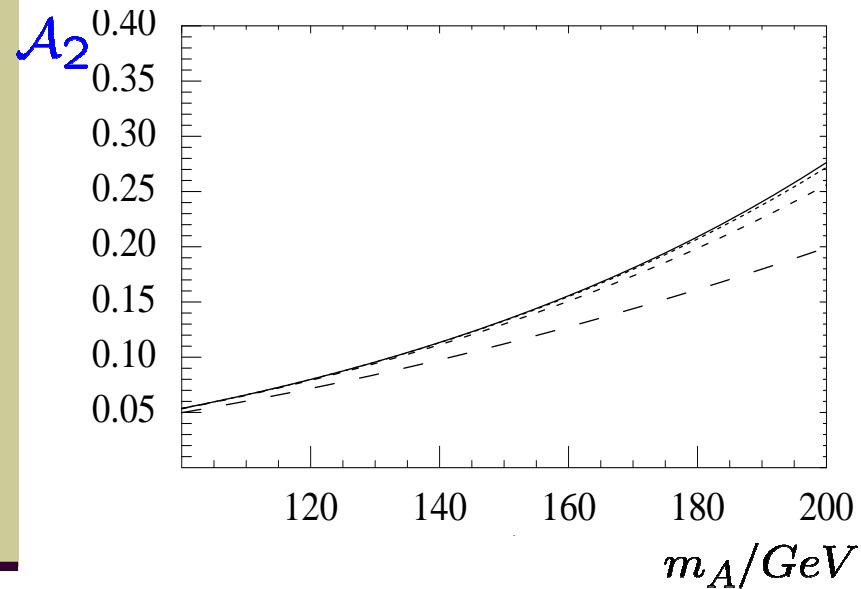
$$m_{\tilde{t}_1} = 250, m_{\tilde{t}_2} = 400, m_{\tilde{g}} = 600, \mu_{SUSY} = 150;$$

$$\tan \beta = 3, \cos \alpha = 1, \theta_t = \pi/2$$

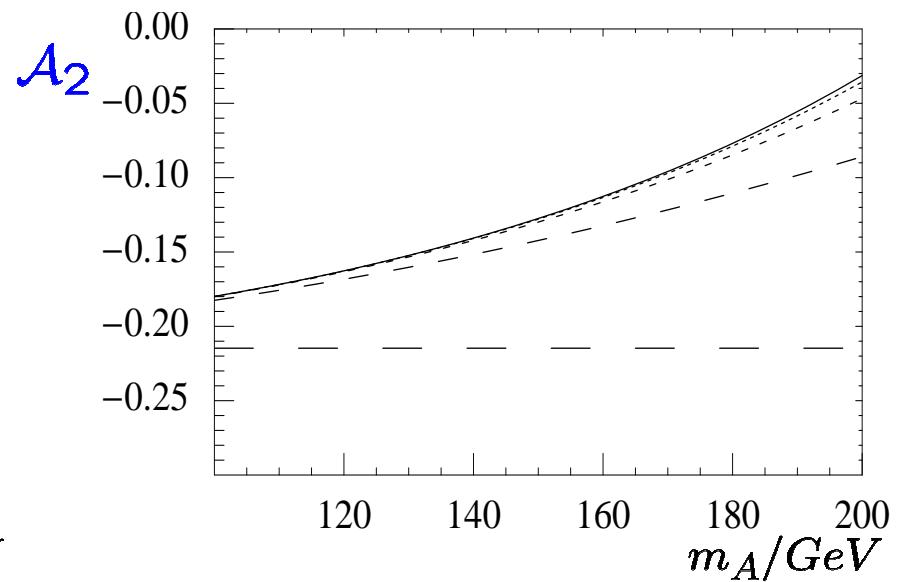
$$m_t, m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{g}}$$

# Amplitude in NLO: $A \rightarrow \gamma\gamma$

QCD:



SUSY-QCD:



$$\begin{aligned} M &= 172.5 \text{ GeV} \\ \tan \beta &= 3 \end{aligned}$$

# Conclusion

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Decay in NLO:  $H, A \rightarrow \gamma\gamma$

- Expansion in

$$c_n(m_t, m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{g}}) \left( \frac{m_{H,A}^2}{m_t^2} \right)^n$$

up to  $n = 3 \rightarrow$  good convergence

- with SUSY-particles: gluino and stops

Outlook:

→ Analytic calculation

→ Inclusion of bottom and sbottom-effects