

# Phenomenology of Little Higgs Models

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*A.B., A. Pukhov* *hep-ph/0608xxx*

**CALC 2006, July 22, 2006**

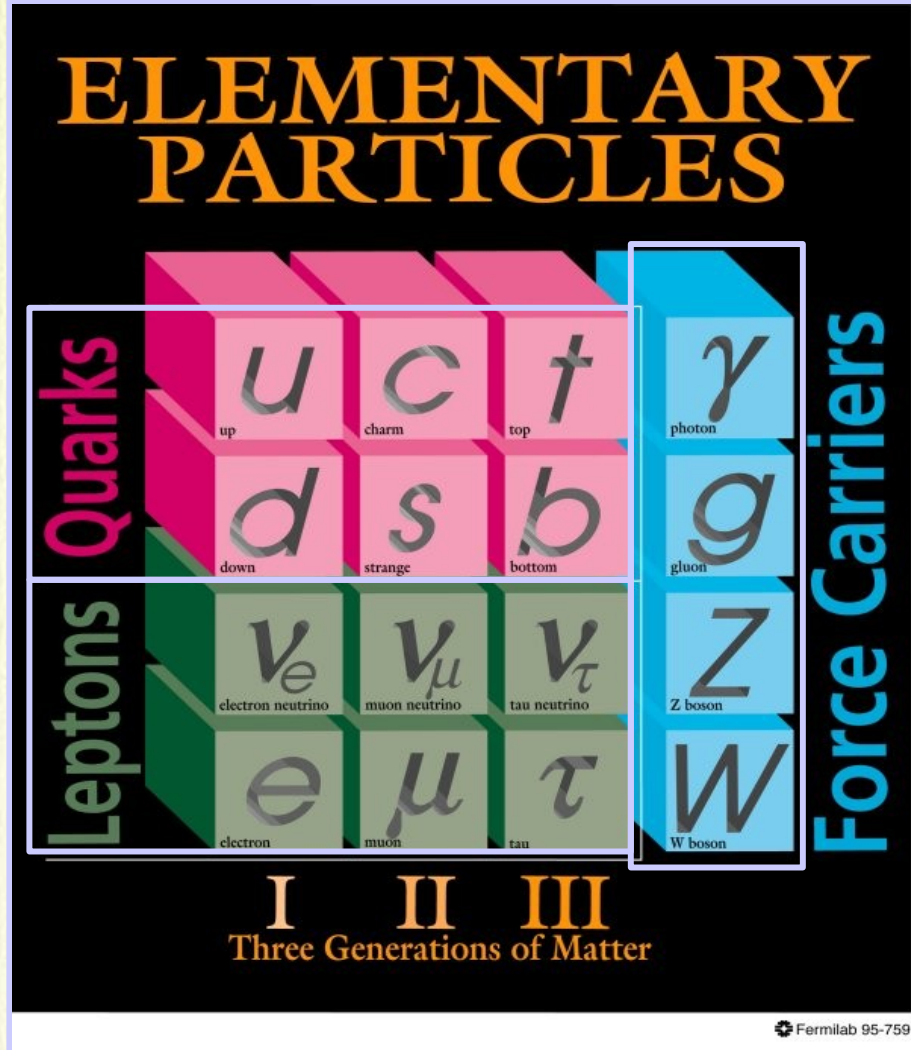
# OUTLINE

- ✦ **Motivation**
- ✦ **Little Higgs model: the idea**
- ✦ **Littlest Higgs model with T-parity (LHT)**
- ✦ **Phenomenology of LHT model**
- ✦ **Conclusions**



# The present status of the SM

- ✚ Based on  $SU(3) \times SU(2) \times U(1)$  symmetry spontaneously broken down to  $SU(3) \times U(1)$ :
- ✚ Matter: 3 generations of quarks and leptons
- ✚ One of the central role is played by Higgs field
  - ➡ *One complex Higgs doublet*
  - ➡ *3 degrees of freedom got eaten by massless  $W$  and  $Z$ , which acquire mass*
  - ➡ *1 DOF becomes the massive scalar, Higgs boson*



✚ Higgs boson is still unobserved, it is the most wanted particle!

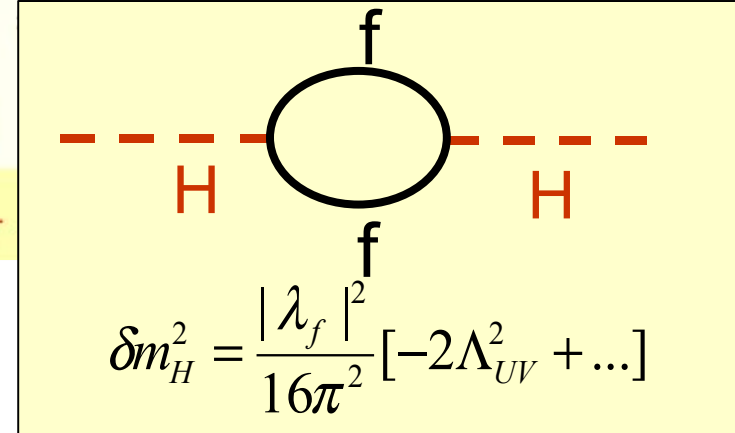
The present Higgs mass limit is 114.4 GeV from LEP2  $e^+e^-$  collider

# SM: Experimental/Theoretical problems

## ■ Theoretical problems

- naturalness and gauge hierarchy problem

$$M_H^2 = M_{H^0}^2 + \Delta M_H, \quad \text{SM: } \Delta M_H \sim \Lambda_{UV}^2$$



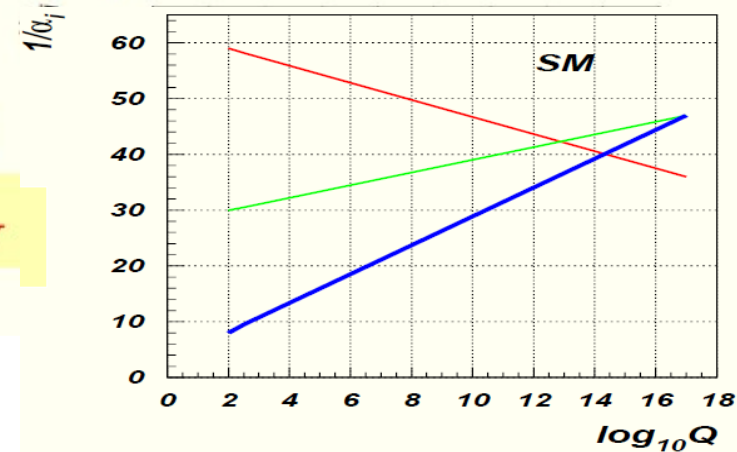
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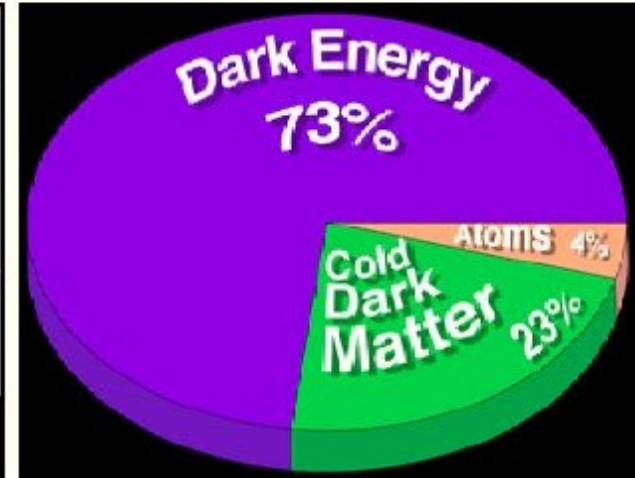
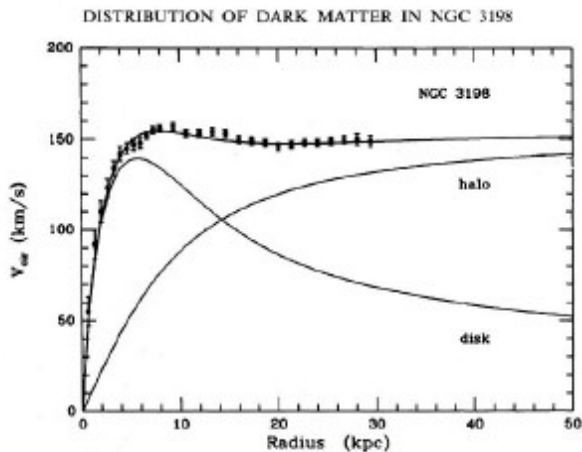
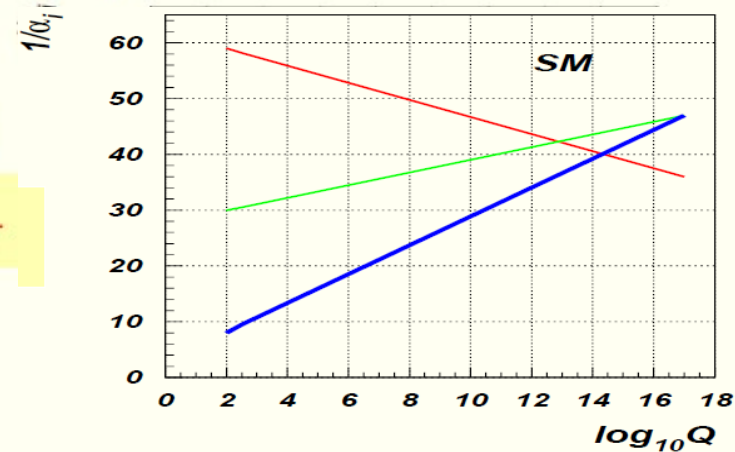
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## Experimental Problems

- Does not explain Dark Matter

(WMAP results, galactic rotation curves, gravitational lensing)



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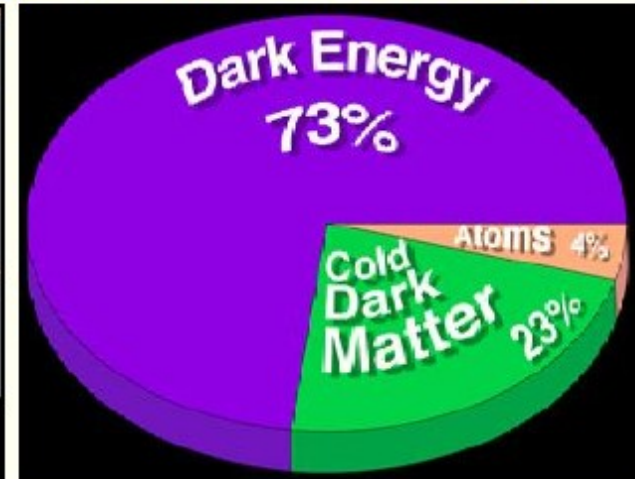
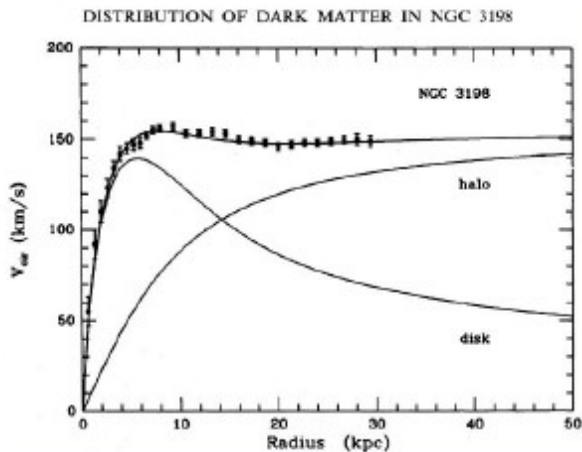
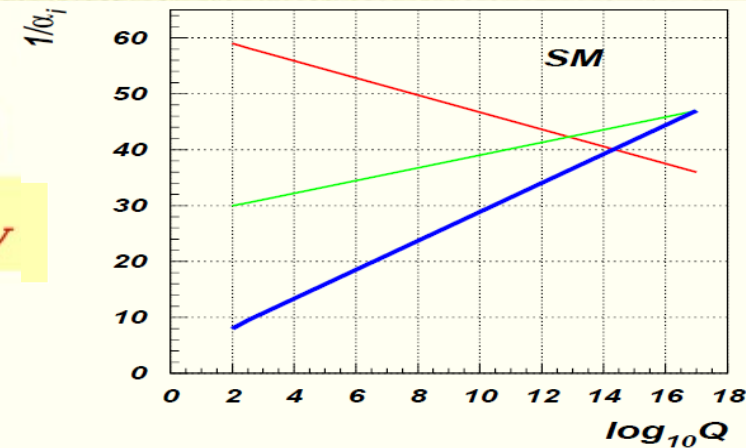
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## Experimental Problems

- Does not explain Dark Matter

(WMAP results, galactic rotation curves, gravitational lensing)



- Baryogenesis: the amount of CP violation is not enough because it predicts baryon asymmetry 10 orders of magnitude below the observed one



# Consequences of SUSY

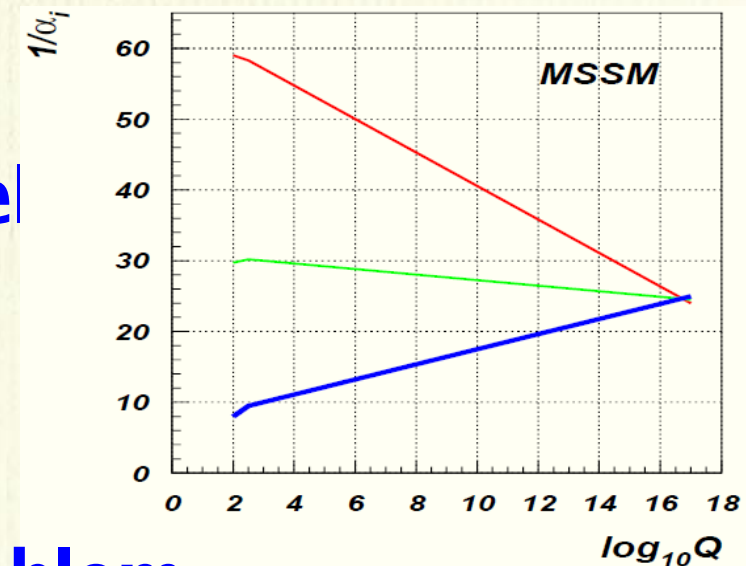
- local SUSY transformations introduce spin-2 graviton

$$spin2 \rightarrow spin3/2 \rightarrow spin1 \rightarrow spin1/2 \rightarrow spin0$$

- Provides connection to superstring models: crucial ingredient - allows to include fermions
- Solves fine-tuning problem of SM

$$M_H^2 = M_{H^0}^2 + \Delta M_H, \quad SM: \Delta M_H \sim \Lambda_{UV}^2, \quad SUSY: \Delta M_H \sim m_{soft}^2 \log(\Lambda_{UV}/m_{soft})$$

- Provides unification of gauge couplings
- EW symmetry is broken radiatively via RGE running  $H_u$  and  $H_D$
- Provides perfect DM candidate: stable LSP
- Potentially solves baryogenesis problem





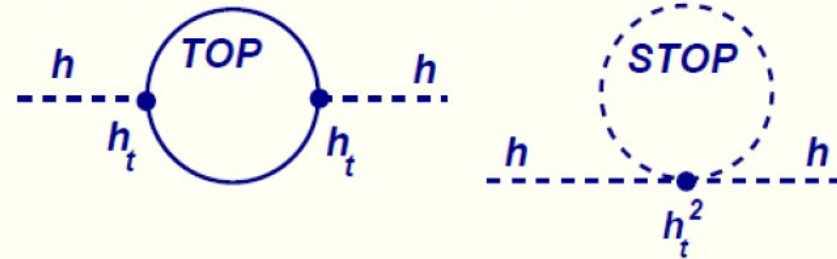
# “Little” Fine Tuning in MSSM

- Tree-level lightest Higgs boson mass is below Z-boson mass

$$M_h^2 = \frac{1}{2} \left[ m_A^2 + M_Z^2 - \sqrt{(M_A^2 + M_Z^2)^2 - 4m_A^2 M_Z^2 \cos^2 2\beta} \right] \Rightarrow M_h \simeq M_Z |\cos 2\beta| \text{ for } M_A \gg M_Z$$

Top-stop Radiative corrections to the light Higgs mass drive its mass up!

$$\delta M_h = \frac{3g^2 m_t^4}{8\pi^2 m_W^2} \left[ \ln \left( \frac{M_S^2}{m_t^2} \right) + x_t^2 \left( 1 - \frac{x_t^2}{12} \right) \right]$$



- SUSY scale  $\sim 1$  TeV and above is required to satisfy LEP2 constraints
- $\sim 1\%$  of tuning to get Z-mass right

$$m_Z^2 = \frac{|m_{H_d}^2 - m_{H_u}^2|}{\sqrt{1 - \sin^2(2\beta)}} - m_{H_u}^2 - m_{H_d}^2 - 2|\mu|^2$$

# Little Higgs model as an alternative to SUSY

Arkani-Hamed, Cohen, Georgi hep-ph/0105239

- ✦ “Little Higgs” is a pseudo-Nambu-Goldstone boson of spontaneously broken global symmetry
- ✦ This symmetry is also explicitly broken but only “collectively”: when two or more couplings in the Lagrangian are non-vanishing:  $\mathcal{L} = \mathcal{L}_0 + \lambda_1 \mathcal{L}_1 + \lambda_2 \mathcal{L}_2$
- ✦ Setting any of these couplings to zero restores the symmetry and therefore the masslessness of the “little Higgs”
- ✦ Thus, little Higgs acquires its mass at second loop

$$\delta m_H^2 \sim \left( \frac{\lambda_1^2}{16\pi^2} \right) \left( \frac{\lambda_2^2}{16\pi^2} \right) \Lambda^2 \sim O(100)\text{GeV} \text{ for } \Lambda \sim 10 \text{ TeV}$$



# Littlest Higgs: a minimal realization of Little Higgs

Arkani-Hamed, Cohen, Katz, Nelson hep-ph/0206021

**SU(5) global symmetry is spontaneously broken to SO(5) by the VEV of**

$$\Sigma_0 = \begin{pmatrix} 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{pmatrix}$$

**at the scale  $f$**

$$SU(5) \supset [SU(2) \times U(1)]_1 \times [SU(2) \times U(1)]_2$$

$$\lambda_1 \mathcal{L}_1 \qquad \lambda_2 \mathcal{L}_2$$



**VEV =  $f \sim O(1)$  TeV**

$$SO(5) \supset SU(2) \times U(1)$$

**$(N^2 - 1) [24] - N(N - 1)/2 [10] =$   
14 goldstone bosons**

$$1_0 \oplus 3_0 \oplus 2_{\pm 1/2} \oplus 3_{\pm 1}$$

$$A_H, Z_H, W_H^\pm$$

$$\Pi = \begin{pmatrix} 0 & \frac{H}{\sqrt{2}} & \Phi \\ \frac{H^\dagger}{\sqrt{2}} & 0 & \frac{H^T}{\sqrt{2}} \\ \Phi^\dagger & \frac{H^*}{\sqrt{2}} & 0 \end{pmatrix}$$

**Goldstone boson matrix parameterization in non-linear sigma model**

$$\Sigma = \exp(i\Pi/f)\Sigma_0$$

**Higgs is exact NG boson under either global SU(3)**

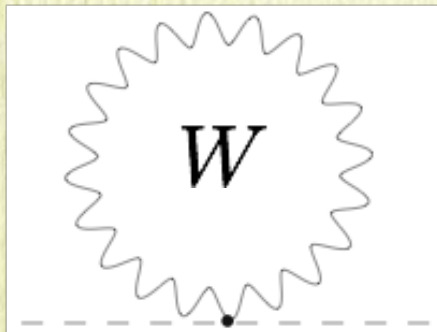
# Collective Symmetry Breaking

$[SU(2) \times U(1)]_1 \times [SU(2) \times U(1)]_2$  *are embedded in global SU(5)*

$$Q_{SU(2)_1}^a = \begin{pmatrix} \sigma^a/2 & 0 & 0 \\ 0 & \boxed{0 & 0} \\ 0 & \boxed{0 & 0} \end{pmatrix} \quad Y_1 = \frac{1}{10} \begin{pmatrix} 3 & & & & \\ & 3 & & & \\ & & \boxed{-2} & & \\ & & & -2 & \\ & & & & -2 \end{pmatrix} \quad \text{preserves } SU(3)$$

$$Q_{SU(2)_2}^a = \begin{pmatrix} \boxed{0 & 0} & 0 \\ \boxed{0 & 0} & 0 \\ 0 & 0 & -\sigma^{a*}/2 \end{pmatrix} \quad Y_2 = \frac{1}{10} \begin{pmatrix} \boxed{2} & & & & \\ & 2 & & & \\ & & \boxed{2} & & \\ & & & -3 & \\ & & & & -3 \end{pmatrix} \quad \text{preserves } SU(3)$$

*Either SU(3) is enough to keep Higgs massless. Sum of all gauge interactions break both SU(3)s and generate the Higgs mass.*



$$\frac{g^2}{2}$$



$$-\frac{g^2}{2}$$

$\Lambda^2$  corrections are canceled.



# Littlest Higgs: scalar kinetic term

$$\mathcal{L}_\Sigma = \frac{1}{2} \frac{f^2}{4} \text{Tr} |\mathcal{D}_\mu \Sigma|^2 \quad \text{with covariant derivative given by}$$

$$\mathcal{D}_\mu \Sigma = \partial_\mu \Sigma - i \sum_{j=1}^2 \left( g_j (W_j \Sigma + \Sigma W_j^T) + g'_j (B_j \Sigma + \Sigma B_j^T) \right)$$

where  $\Sigma$  expanded around its vacuum expectation value

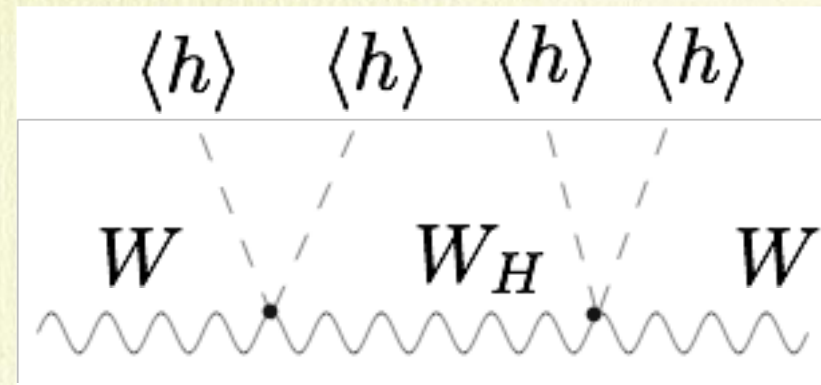
$$\Sigma = \Sigma_0 + \frac{2i}{f} \begin{pmatrix} \phi^\dagger & \frac{h^\dagger}{\sqrt{2}} & \mathbf{0}_{2 \times 2} \\ \frac{h^*}{\sqrt{2}} & 0 & \frac{h}{\sqrt{2}} \\ \mathbf{0}_{2 \times 2} & \frac{h^T}{\sqrt{2}} & \phi \end{pmatrix} + \mathcal{O}\left(\frac{1}{f^2}\right),$$

**Lagrangian contains non-renormalizable interactions:  
can be only low energy effective description of physics.**

**The loop contribution becomes as important as tree-level diagram  
at the scale  $\Lambda \lesssim 4\pi f$  : theory becomes strongly coupled**

# Little Higgs Model with T-parity (LHT)

- Large tree-level corrections e.g. due to the exchange of additional heavy gauge bosons and non-vanishing VEV of triplet higgs:  $f > 5 \text{ TeV}$ , fine-tuning again!



- T-parity (Cheng, Low 2003),  $Z_2$  symmetry forbids mixing with SM

$$SU(2)_1 \times U(1)_1 \leftrightarrow SU(2)_2 \times U(1)_2$$

$$\begin{aligned} \text{SM particles} &\rightarrow + \text{SM particles} \\ (W_H, Z_H, A_H, \Phi, Q) &\rightarrow -(W_H, Z_H, A_H, \Phi, Q) \end{aligned}$$

$$g_1 = g_2 = \sqrt{2}g \text{ and } g'_1 = g'_2 = \sqrt{2}g'$$

- ➡ No tree-level to EW observables
- ➡ The lightest T-odd particle is a good DM candidate
- ➡ New scale  $f$  can be lower than 1 TeV

interesting phenomenology! (Hubisz et al., 2004)



# LHT Model

*Hsin-Chia Cheng, Ian Low,*

*Jay Hubisz, Patrick Meade,*

*Andrew Noble, Maxim Perelstein,*

*Claudio O. Dib, Rogerio Rosenfeld,*

*Alfonso Zerwekh, Seung J. Lee, Gil Paz,*

*Chuan-Ren Chen, Kazuhiro Tobe,*

*C.-P. Yuan, Andreas Birkedal, ...*

# LHT: new particles

## Gauge sector

$$A_H, m \sim g' f / \sqrt{5}$$

*DM candidate!*

$$Z_H, W_H^\pm, m \sim g f$$

## Higgs sector

$$\Phi : \phi^{++}, \phi^+, \phi^0, \phi^P; m \sim \sqrt{2} m_h f / v$$

**$SU(2)_L$  doublets**

## Fermion sector

$$t'_+, m \sim \sqrt{\lambda_1^2 + \lambda_2^2} f$$

**singlet, the only T-even**

$$t'_-, m \sim \lambda_2 f$$

**singlet**

$$Q_L^{(-)}, L_L^{(-)}, m \sim \sqrt{2} \kappa f \quad \mathbf{SU(2)_L doublets}$$

**Have not been included in the previous phenomenological studies! Do not decouple.**



# LHT Model: Yukawa interactions

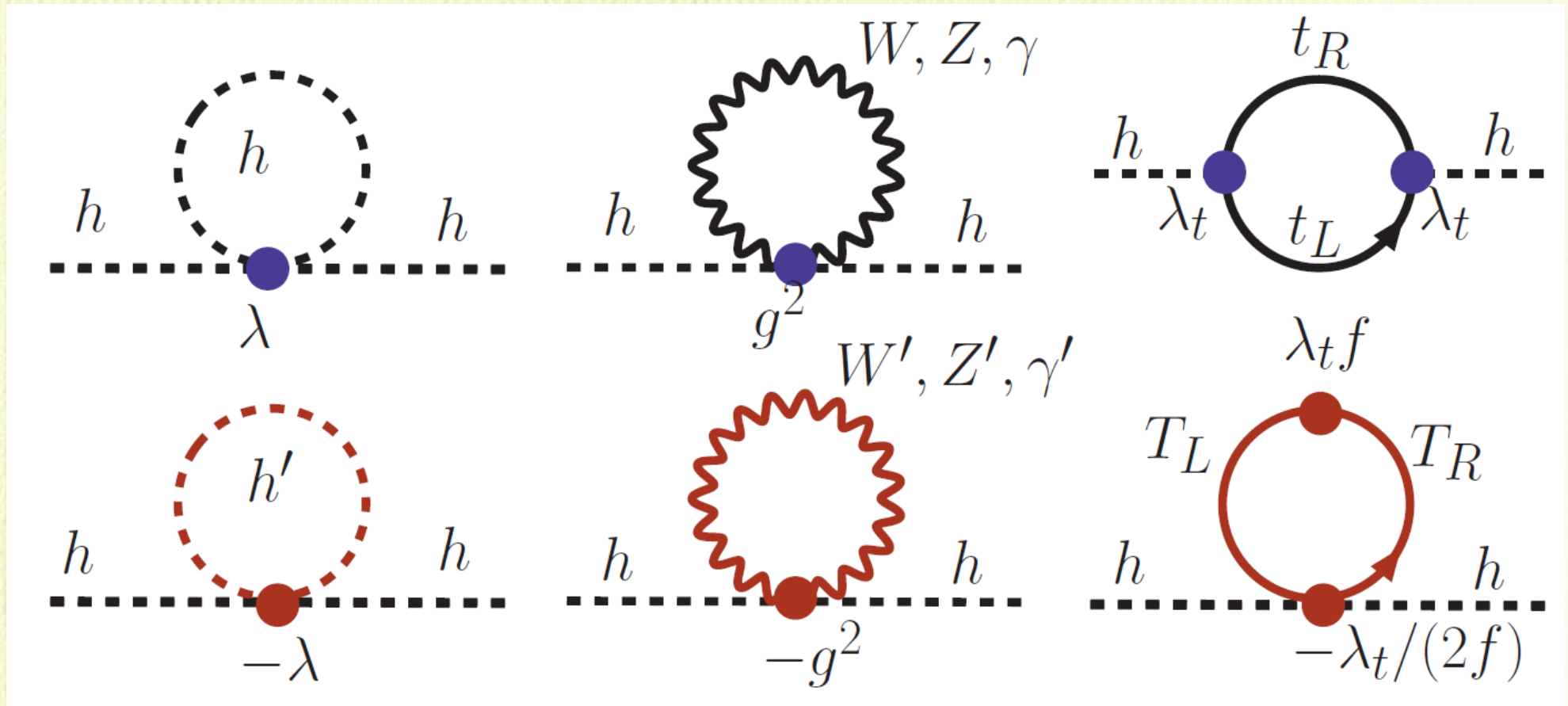
$$-\frac{\lambda_1}{2\sqrt{2}} f \epsilon_{ijk} \epsilon_{xy} \left[ (\bar{Q}_1)_i \Sigma_{jx} \Sigma_{ky} - (\bar{Q}_2 \Sigma_0)_i \tilde{\Sigma}_{jx} \tilde{\Sigma}_{ky} \right] u_{R+} \\ - \lambda_2 f (\bar{U}_{L1} U_{R1} + \bar{U}_{L2} U_{R2}) + \text{h.c.},$$

with  $Q_1 = (q_1, U_{L1}, 0_2)^T$  and  $Q_2 = (0_2, U_{L2}, q_2)^T$   
 giving  $t, t_+, t_-$  with  $\sin \alpha = \lambda_1 / \sqrt{\lambda_1^2 + \lambda_2^2}$   
 $M_t \simeq (\lambda_2 \sin \alpha) v, \quad M_{t-} \simeq \lambda_2 f, \quad M_{t+} \simeq (\lambda_2 / \cos \alpha) f$

$$-\kappa f (\bar{\Psi}_2 \xi \Psi_c + \bar{\Psi}_1 \Sigma_0 \Omega \xi^\dagger \Omega \Psi_c) + \text{h.c.}$$

fermion  $SU(2)$  doublets  $q_1$  and  $q_2$ :  
 $\Psi_1 = (q_1, 0, 0_2)^T$  and  $\Psi_2 = (0_2, 0, q_2)^T$   
 giving  $U_-, D_-$ , with  $M_{Q-} = \sqrt{2} \kappa f$

# Cancellation of quadratic divergences



**New heavy particles *bosons, top-quarks, scalars* cancel the respective SM one-loop quadratic divergences**



# LHT: model parameters and mass spectrum

$$A_H, m \sim g' f / \sqrt{5}$$

$$Z_H, W_H^\pm, m \sim g f$$

$$\phi^{++}, \phi^+, \phi^0, \phi^P;$$

$$m \sim \sqrt{2} m_h f / v$$

$$\sin \alpha = \lambda_1 / \sqrt{\lambda_1^2 + \lambda_2^2}$$

$$M_{t_-} \simeq (\lambda_2 \sin \alpha) v,$$

$$M_{t_-} \simeq \lambda_2 f,$$

$$M_{t_+} \simeq (\lambda_2 / \cos \alpha) f$$

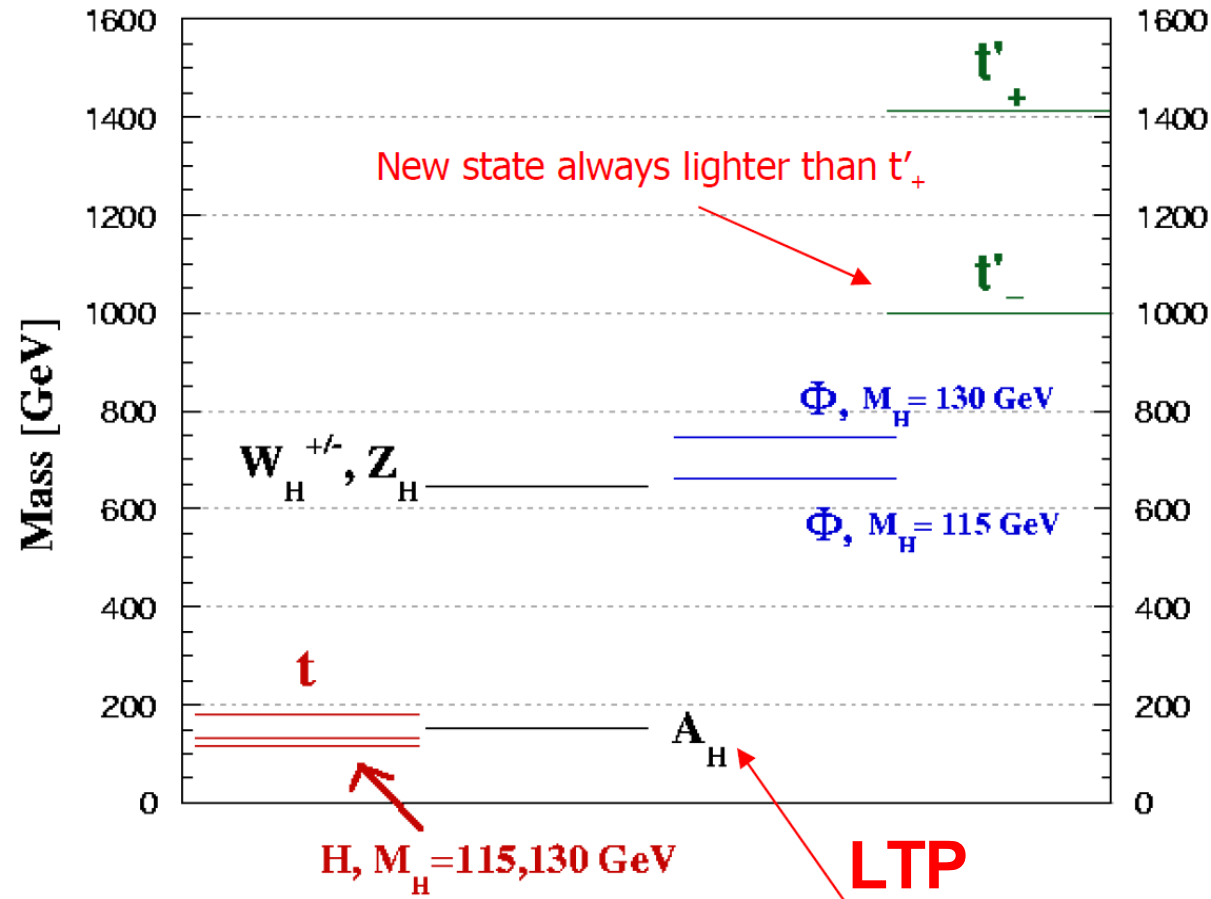
$$Q_L^{(-)}, L_L^{(-)},$$

$$m \sim \sqrt{2} \kappa f$$

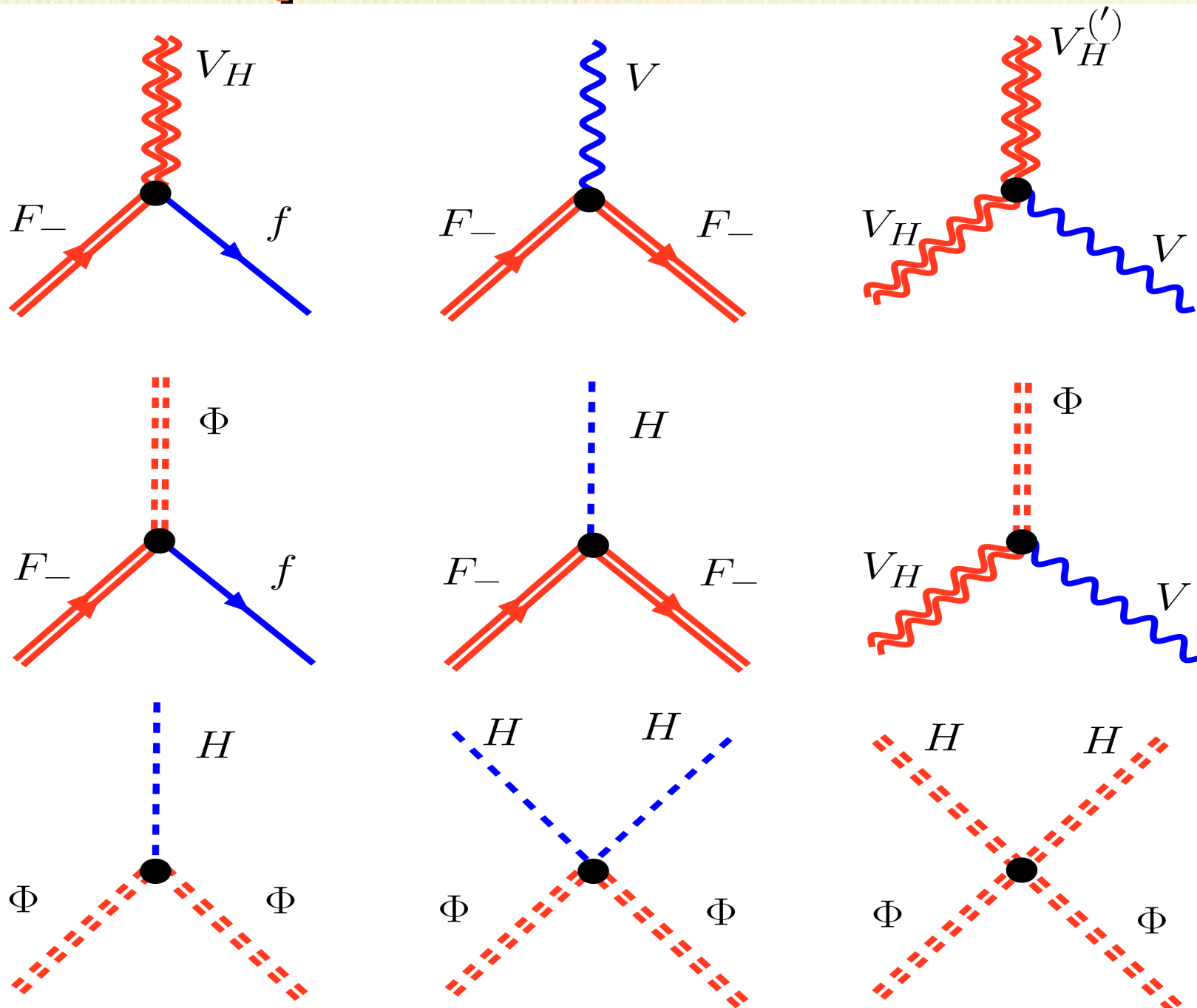
Model parameters:

$f, M_h, \sin \alpha, \kappa$

Example Spectrum of the Littlest Higgs with T-parity



# LHT: particle interactions





# Phenomenology of LHT model

## ✦ Model implementation

**Lanhep** → **CalcHEP**

**Lanhep (A.Semenov)** is the package for automatic generation of Feynman rules (model) for **CompHEP/CalcHEP**

**lowers down a lot the possibility of human mistake**

✦ **Previously, the essential part of the model**

**has been implemented by J. Hubisz and P. Meade in hep-ph/0411264**

✦ **Our study aims**

➔ ***to implement the complete model***

➔ ***to check the previous studies***

➔ ***to systematise all possible phenomenology***

➔ ***to apply CalcHEP-PYTHIA for multibody final states***

➔ ***To calculate DM relic density within the complete model using MicroMEGAs 2.0 (A. Pukhov et al)***

# LHT implementation using LanHEP(1)

CalcHEP/symb

**Model:** Littlest Higgs-T

**Abstract**

CalcHEP package is created for calculation of decay and high energy collision processes of elementary particles in the lowest order (tree) approximation. The main idea put into the CalcHEP was to make available passing from the lagrangian to the final distributions effectively with the high level of automatization.

Use F2 key to get information about interface facilities and F1 - as online help.

**\* Enter Process**  
Force Unit.Gauge OFF  
Edit model  
Delete model



# LHT implementation using LanHEP(2)

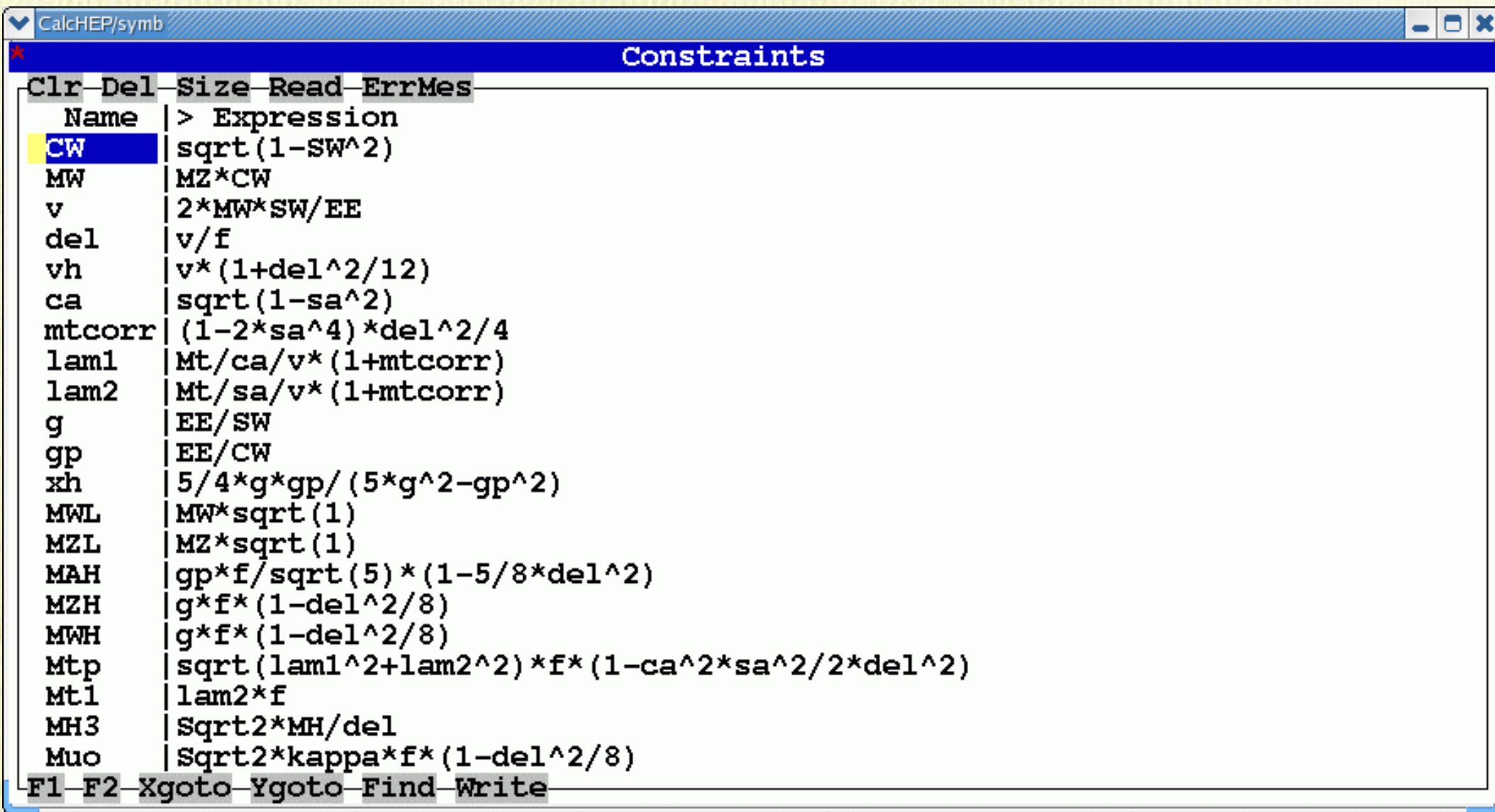
CalcHEP/symb

**Variables**

Clr	Del	Size	Read	ErrMes	
Name	Value				> Comment <
EE	0.307885				Electromagnetic coupling constant ( $\leftrightarrow 1/128$ )
GG	1.21772				Strong coupling constant (Z point) (PDG-94)
SW	0.4713				sin of the Weinberg angle (PDG-94, "on-shell")
s12	0.221				Parameter of C-K-M matrix (PDG-94)
s23	0.04				Parameter of C-K-M matrix (PDG-94)
s13	0.0035				Parameter of C-K-M matrix (PDG-94)
MZ	91.1876				Z-boson mass
f	1000				
sa	0.707107				
zero0	0				
Mt	175				
MH	120				
kappa	1				
Mb	4.7				
Mc	1.3				
Ms	0.2				
wW	2.502				width of W boson
wWh	10				width of W heavy
wZ	2.502				width of Z boson
wZh	10				width of Z heavy
Mm	0.1057				mass of muon

F1 F2 Xgoto Ygoto Find Write

# LHT implementation using LanHEP(3)



The screenshot shows a window titled "Constraints" with a list of variables and their corresponding mathematical expressions. The window has a menu bar with options: Clr, Del, Size, Read, ErrMes, F1, F2, Xgoto, Ygoto, Find, Write. The list of variables and expressions is as follows:

Clr	Del	Size	Read	ErrMes	Name	Expression
					CW	$\sqrt{1-SW^2}$
					MW	$MZ * CW$
					v	$2 * MW * SW / EE$
					del	$v / f$
					vh	$v * (1 + del^2 / 12)$
					ca	$\sqrt{1 - sa^2}$
					mtcorr	$(1 - 2 * sa^4) * del^2 / 4$
					lam1	$Mt / ca / v * (1 + mtcorr)$
					lam2	$Mt / sa / v * (1 + mtcorr)$
					g	$EE / SW$
					gp	$EE / CW$
					xh	$5 / 4 * g * gp / (5 * g^2 - gp^2)$
					MWL	$MW * \sqrt{1}$
					MZL	$MZ * \sqrt{1}$
					MAH	$gp * f / \sqrt{5} * (1 - 5 / 8 * del^2)$
					MZH	$g * f * (1 - del^2 / 8)$
					MWH	$g * f * (1 - del^2 / 8)$
					Mtp	$\sqrt{lam1^2 + lam2^2} * f * (1 - ca^2 * sa^2 / 2 * del^2)$
					Mt1	$lam2 * f$
					MH3	$Sqrt2 * MH / del$
					Muo	$Sqrt2 * kappa * f * (1 - del^2 / 8)$



# LHT implementation using LanHEP(4)

CalcHEP/symb

32

Particles

Clr	Del	Size	Read	ErrMes	number	2*spin	mass	width	color	aux	>	LaTeX (A)
p++	higgs	~++	~--		0	0	MH3	0	1		(++)	
neutrino		n1	N1		0	1	0	0	1		n1	
electron		e1	E1		0	1	0	0	1		e1	
mu-neutrino		n2	N2		0	1	0	0	1		n2	
muon		e2	E2		0	1	Mm	0	1		e2	
tau-neutrino		n3	N3		0	1	0	0	1		n3	
tau-lepton		e3	E3		0	1	Ml	0	1		e3	
u-quark		u	U		2	1	0	0	3		u	
d-quark		d	D		1	1	0	0	3		d	
c-quark		c	C		4	1	Mc	0	3		c	
s-quark		s	S		3	1	Ms	0	3		s	
t-quark		t	T		6	1	Mt	wtop	3		t	
b-quark		b	B		5	1	Mb	0	3		b	
tp-quark		tp	Tp		0	1	Mtp	wtp	3		tp	
u-todd		~u	~U		0	1	Muo	w tq	3		(u)	
d-todd		~d	~D		0	1	Mdo	w tq	3		(d)	
c-todd		~c	~C		0	1	Muo	w tq	3		(c)	
s-todd		~s	~S		0	1	Mdo	w tq	3		(s)	
b-todd		~b	~B		0	1	Mdo	w tq	3		(b)	
T2-todd		~t2	~T2		2000006	1	Mt2	w t2	3		(t2)	
<b>T1-todd</b>		<b>~t1</b>	<b>~T1</b>		<b>1000006</b>	<b>1</b>	<b>Mt1</b>	<b>w t1</b>	<b>3</b>		<b>(t1)</b>	

F1 F2 Xgoto Ygoto Find Write

# LHT implementation using LanHEP(5)

```

CalcHEP/symb
Lagrangian 51
Clr-Del-Size-Read-ErrMes
P1 | P2 | P3 | P4 | > Factor | <|> dLagrangian/ dA(p1) dA(p2) dA(p3)
D | u | W- | | EE*Sqrt2/(4*SW) | G(m3)*(1-G5)
D | ~d | ~A | | EE/(20*CW*SW) | -SW*G(m3)*(1-G5)+5*del^2*CW*xh*(1-G5)*G(m3)
D | ~d | ~Z | | EE/(20*CW*SW) | 5*CW*G(m3)*(1-G5)+del^2*SW*xh*(1-G5)*G(m3)
D | ~u | ~W- | | -EE*Sqrt2/(4*SW) | G(m3)*(1-G5)
E1 | e1 | A | | -EE | G(m3)
E1 | e1 | Z | | -EE/(4*CW*SW) | (1-2*SW^2)*G(m3)*(1-G5)-2*SW^2*G(m3)*(1+G5)
E1 | n1 | W- | | EE*Sqrt2/(4*SW) | G(m3)*(1-G5)
E2 | e2 | A | | -EE | G(m3)
E2 | e2 | H | | -Mm/v | 1
E2 | e2 | Z | | -EE/(4*CW*SW) | (1-2*SW^2)*G(m3)*(1-G5)-2*SW^2*G(m3)*(1+G5)
E2 | n2 | W- | | EE*Sqrt2/(4*SW) | G(m3)*(1-G5)
E3 | e3 | A | | -EE | G(m3)
E3 | e3 | H | | -Ml/v | 1
E3 | e3 | Z | | -EE/(4*CW*SW) | (1-2*SW^2)*G(m3)*(1-G5)-2*SW^2*G(m3)*(1+G5)
E3 | n3 | W- | | EE*Sqrt2/(4*SW) | G(m3)*(1-G5)
G | G | G | | GG | m2.p3*m1.m3-m1.p3*m2.m3+m3.p1*m1.m2-m2.p1*m1.m3-m3
G.C | G.c | G | | GG | m3.p2
H | H | H | | 4*lamh4*vh | 1
H | W+ | W- | | EE^2*vh/(2*SW^2) | m2.m3
H | Z | Z | | EE^2*vh/(2*CW^2*SW^2) | m2.m3
H | ~A | ~A | | -EE^2*vh/(2*CW^2*SW^2) | SW^2*m2.m3+(zero0*CW^2*xh^2*m2.m3+2*del^2*SW*CW*xh
F1 F2 Xgoto Ygoto Find Write

```



# LHT implementation using LanHEP(6)

```
CalcHEP/symb
Model: Littlest Higgs-T

List of particles (antiparticles)

W+(W- )- W boson
Z(Z )- Z boson
G(G )- gluon
~PS - pp higgs
n1(N1 )- neutrino
e2(E2 )- muon
u(U )- u-quark
s(S )- s-quark
tp(Tp )- tp-quark
~c(~C )- c-todd
~t2(~T2)- T2-todd

~W+(~W-)- W heavy
~A(~A )- photon heavy
H(H )- H higgs
~P+(~P-)- p+ higgs
e1(E1 )- electron
n3(N3 )- tau-neutrino
d(D )- d-quark
t(T )- t-quark
~u(~U )- u-todd
~s(~S )- s-todd
~t1(~T1)- T1-todd

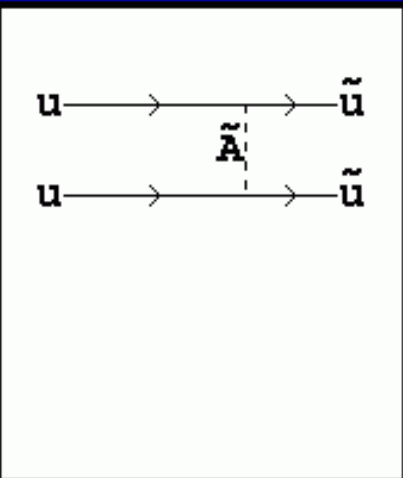
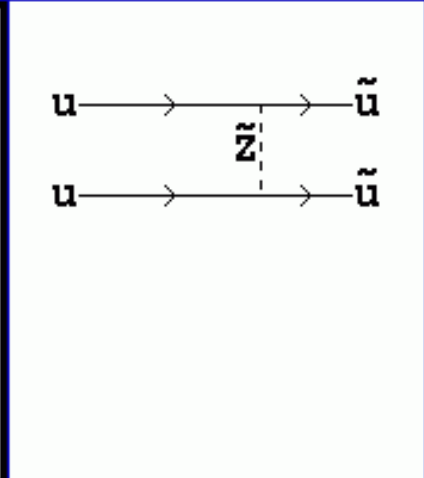
A(A )- photon
~Z(~Z )- Z heavy
~P0 - P0 higgs
~++(~--)- p++ higgs
n2(N2 )- mu-neutrino
e3(E3 )- tau-lepton
c(C )- c-quark
b(B )- b-quark
~d(~D )- d-todd
~b(~B )- b-todd

Enter process: u,u ->~u,~u
```

# LHT implementation using LanHEP(7)

CalcHEP/symb

Delete, On/off, Restore, Latex 1/2

F1-Help, F2-Man, PgUp, PgDn, Home, End, #, Esc



# LHT implementation using LanHEP(8)

CalcHEP/num

(sub)Process: u, u -> ~u, ~u  
Monte Carlo session: 1(continue)

#IT	Cross section [pb]	Error %	nCall	chi**2
1	5.2297E-02	2.45E+00	9826	
2	5.2174E-02	3.16E-01	9826	
3	5.2195E-02	2.26E-01	9826	
4	5.1794E-02	2.34E-01	9826	
5	5.1761E-02	2.37E-01	9826	
< >	5.1961E-02	1.23E-01	49130	3

XX

Constraints

Display dependence

\* Sqrt2= 1.4142

CW= 0.88197

MW= 80.425

v= 246.22

del= 0.24622

g= 0.65327

gp= 0.34909

xh= 0.14168

MAH= 150.2

MZH= 648.32

Muo= 1403.5

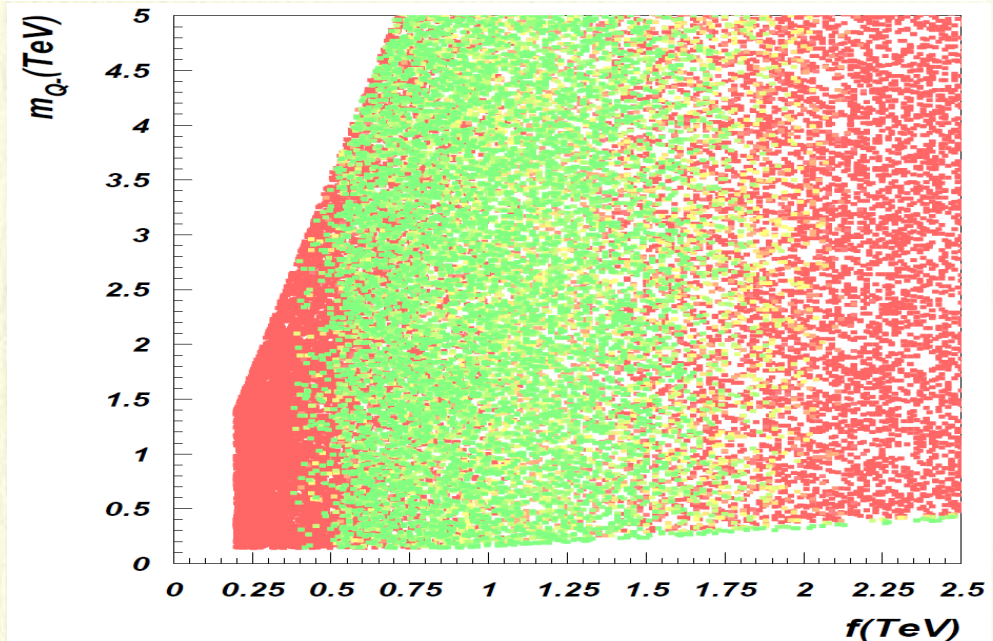
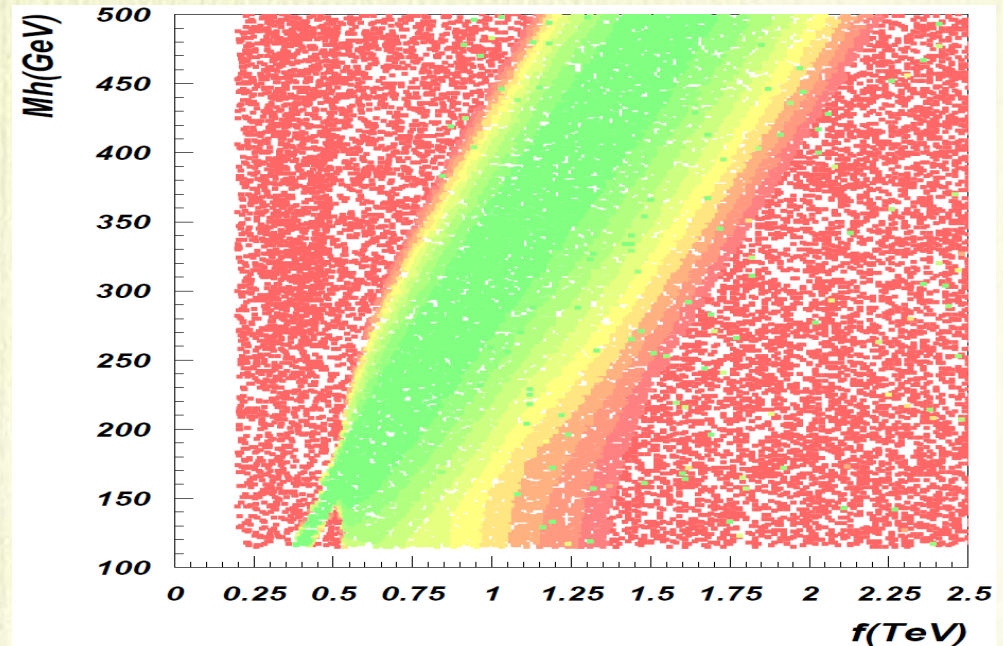
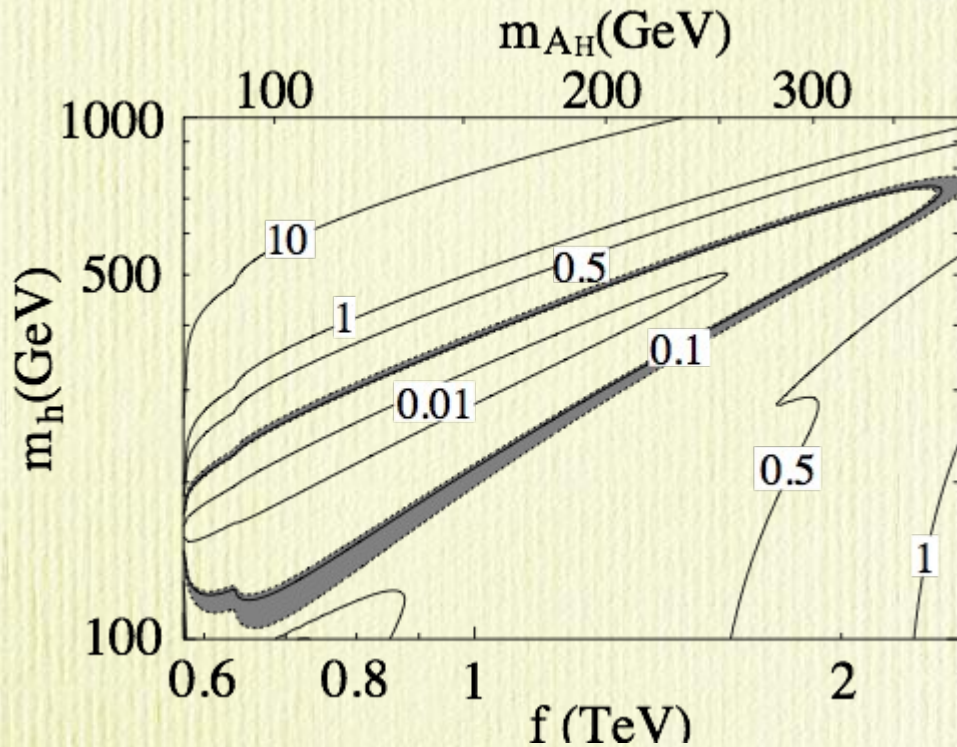
F1-Help F2-Man F6-Results F9-Ref F10-Quit

# LHT: relic density abundance results

$$0.094 < \Omega h^2 < 0.129$$

A.B, A. Pukhov (preliminary)

Asano, Matsumoto, Okada,  
Okada, hep-ph/0602157



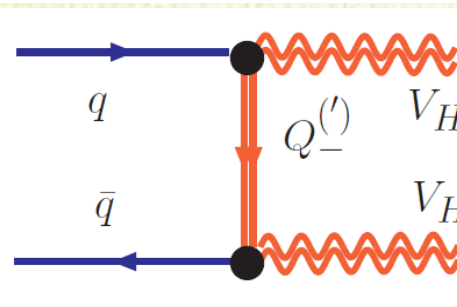
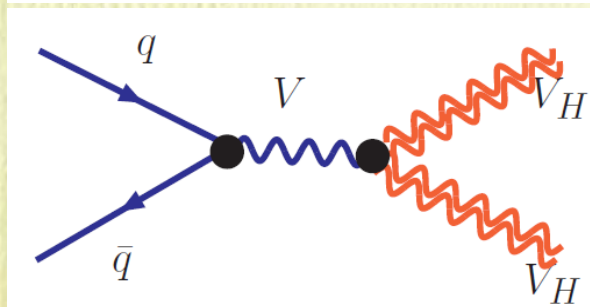
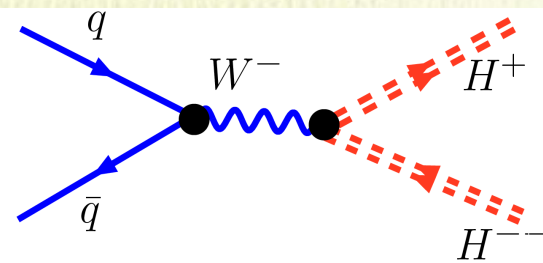
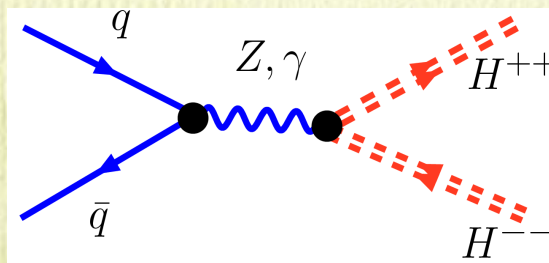
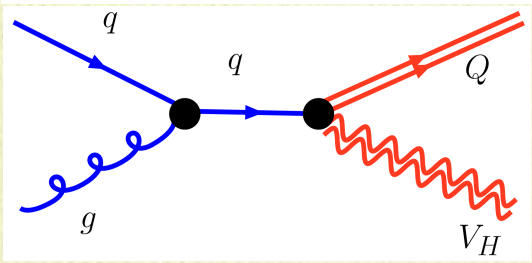
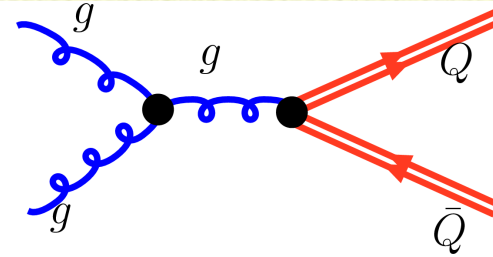
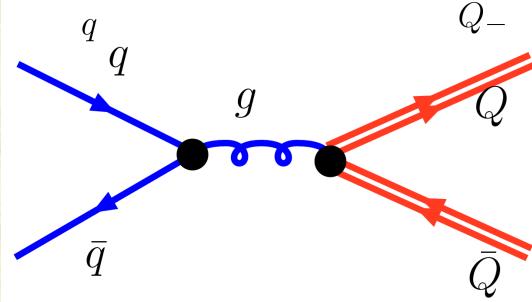
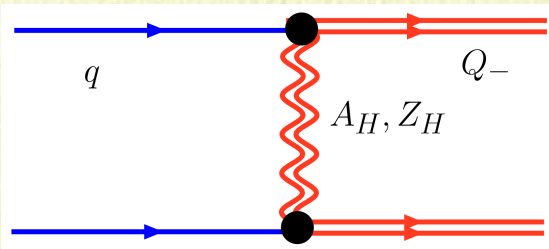
Model parameters:

$$f, M_h, \sin \alpha, \kappa$$



# LHT: processes

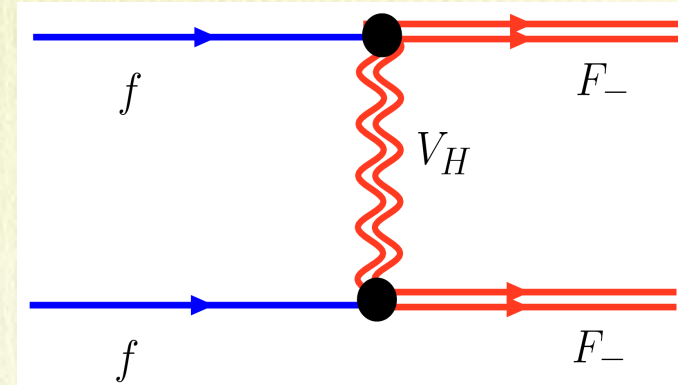
*like-sign leptons!*



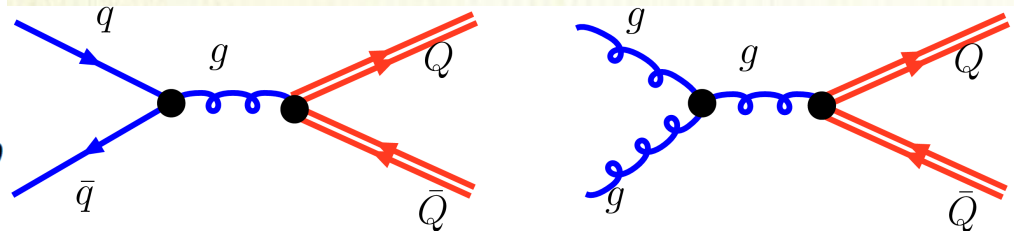
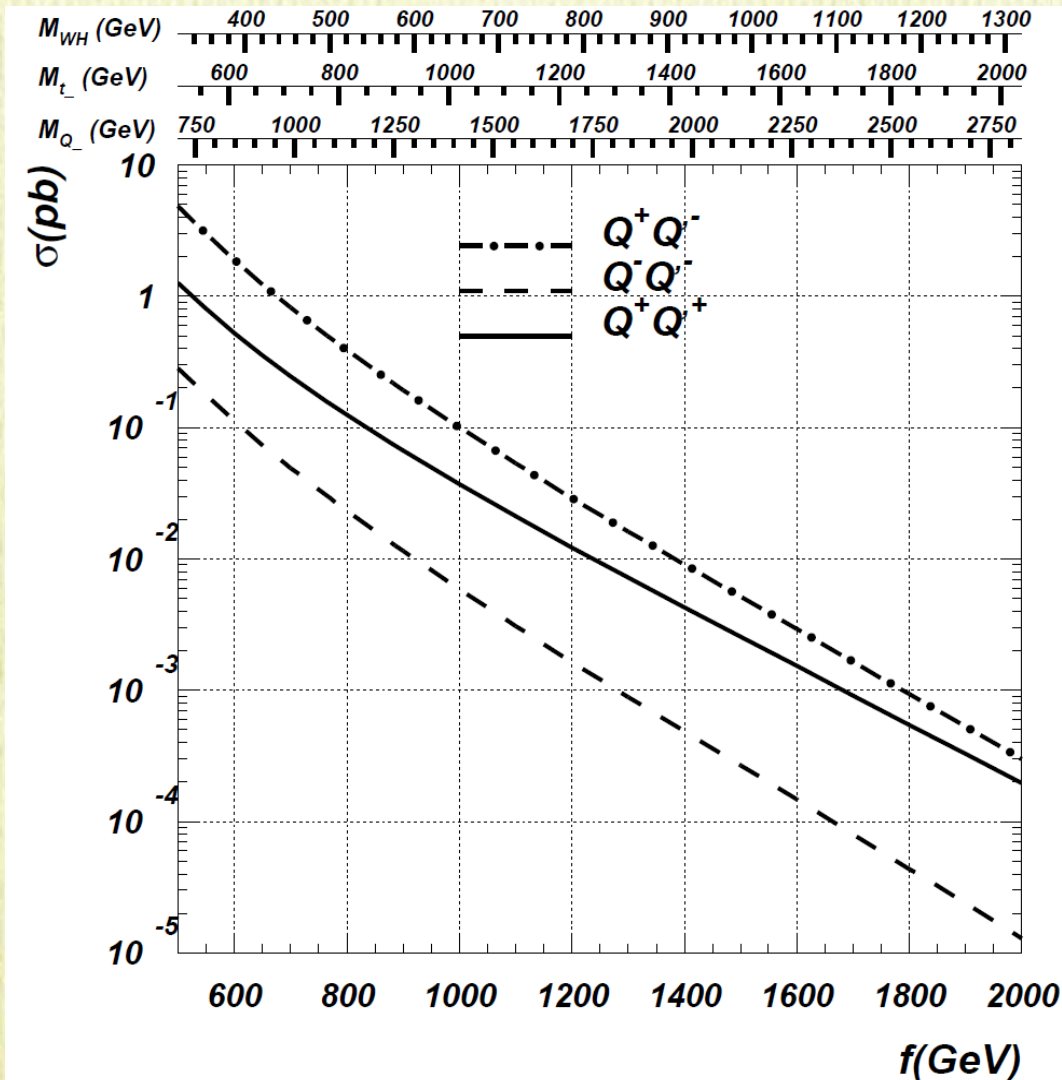


# Heavy quarks production rates and signatures

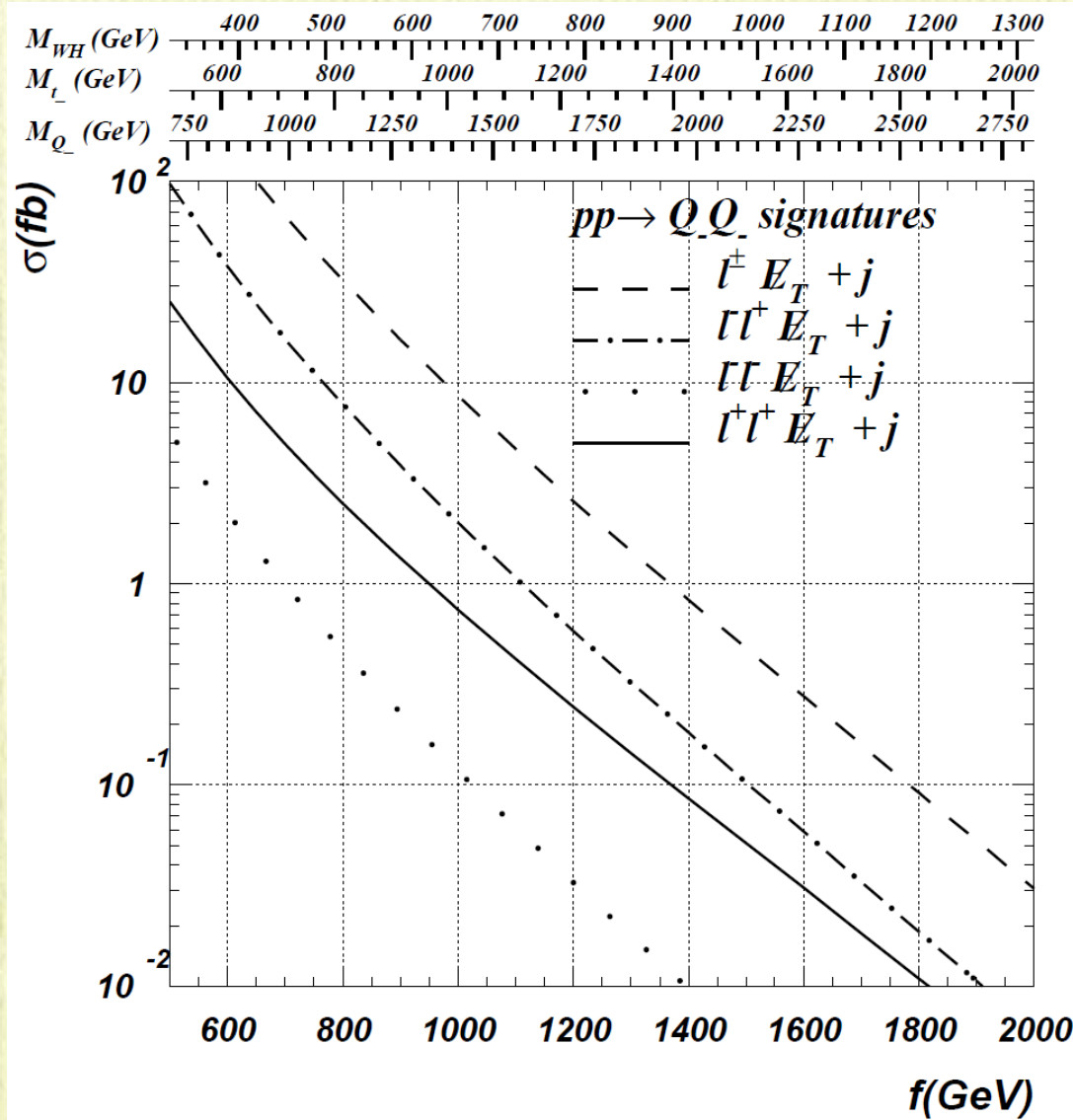
$$\sin \alpha = 1/\sqrt{2} \quad (\lambda_1 = \lambda_2), \kappa = 1$$



***EW production due to the initial double valence quarks leads to like sign lepton signature (LSL), it is comparable to strong production and becomes even more important for heavier masses due to parton luminosity behavior!***



# Heavy quarks production rates and signatures



$$\lambda_1 = \lambda_2 = 1$$

$$f = 1 \text{ TeV}, \quad \kappa = 1$$

$$Br(Q \rightarrow W_H q') = 0.62$$

$$Br(W_H \rightarrow W A_H) = 1$$

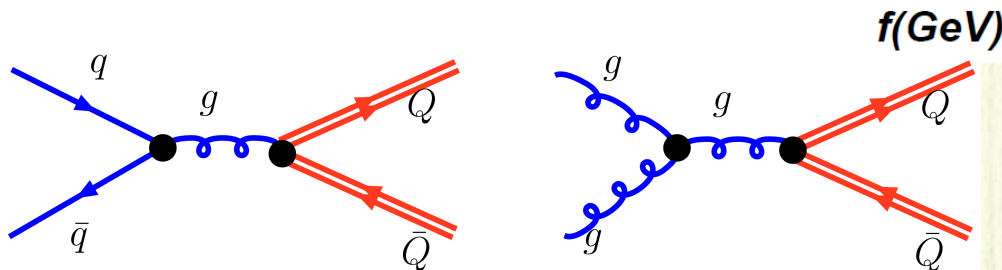
## Like-sign lepton signature (LSL)

$$qq \rightarrow QQ$$

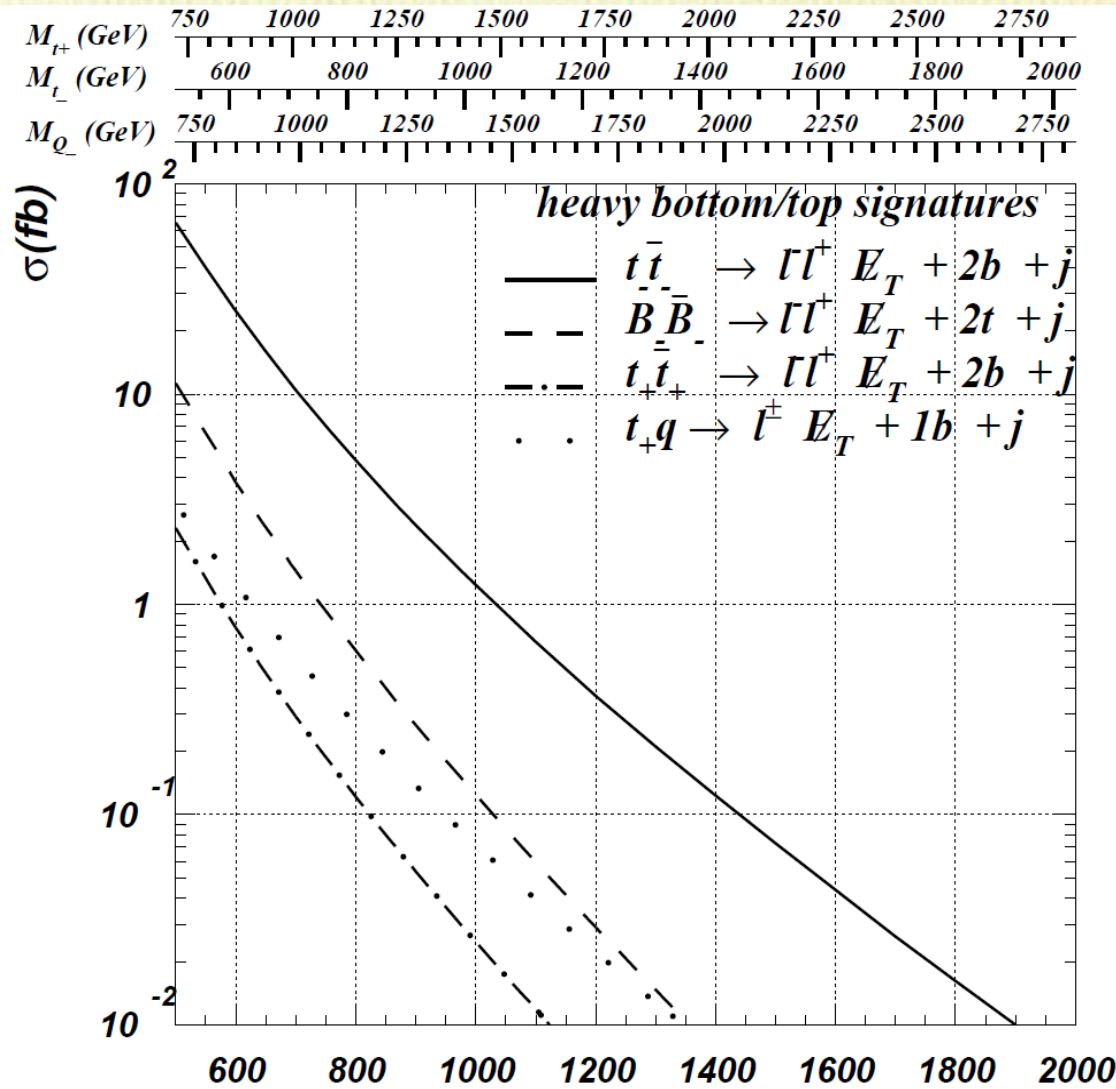
$$(Q \rightarrow W_H^+ q') \rightarrow W_H^+ W_H^+ q' q'$$

## Opposite sign lepton signature and 1-lepton signature (1L)

$$q\bar{q}(gg) \rightarrow Q\bar{Q} \rightarrow W_H^+ W_H^- q' \bar{q}'$$



# Heavy top/bottom production rates and signatures



$$f = 1 \text{ TeV}, \quad \kappa = 1$$

$$Br(T \rightarrow W_H b) = 0.62$$

$$Br(B \rightarrow W_H t) = 0.62$$

$$Br(t_- \rightarrow A_H t) = 1$$

$$Br(t_+ \rightarrow W b) = 0.44$$

$$Br(t_+ \rightarrow H t) = 0.19$$

$$Br(t_+ \rightarrow Z t) = 0.21$$

$$Br(t_+ \rightarrow A_H t_-) = 0.16$$

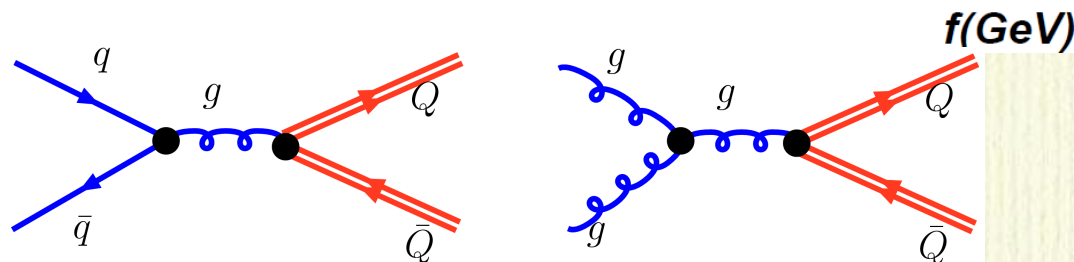
## OSL + 2b (2t) signature

$$q\bar{q}(gg) \rightarrow T\bar{T} \rightarrow W_H^+ W_H^- b\bar{b}$$

$$q\bar{q}(gg) \rightarrow B\bar{B} \rightarrow W_H^+ W_H^- t\bar{t}$$

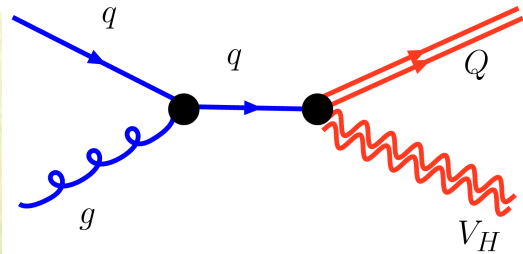
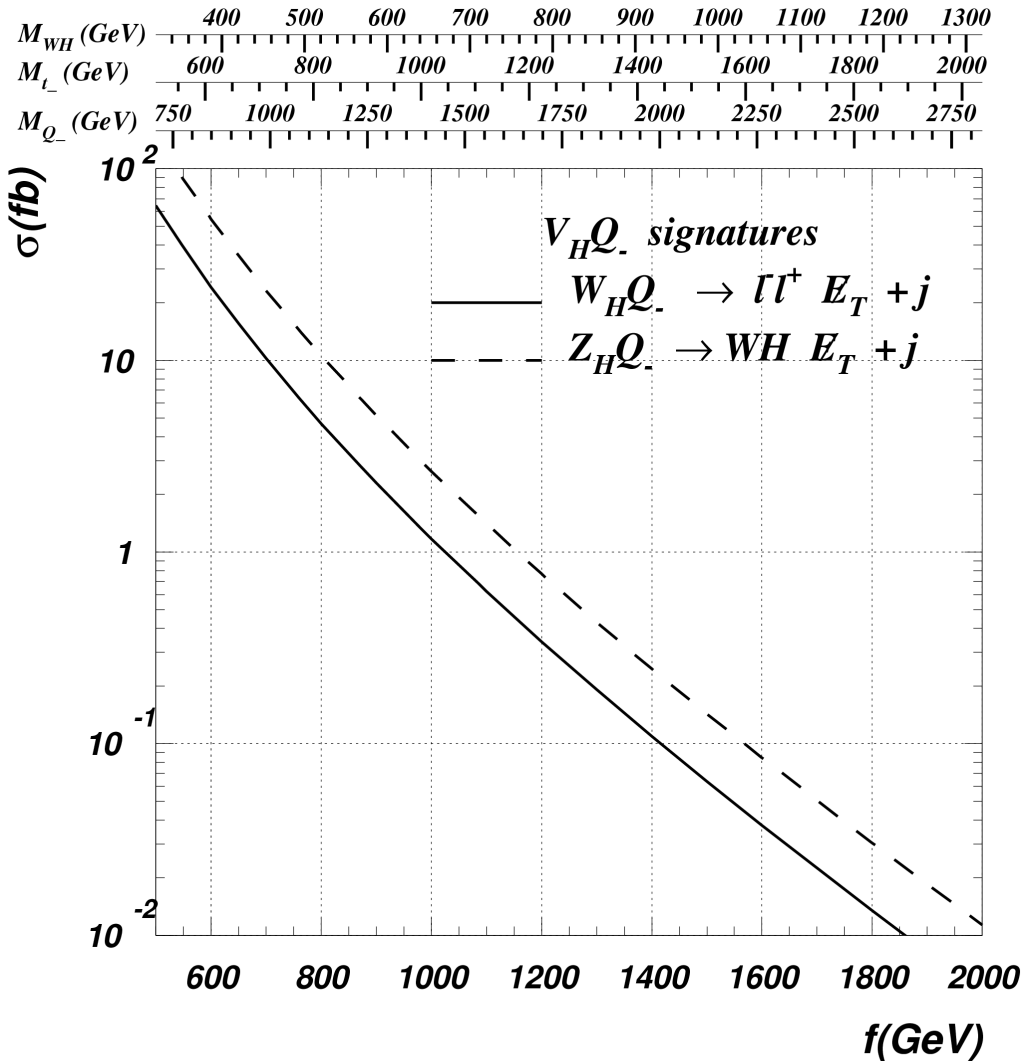
## Single top 1L + 1b signature

$$bq \rightarrow t_+ q \rightarrow W_H b q$$





# Heavy quark-vector boson associate production



$$f = 1 \text{ TeV}, \quad \kappa = 1$$

$$Br(Q \rightarrow W_H q') = 0.62$$

$$Br(W_H \rightarrow A_H W) = 1.0$$

$$Br(Z_H \rightarrow A_H H) = 1.0$$

## OSL, 1L signatures

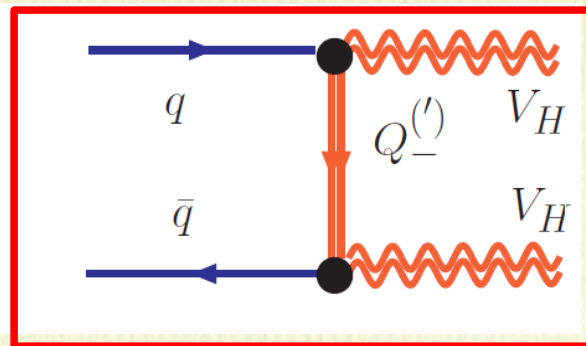
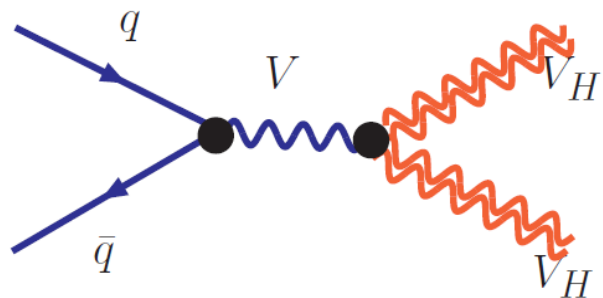
$$qg \rightarrow Q - W_H \rightarrow W_H W_H q'$$

**Indirect Higgs production  
as a result of cascade decays**

$$qg \rightarrow Q - Z_H \rightarrow W_H Z_H q' \\ \rightarrow W q' A_H A_H H$$

$$M_H = 120 \text{ GeV}$$

# Heavy vector boson pair production

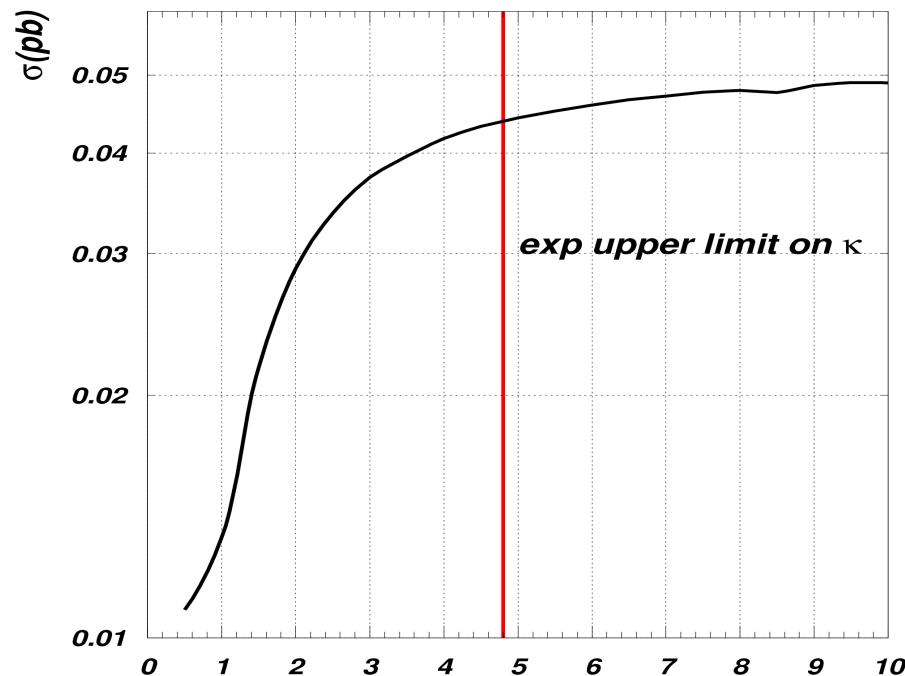
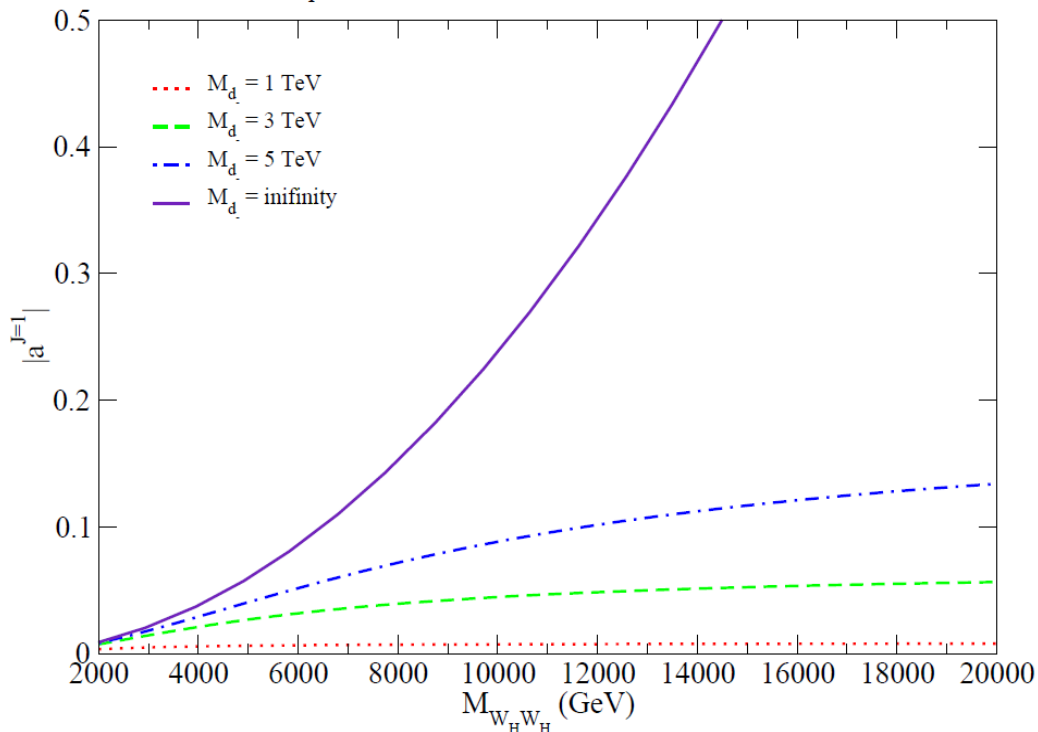


*diagram was neglected in previous studies, but crucial for the correct rate prediction, gauge invariance and unitarity*

**There is no decoupling (Hubisz et al)**  $M_Q < 4.8(f^2/1 \text{ TeV})^2 \text{ TeV}$ ,  $M_Q = \sqrt{2}\kappa f$

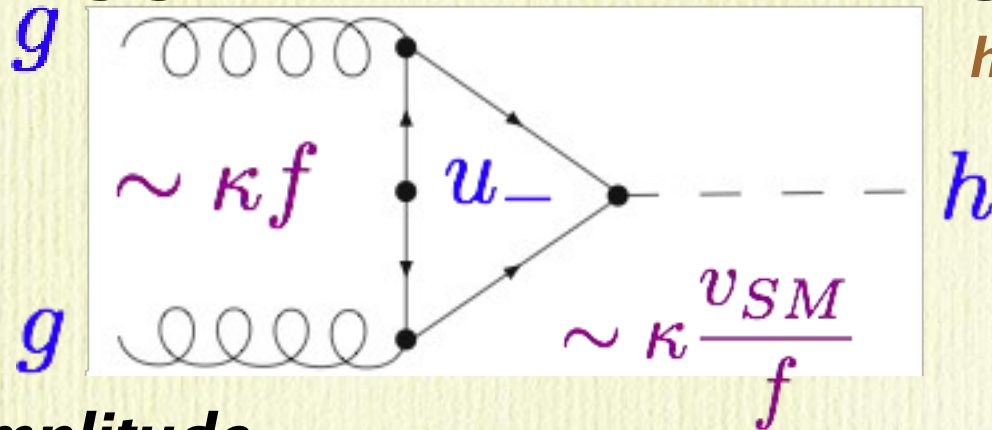
$$A^\gamma(-+) = -\frac{s_W^2 \sin \theta}{3f^2} s, \quad A^Z(-+) = -\left(1 - \frac{4}{3}s_W^2\right) \frac{\sin \theta}{4f^2} s, \quad A^{d-}(-+) = \frac{\sin \theta}{4f^2} s$$

J=1 partial wave of the sum of S-channel and T-channel



**rates were overestimated by factor 2-5**

# Important T-odd fermion contribution to Higgs production via gluon-gluon fusion



hep-ph/0602211 Chen, Tobe, Yuan

**Amplitude**

$$A(\text{T odd fermions}) \propto m_{u-} g_{hu-u-} \frac{1}{m_{u-}^2} \sim \frac{v_{SM}}{f^2}$$

**no  $\kappa$  dependence!**

**(Once  $f$  is fixed, the T-odd fermion can not decouple.)**

**Correction to the cross section**

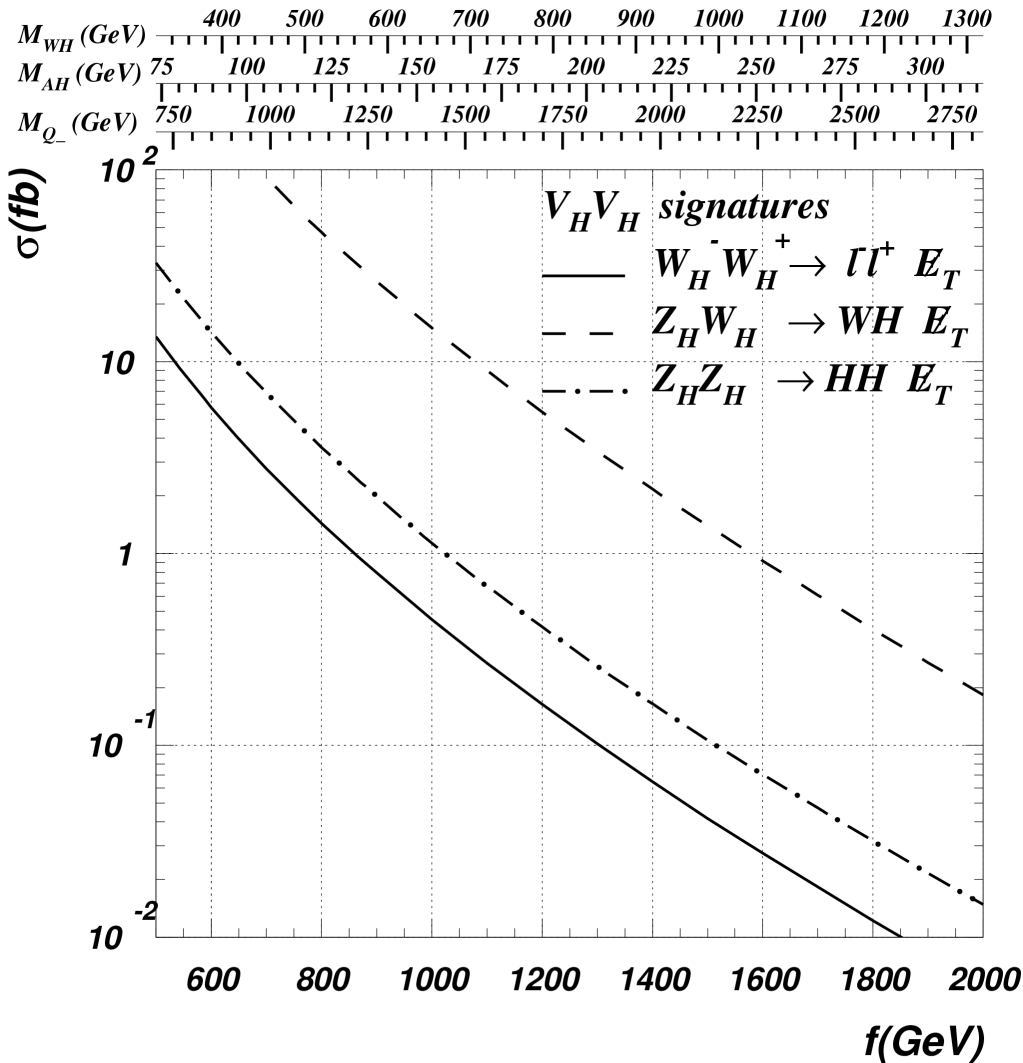
$$\frac{\delta\sigma_{gg \rightarrow h}}{\sigma_{gg \rightarrow h}^{SM}} \simeq - \left( \frac{3}{2} + \frac{3}{2} \right) \frac{v_{SM}^2}{f^2} \simeq \begin{cases} -37\% & \text{for } f = 700 \text{ GeV,} \\ -18\% & \text{for } f = 1000 \text{ GeV.} \end{cases}$$

**top sector**  $\uparrow$   $\downarrow$  **T-odd fermions**

for  $m_H < 2m_t$



# Heavy vector boson pair production



$$f = 1 \text{ TeV}, \quad \kappa = 1$$

$$Br(Q \rightarrow W_H q') = 0.62$$

$$Br(W_H \rightarrow A_H W) = 1.0$$

$$Br(Z_H \rightarrow A_H H) = 1.0$$

**OSL, 1L signatures**

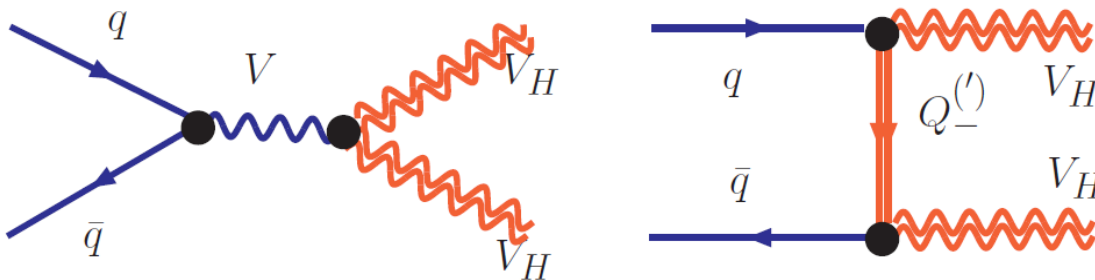
$$W_H^+ W_H^- \rightarrow W^+ A_H W^- A_H$$

**Associate Higgs production**

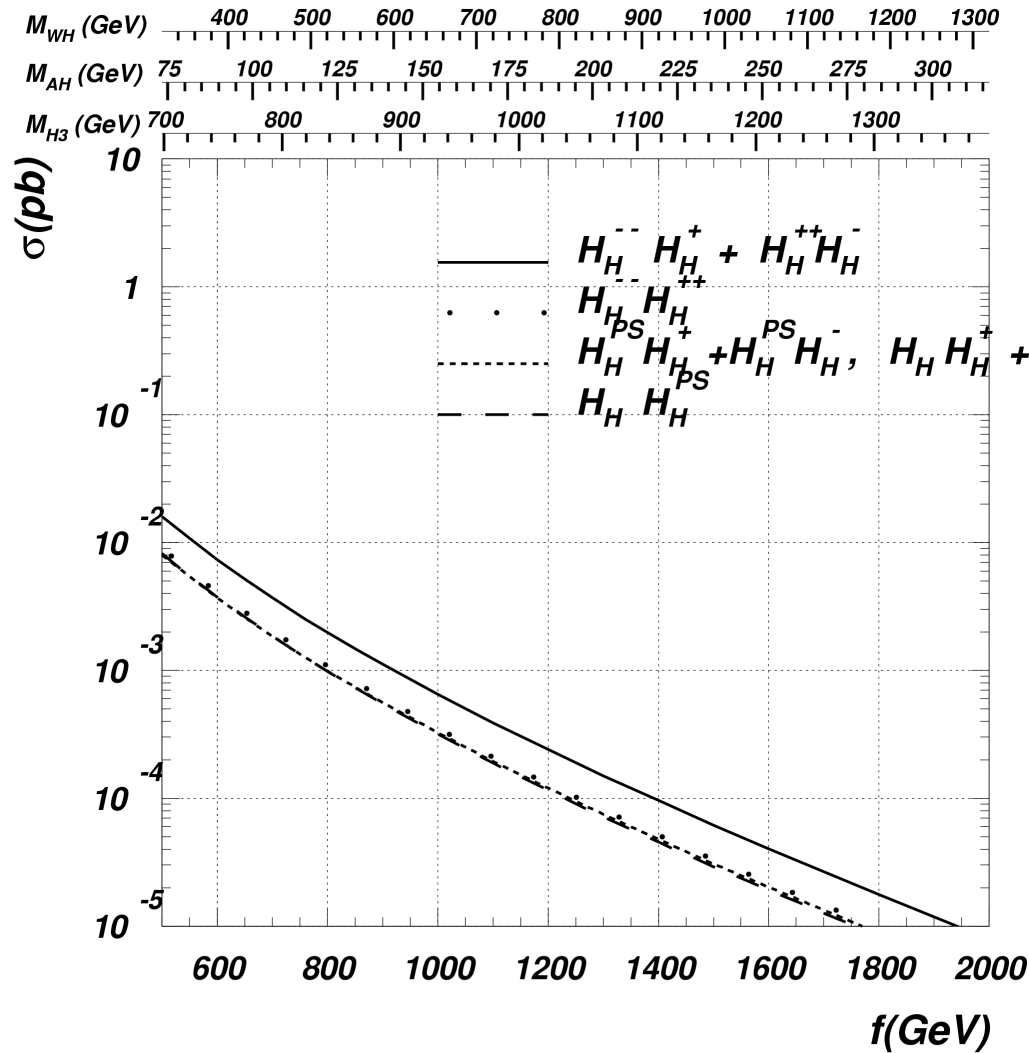
$$Z_H W_H \rightarrow H W A_H A_H$$

**Higgs pair production**

$$Z_H Z_H \rightarrow H H A_H A_H$$



# Heavy scalar boson pair production

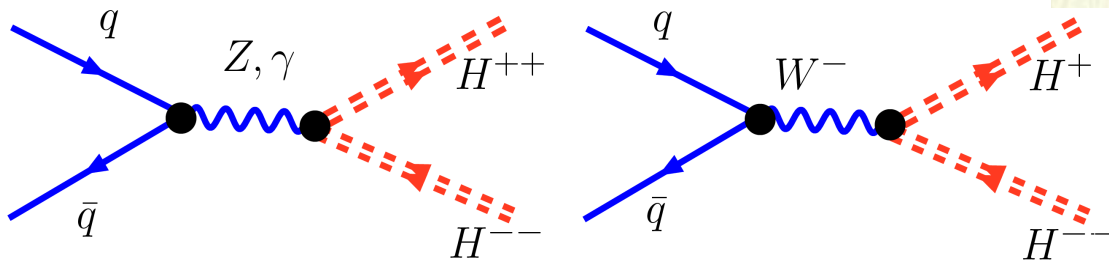


$$Br(H^+ \rightarrow A_H W^+) = 1$$

$$q\bar{q} \rightarrow H^{++} H^{--}$$

$$q\bar{q}' \rightarrow H^{++} H^-$$

**Study of 3-body tree-level decays for Heavy Higgs bosons is needed!**



# The signal observability

- + CalcHEP – PYTHIA interface is crucial for further analysis beyond the parton level
- + PYTHIA allows now to include new particles and their decay in easy fashion (thanks to Peter Skands and Sasha Pukhov)

**BLOCK QNUMBERS 90024 # WH+**

1 3 # 3 times electric charge

2 3 # number of spin states (2S+1)

3 1 # colour rep (1: singlet, 3: triplet, 8: octet)

4 1 # Particle/Antiparticle distinction (0=own anti)

**BLOCK MASS # Mass Spectrum**

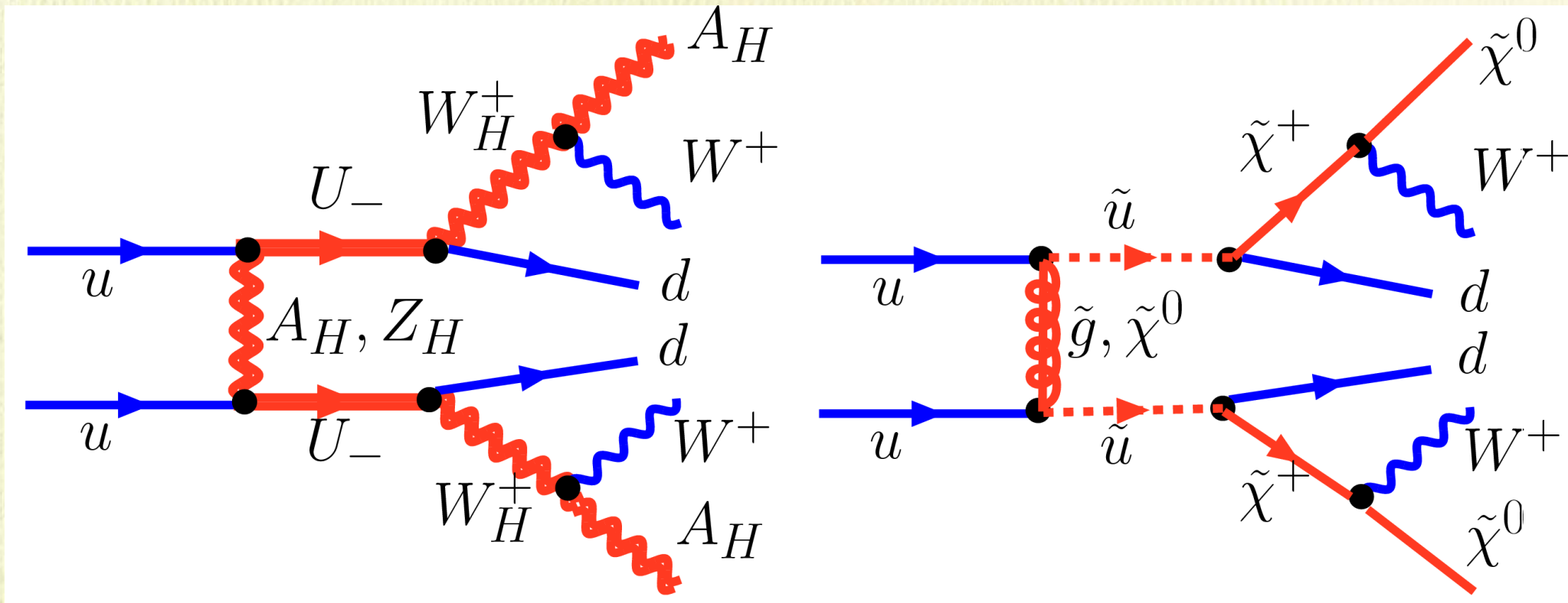
90024 5.000000E+02 # WH+

**DECAY 90024 1.000000E+00 # WH+ width**

1.0000E-00 2 24 90022 # Br(WH -> W+ AH)



# Lets look at LHT vs SUSY cascade decays



✚ Both, SUSY and LHT could give the same signature pattern

$$\lambda_1 = \lambda_2 = 1$$

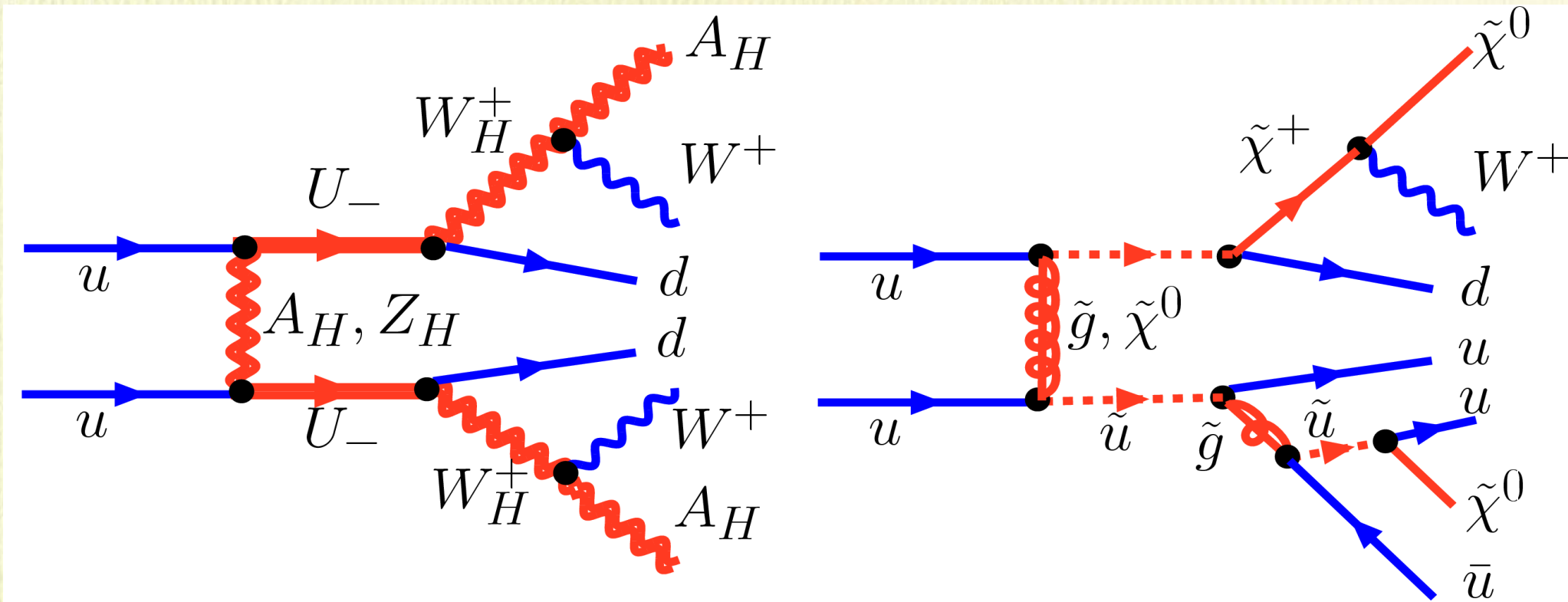
$$f = 1 \text{ TeV}, \quad \kappa = 1$$

$$Br(Q \rightarrow W_H q') = 0.62$$

$$Br(W_H \rightarrow W A_H) = 1$$

✚ One should look closely: various decay channels, spin correlations, couplings

# Lets look at LHT vs SUSY cascade decays



✚ **Glueon has no partner in LHT model!**

$$\lambda_1 = \lambda_2 = 1$$

$$f = 1 \text{ TeV}, \quad \kappa = 1$$

$$Br(Q \rightarrow W_H q') = 0.62$$

$$Br(W_H \rightarrow W A_H) = 1$$

✚ **Study of spins and couplings is quite a challenge at the LHC**

# Conclusions

- ✦ **LHT model is well motivated and leads to an exciting phenomenology at the LHC**
- ✦ **The complete LHT model has been implemented into CalcHEP, independent implementation was important!**
- ✦ **New results**
  - *all relevant LHC signatures are classified*
  - *$\kappa$  – term quark production has been suggested*
  - *new signatures, including LSL has been pointed out*
  - *Importance of non-decoupling effects: especially for heavy boson pair and higgs boson production*
- ✦ **CalcHEP-PYTHIA interface: understanding the signal observability and including spin correlations is important**
- ✦ **Relic density abundance has been evaluated for the complete model with MicroMEGAs - important constraint**



# LHT Model: Yukawa interactions

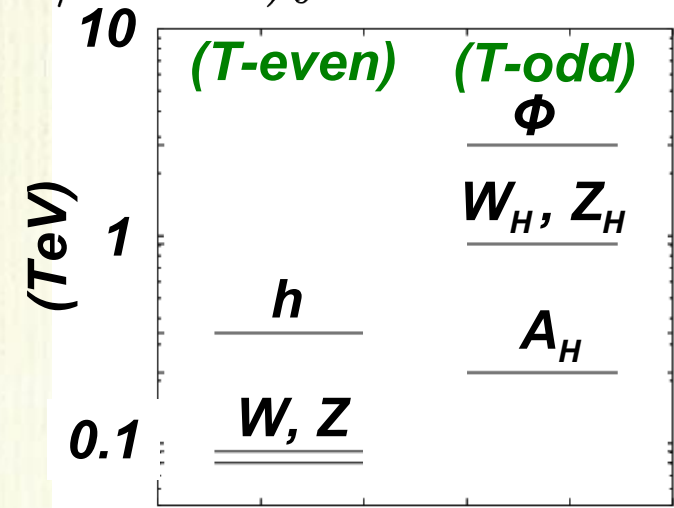
$$-\frac{\lambda_1}{2\sqrt{2}} f \epsilon_{ijk} \epsilon_{xy} \left[ (\bar{Q}_1)_i \Sigma_{jx} \Sigma_{ky} - (\bar{Q}_2 \Sigma_0)_i \tilde{\Sigma}_{jx} \tilde{\Sigma}_{ky} \right] u_{R+}$$

$$-\lambda_2 f (\bar{U}_{L1} U_{R1} + \bar{U}_{L2} U_{R2}) + \text{h.c.},$$

with  $Q_1 = (q_1, U_{L1}, 0_2)^T$  and  $Q_2 = (0_2, U_{L2}, q_2)^T$   
 giving  $t, t_+, t_-$  with  $\sin \alpha = \lambda_1 / \sqrt{\lambda_1^2 + \lambda_2^2}$   
 $M_t \simeq (\lambda_2 \sin \alpha) v, \quad M_{t-} \simeq \lambda_2 f, \quad M_{t+} \simeq (\lambda_2 / \cos \alpha) f$

$$-\kappa f (\bar{\Psi}_2 \xi \Psi_c + \bar{\Psi}_1 \Sigma_0 \Omega \xi^\dagger \Omega \Psi_c) + \text{h.c.}$$

fermion  $SU(2)$  doublets  $q_1$  and  $q_2$ :  
 $\Psi_1 = (q_1, 0, 0_2)^T$  and  $\Psi_2 = (0_2, 0, q_2)^T$   
 giving  $U_-, D_-$ , with  $M_{Q-} = \sqrt{2} \kappa f$



# SUSY LHwTP dictionary

squarks, sleptons	↔	mirror fermions
gauginos	↔	heavy gauge bosons
2 Higgs	↔	scalar triplet
gluino	↔	NONE
NONE	↔	Singlet quarks